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AIRCRAFT ANTISKID PERFORMANCE AND SYSTEM COMPATIBILITY ANALYSIS



BYRON H. ANDERSON
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TECHNICAL REPORT AFFDL-TR-70-128

FEBRUARY 1971

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The distribution of this report is limited because release of information would significantly diminish the technological lead time of the United States and friendly foreign nations by revealing formulas, processes, or techniques having a potential strategic or economic value not generally known throughout the world.



FOREWORD

The study of aircraft antiskid performance and system compatibility reported herein was performed by the Fort Worth Division of General Dynamics Corporation under U. S. Air Force Contract No. F33615-70-C-1004. The contract was initiated under Project No. 1369 "Mechanical Subsystems for Advanced Military Flight Vehicles" and Task No. 136910 "Steering and Deceleration Subsystems for Advanced Military Flight Vehicles." This study was administered under the direction of the Air Force Flight Dynamics Laboratory, Mr. Paul M. Wagner (FEM), Project Engineer.

This report describes work conducted during the period from August 1969 to August 1970. The study was performed under the project leadership of Mr. R. C. Churchill. The General Dynamics Report Number is FZM-5560. The authors wish to acknowledge the assistance of Mr. R. C. Barron, Mr. C. W. Austin and Mrs. L. J. Schnacke for their efforts in analog and digital computer programing.

The authors wish to thank Mr. Wagner for his guidance and assistance throughout the program. The cooperation of the Antiskid Engineering Department of the Goodyear Aerospace Corporation is also acknowledged. This report was submitted by the authors in September 1970.

Publication of this technical report does not constitute Air Force approval of the report's findings or conclusions. It is published only for the exchange and stimulation of ideas.

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ABSTRACT

The operation of an aircraft antiskid wheel brake control system has the potential for producing adverse aircraft dynamic behavior and structural damage. Antiskid operation is also a major influence upon stopping performance. Unless the characteristics and effects of antiskid operation can be defined, an aircraft's capability for safe, reliable and economical accomplishment of its intended usage cannot be assured. This report presents an analysis procedure for predicting antiskid operational characteristics and the inter-related effects upon the aircraft and its performance. The analytical procedure is the development of mathematical equations for a comprehensive description of the antiskid system components, the significantly influencing aircraft systems and the characteristics of the surface upon which the aircraft is operating. The mathematical description includes such considerations as landing gear dynamics, tire elasticity, brake torque response characteristics, antiskid electronic circuitry, brake hydraulic control system dynamics, runway surface profile and tire-to-runway friction characteristics. Both on-off and 'modulated" antiskid systems are analyzed. Procedures for quantitative evaluation of the influencing parameters and examples of their usage are also presented. The implementation of the analytical prediction procedure by simultaneous solution of all the mathematical equations on an electronic computer is described.

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SECTION I

INTRODUCTION

An antiskid system is provided as a part of the landing gear wheel brake control system of most large aircraft, particularly those having full power brake actuation. Aircraft operational experience has shown that an antiskid system is required because there are many occasions where the maximum available friction force between the tires and runway surface is insufficient to react the applied brake torque. For cases where excessive brake torque is applied the antiskid system functions to control tire motion so that skids are prevented and so that the associated problems and hazardous circumstances which are detrimental to safe, predictable and economical aircraft operation are avoided. The antiskid function is accomplished by a group of ancillary components which provide an automatic means for detecting and alleviating an incipient tire skid condition by controlling brake torque. An incipient skid is alleviated by temporarily reducing brake torque to a value less than the torque being produced by the friction force at the tire-runway interface. Brake torque reduction is sustained for a time interval of sufficient duration to allow the wheel to regain speed. After the wheel has regained speed, brake torque is reapplied.

The reduction and subsequent reapplication of brake torque results in an oscillatory braking force being applied to the airplane. This oscillatory force has the potential for causing adverse dynamic loading of the airplane structure, for causing directional control difficulty and for degrading the aircraft's stopping performance. Therefore, the antiskid system must control tire motion in a way such that objectionable or unsafe conditions other than those related to tire skidding are not incurred. The need for evaluating the potentially deleterious effects of an oscillatory braking force is now recognized because there have been a number of instances where failure to do so has resulted in severe operational difficulty and in some cases catastrophic landing gear failure.

The objective of this study is to develop analytical procedures and techniques for predicting aircraft antiskid operational behavior and its effects. These analysis

techniques are intended to help overcome some of the previously experienced problems or uncertainties and to provide a foundation for a comprehensive evaluation of aircraft antiskid performance and total system compatibility. It is also intended that these procedures be capable of application during the conceptual design phase of new airplanes. In the initial design of a new airplane the capabilities of various candidate equipment which might be used for stopping during the landing sequence or rejected takeoff should be evaluated with respect to the airplane's mission requirements. Factors such as stopping performance, weight, cost and reliability should be considered when the influence of the braking equipment is being examined to establish the overall effect upon the aircraft's configuration. In such an evaluation, the performance of the wheel braking system, including any applicable antiskid equipment, is a major consideration. Use of an analysis procedure whereby the effects of antiskid operation can be accurately predicted provides the means for minimizing the technical and financial risks of both the aircraft manufacturer and the aircraft user. Inaccurately predicting the wheel braking system's performance can result in an airplane design unsuited for its intended usage, a costly redesign program, or both.

This study mathematically describes the physical operation of antiskid equipment in conjunction with the airplane and its other applicable components. The basis of the mathematical relationships is the description of actual (or conceivable) hardware behavior rather than a compilation of equations relating various parameters in a desirable or compatible manner without regard to detail design features. This approach is taken to assure all influencing parameters are accounted for and to provide criteria for equipment detail design and test. Also, by examining the individual component behavior, the evaluation can include such considerations as cost and weight along with performance characteristics.

The essence of antiskid operation is the cumulative effect of a number of successive events, where the intervening occurrences and outcome of each is influenced by and dependent upon the conditions resulting from preceding events. Since these events occur quite rapidly and involve

the behavior of the aircraft and many of its components, the instantaneous condition of a very large number of variables must be continually maintained with high accuracy so that they are available when needed. Consequently, one of the major problems associated with analyzing antiskid operation is the magnitude of the computation task. It will be noted that the study has analytical components encompassing several engineering and scientific disciplines such as electronics, aerodynamics, mechanics and hydraulics. Each of the individual analytical components is often deserving of considerable more elaborate and complete treatment. However, to provide an economically feasible and comprehensible composite solution, the scope of the individual analytical components has been limited to account for only those effects or influencing factors which are of traditional interest and which are required to achieve reasonable agreement between observed operational behavior and analytical results.

SECTION II

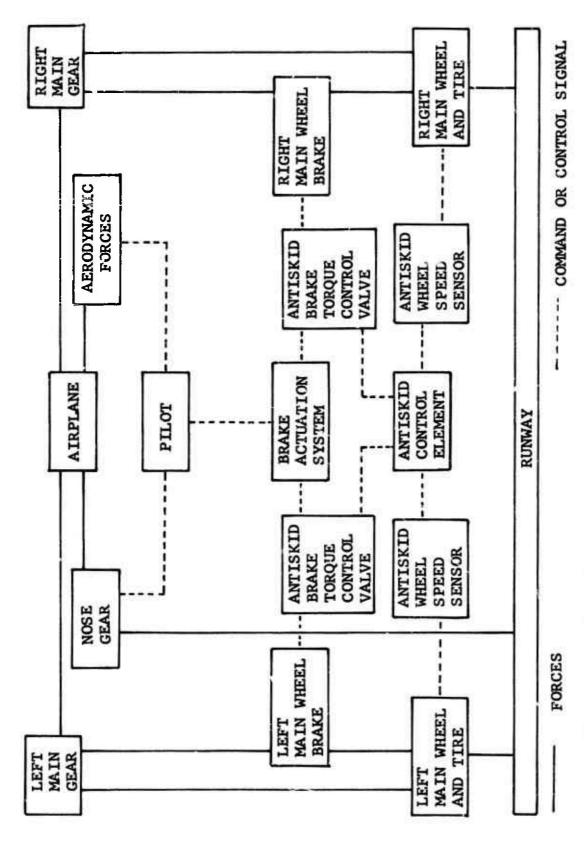
ANALYTICAL APPROACH

The analytical approach of this study is directed toward predicting the existence of adverse circumstances which have caused various problems in the past and foward providing information which is typically needed to establish detail design criteria and to define aircraft operating procedures. Specific consideration is given to providing the means for:

- (a) Establishing the magnitude and frequency of dynamic loading applied to the landing gear.
- (b) Establishing the value of the braking force which can be predictably and dependably achieved for various runway surface and aircraft operating conditions.
- (c) Determining individual component and system operational characteristics which are required so that overall aircraft performance objectives are achieved.
- (d) Establishing the effects of varying performance characteristics of individual components within the brake control system to assure no incompatibilities exist.

1. PROBLEM DEFINITION

Figure 1 is a block diagram showing the typical arrangement of an antiskid system and its relationship within the total aircraft system. This arrangement is representative of most antiskid systems in current use and the various types of airplanes on which they are installed. The major components, the significant forces and their controlling elements are shown for a single wheel main gear configuration of a nose wheel type airplane which is the usual case for fighter type aircraft. For airplanes having multiple wheeled landing gears and/or multiple landing gears the same basic relationships prevail with the addition of similar type components as appropriate.



Aircraft Antiskid Arrangement Block Diagram Figure 1.

Antiskid systems usually operate by measuring a wheel's motion, comparing the measurement to an index of acceptability and causing brake torque to be decreased or increased in accordance with some function of the difference between the measured motion and comparison index. A detailed description of the operational behavior and influence of the individual elements is presented in Section III.

Since antiskid operation is basically the control of tire motion and since the motion of a tire is determined by the forces imposed (the same as for any other object) the study of antiskid operation resolves itself into (1) defining the forces on the tire and wheel and (2) establishing the resultant effects of these forces. It is easily observed that the forces acting upon an airplane tire and wheel are the forces between the tire tread and runway surface and the forces from the airplane's landing gear and brake. The values of these forces are established by the wheel's relative position and relative motion with respect to the runway surface and to the airplane. wheel's relative motion and position is determined by considering simultaneous and interrelated actions of the aircraft and a number of its systems. The effects of the following parameters are considered in this study.

- (a) Tire circumferential deformation and its rate
- (b) Tire radial deformation and its rate
- (c) Brake torque as a function of velocity, the brake's inertia, and actuation pressure
- (d) Brake actuation pressure as a function of the actuation media's compressibility and inertia, line restrictions and elasticity, variable flow areas within valves and the actuation media's containment vessels' (lines, brake housing, valve bodies) volume
- (e) Elastic and inertia properties of the landing gear
- (f) Aerodynamic forces upon the airplane
- (g) Runway surface profile
- (h) Tire-to-runway friction coefficient as a function of relative velocity and runway surface condition including hydroplaning effects
- (i) The aircraft's inertia and control surface position including stability augmentation system effects.

2. BACKGROUND

During the initial design and system development phase for most new aircraft, it has become a customary practice to analyze antiskid operation to define its effects and thereby assure compliance with the airplane's stopping performance objectives and assure adverse dynamic loading conditions or directional control problems will not be encountered. These analyses have usually been accomplished by utilizing a set-up composed of hardware representative of aircraft components interfaced with an electronic computer (most often an analog computer). The computer is used to solve mathematical equations describing the motion of the aircraft and the landing gear, forces on the aircraft, tire and wheel motion and tire-to-runway friction, etc. The actual behavior of a laboratory set-up including such components as the antiskid control circuit, hydraulic brake valves and interconnecting lines is measured by suitable instrumentation and fed into the computer to obtain a composite solution. This analysis procedure is used because a complete mathematical computer setup requires greater computer capacity than is usually available and because an accurate mathematical description for some components such as the electronic antiskid control circuit is often unavailable.

Some antiskid analyses have been performed using an "all mathematical" approach; however, these have usually been associated with academic endeavors or a comparative evaluation of a specific device and did not account for all of the known significant influencing parameters and constraints for an actual aircraft antiskid sytem installation. While the hybrid hardware-computer analyses have often satisfied their objectives, several factors have led to a number of uncertainties for which the bounds are not adequately established, either because of great difficulty and expense or because of inadequate knowledge. uncertainties tend to obscure the analysis results and generally detract from their credibility. The most significant factor causing uncertainty is that the usual definition for the friction force between the tire and runway surface does not account for all the observed variations. A second factor is the analytical limitations

associated with the use of actual hardware. The use of actual hardware dictates that the analysis be performed "real time" and complicates or prevents examination of some parameter variations. Since some parameters have a very high rate of variation with respect to time, the outputs from a "real time" solution can be extremely difficult to observe and interpret. Also, the instrumentation used to interface the hardware with the computer introduces additional variables to an otherwise very complex system. This study is intended to provide the means for overcoming these problems and for minimizing uncertainty.

3. ANALYTICAL PROCEDURE AND RATIONALE

The evaluation of antiskid operation is conducted using a modular analysis technique whereby the problem is divided into a number of modules or component parts, each having defined inputs and outputs such that the outputs from one or more components are provided as inputs to other By combining all the analytical components, a composite simultaneous solution is obtained. The analytical modules are formulated so as to correspond to various aircraft components or systems. The modules can be arranged in a number of combinations representative of a variety of aircraft configurations. In addition, the modular approach allows maximum computation flexibility in that changes can be made within individual modules without affecting the overall analysis program. The predominate influencing factors governing the choice of each analytical component's content and treatment are experience and judgment as to the degree of detail which is required to accurately establish the timing or relative sequence of significant events. Each analytical module is formulated so that particular effects or circumstances can be examined and so that its outputs will supply the information needed as inputs to other modules. It will be noted that some relatively insignificant parameters must be considered to achieve mathematical continuity. To exemplify the analysis procedure antiskid operation for a fighter type aircraft having a single wheel main landing gear arrangement is evaluated. All of the analytical components, except for the antiskid control circuit, are expressed in general terms and could be applied to almost any airplane. The antiskid control circuits considered are those specifically utilized on the F104 and the F-111.

For the case of the F-104 on-off antiskid control circuit, the wheel speed input signal is arbitrarily adjusted to account for the difference between the F-104 and F-111 tire sizes. All parameter values used to prove the validity of the analysis procedures are those associated with the F-111 airplane so that the analytical results can be compared to available records of actual aircraft operation. To analyze other control circuits will require that their mathematical models be formulated and incorporated in the composite solution. The detail assumptions and procedures for establishing parameter values are presented in Section III within the description of each analytical module.

4. PARAMETER INVESTIGATIONS

The basic intent of this study is to account for the influence of parameters and effects which have been identified as responsible for previously experienced operational difficulties or which are otherwise known to significantly affect antiskid performance. Such items as tire radial and circumferential spring rate. the characteristics of brake torque variations with velocity and actuation pressure, brake chatter and squeal, hydraulic system response as affected by linesizes, component flow restrictions and metering valve characteristics, the airplane's response to aerodynamic forces and runway roughness, landing gear elastic characteristics and the characteristic of the tire-torunway friction force variations are given particular attention. The treatment of most parameters is that which experience has proven gives satisfactory results. However, to overcome some previous antiskid evaluation analytical difficulties associated with tire-to-runway friction and hydraulic system operation and to examine the effects of brake chatter and squeal, some preliminary investigations were conducted.

A. Brake Investigation

Since an antiskid system controls brake torque implicitly by controlling brake application pressure, the hysteresis in the brake's torque response to pressure changes must be accounted for. hysteresis results from inertia of the brake moving parts, friction forces on the actuating pistons due to hydraulic seals and piston side loading, and from friction in the splined connections between the brake discs and the wheel and between the discs and the torque tube. To evaluate a typical brake's torque response to rapidly changing actuation pressure and to briefly investigate brake chatter and squeal effects, a relatively complex six-degree of freedom brake mathematical model was initially formulated. In this model six discs were treated as separate masses with individual axial position, velocity and acceleration computation, non-linear keyway and piston friction as a function of axial velocity, non-linear brake lining friction as a function of rotational velocity, and variable

elasticity to simulate the effects of disc warpage. The model was set up on an analog computer and subjected to step input pressures and to sinusoidal pressure oscillations of various amplitudes and mean values at frequencies from 10 cps to 1000 cps. computer setup also included rotational and longitudinal elastic deformations within the tire and brake supporting structure. The set up was operated at 1/100 real time and at a number of aircraft velocities. By suitable choice of elastic, damping and friction characteristics, both chatter and squeal were produced at low aircraft speed. Using a keyway friction coefficient varying from 0.15 at zero velocity to 0.10 at high velocity, it was found that the brake torque oscillated in response to oscillating pressure at all frequencies up to 1000 cps. At low brake rotational velocities (20-40 rad/sec) with low frequency pressure oscillation where the minimum pressure was the value for full brake release, the brake torque oscillation had considerable deviation from a sinusoidal variation. The phase lag between instants of maximum torque and maximum pressure varied from 15-20 degrees at 10 cps to 40-50 degrees at 100 cps to 110-150 degrees at 1000 cps. The oscillatory component of the brake torque exhibited appreciable attenuation at high frequency such that the amplitude at 1000 cps was about 20 percent of the 10 cps amplitude with constant pressure amplitude. Even though there was noticeable phase lag in the pressure-torque characteristic, it was found that throughout the 10-1000 cps frequency range there was no appreciable phase difference between the displacement, velocity or acceleration of the individual discs. Therefore, a simplified model was formulated where all the discs were treated as a single mass. The simple model was set up and tested on the analog computer where its torque response to varying pressure was confirmed to be identical to the more complex model. The more simple brake mathematical model is used in this study and is described in Section III. A significant and somewhat unexpected finding of this investigation is that a typical airplane brake can be expected to have appreciable torque response when subjected to pressure oscillations in the 100-200 cps frequency range as might be associated with a hydraulic line resonance.

B. Tire-to-Runway Friction Investigation

The usual and relatively arbitrary function relating coefficient of friction to tire or wheel slip ratio has been used in most prior antiskid analyses to establish the tire-to-runway friction force. While there are many circumstances where the slip ratio approach is adequate for examining most of the aspects of antiskid operation, a number of difficulties and undesirable effects are associated with its use. A major analytical problem is that examination of antiskid operation at low aircraft speed is prohibited because the slip ratio computation would require division by zero. In addition, the large differences in the friction coefficientslip ratio characteristic variation which have been observed for changes such as aircraft speed, y away surface condition and tire properties lead to a number of uncertainties, particularly with respect to stopping performance predictions.

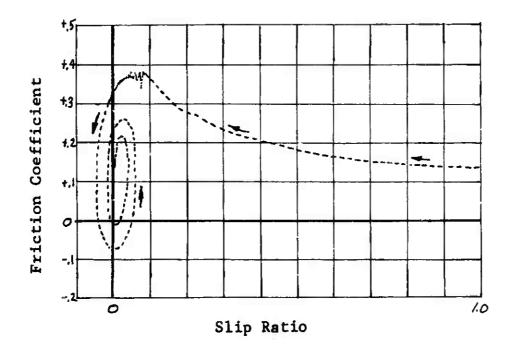
To satisfy the objectives of this study, it was considered necessary that a mathematical description of the tire-to-runway friction coefficient be used which would not have the above undesirable qualities. To develop such a description, several hypotheses were formulated considering the tire's elastic deformation and its response to ground friction forces. Effects such as tread stretch, tread circumferential displacement and variation of relative velocity between tire tread particles and the runway surface throughout the footprint were examined mathematically. Because of the extremely complex nature of a tire's elastic behavior, these examinations quickly lead to an analytical task at least equal to the scope of the entire antiskid study. Even though this subject deserves further investigation, a more simple hypothesis accounting for most known variations and effects was adopted to comply with this program's objectives. For the purpose of this analysis, it is assumed that: (1) the tire tread is a perfectly flexible inelastic belt with radial and torsional elastic attachment to the wheel. (2) All tread particles within the footprint have the same relative velocity with respect to the runway surface and the coefficient of friction between the tire tread and runway surface is a function of relative

velocity. (3) The function defining the friction coefficient variation with relative velocity is that established by testing a tire in a full skid.

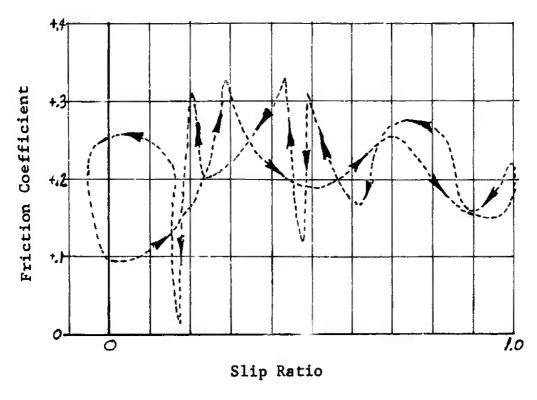
A description of the tire and wheel mathematical model utilizing these assumptions is contained in Section III. The equations listed show that the relative velocity between the tire footprint and runway surface is determined by computing the tread belt's C. G. (center of gravity) translational velocity component parallel to the runway surface and the angular velocity of a point on the tread belt about the C. G. The footprint horizontal velocity component relative to the C. G. is computed from the angular velocity and an apparent rolling radius. The apparent rolling radius is the unbraked rolling radius plus a fraction of the tread belt's C. G. horizontal displacement with respect to the wheel's rotational axis. The net footprint velocity relative to the runway surface is then the sum of the tread belt C. G. translational velocity and the velocity of the footprint relative to the tread belt C. G. The mathematical expression for friction coefficient as a function of relative velocity is of exponential form with coefficients chosen to fit test data.

This model was set up on an analog computer and examined statically and dynamically. Statically, the friction coefficient versus slip ratio (with respect to the wheel) characteristic varies with axle velocity in accordance with observations. This observed variation is that the slip ratio value associated with maximum friction coefficient is greater at low axle velocity than at high axle velocity, and the value of friction coefficient at maximum slip ratio decreases as axle velocity increases. Figure 2A shows friction coefficient versus slip ratio (with respect to the wheel) recorded dynamically during an analog computer run with an ON-OFF antiskid system. Figure 2B is a similar curve recorded dynamically during wheel spinup from a full skid. For both cases shown on Figure 2 axle velocity is constant.

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(B) Recorded During Wheel Spin Up



(A) Recorded During On-Off Antiskid Operation

Figure 2 Friction Coefficient Versus Wheel Slip Ratio

C. Hydraulic System Investigation

From experience gained in conjunction with practically all antiskid development programs, it is generally accepted that one of the more predominate influences upon antiskid operation and aircraft stopping performance is the time lag between the antiskid control device's command for a brake torque change and the actual brake torque response. Hydraulic flow restrictions and the response characteristics of the antiskid control valve and other hydraulic system elements are responsible for most of this time lag. In an attempt to minimize the effects of the time lag many antiskid control devices actually issue commands in anticipation of a predicted circumstance. Confident prediction of antiskid overall operational effects including the resultant airplane stopping performance requires that the hydraulic time lag be accurately accounted Therefore, to comply with the objectives of this study, a preliminary exploration was conducted to establish a suitable mathematical model permitting evaluation of antiskid control valve and pilot's metering valve response characteristics and such effects as hydraulic line resonant oscillation. During these explorations the operation of the pilot's metering valve, antiskid control valve and the hydraulic line connecting the control valve to the brake were examined. In each case several different mathematical descriptions were formulated and investigated on an analog computer.

For both the pilot's metering valve and antiskid control valve mathematical descriptions accounting for all component characteristics of an actual physical device and simpler descriptions eliminating spool mass considerations were examined. While by suitable choice of parameter values either mathematical model can produce an accurate description, the second order equations resulting from consideration of spool mass cause analytical difficulty because the inertia is very small in comparison with hydraulic pressure and spring forces. These very high gain second order systems necessitate very rapid integration; therefore, using the "massless" first order equations is highly desirable to achieve

computation economy. In Section III the pilot's metering valve description (a part of the hydraulic system) is the simpler first order system while the control valve equations account for spool mass. This approach is taken to permit easy recognition of the relationship between the control valve's physical construction and its performance characteristics. While having the same facility for the metering valve is desirable, it was considered analytically too extravagant. A metering valve having satisfactory performance, by whatever physical means it is achieved, will exhibit behavior in accordance with the "massless" equation.

To explore hydraulic line resonant oscillation and "water hammer" effects, a ten element hydraulic line model (ten degree of freedom) was initially formulated and examined on an analog computer with On-Off antiskid operation at one hundredth real time. This model produced very excellent results; however, the low intensity of the higher frequency harmonics (above 100 cps) showed that a more simplified model would probably be satisfactory. Accordingly, a single degree of freedom model was formulated and tested in the same manner as the ten element model. For the purpose of antiskid evaluation, the single degree of freedom model gave satisfactory results and is described in Section III.

SECTION III

DEVELOPMENT OF MATHEMATICAL MODELS

This section is devoted to the exposition of mathematical models for each of the following total system components:

- 1. Brake System
- 2. Hydraulic System
- 3. Airplane System
- 4. Wheel and Tire System
- 5. Wheel Speed Sensor
- 6. Antiskid Control Circuit
- 7. Antiskid Control Valve
- 8. Horizontal Tail Control
- 9. Runway System

For some of the system components alternate models are provided. These alternate models are listed alphabetically within each section. For example, 3a describes an airplane system modeled as a laboratory flywheel, 3b describes an airplane which has three degrees of freedom, and 3c describes an airplane with six degrees of freedom. Each component model is discussed as a self-contained unit without any particular reference to the total system and each model, in general, contains its complete mathematical description such that it is essentially immune to changes within other models of the total system.

Format and Convention Useage

The presentation of the various sytems follows a common format. Each system discussion begins with an introductory explanation of its function or its characteristics relevant to antiskid operation. Following this introduction is the main body of the discussion under the heading, "A. Mathematical Description," containing the derivation of the equations that describe the system dynamically. This section is concluded with an equation flow diagram showing the relationship among the various system equations. A final discussion follows under the heading, "B. Parameter Evaluation," which sets forth methods of determining the values of the constants appearing in the system equations. The system presentation

closes with a "Table of Parmeters" which lists all of the system variables and constants.

The flow diagram which appears at the end of Section A is provided principally as an aid in the preparation of the digital computer program which solves the system equations. This flow diagram could also be used for an analog solution although other flow diagram arrangements would be more efficient for that purpose. The following conventions apply as to the usage of the flow diagrams: The triangles outside the enclosing phantom line denote variables which are used as inputs and outputs to other systems. The numbered rectangles refer to equations within the system. As an example, in Figure 5 the rectangle numbered 9 indicates that Ter is a function of Us and Fa and that the equation that gives the exact relationship is equation 1.9. No constants are shown in these diagrams. The triangles denoting integrators do not always contain an equation number. If the input to an integrator is \dot{X}_P and its output is $x_{\rm P}$, then the equation is implied. Thus, as in Figure 63, if the input to an integrator is R4 and the output is UR4, then the equation $MR4 = \int R_4 dt$, or equivantly, MR4 = R4. is implied. Because of the size of the six degree airplane system, the flow diagram in Figure 32 is slightly different. Its use is strictly limited to the digital program generation. It says that all equations within one block must be written before proceding to the next block. Thus, the first variables to be solved for are Zsw, Zsw, Yoln, ..., Sml. After this F_{VN} , F_{LN} , \cdots , Z_{GLR} are solved for. After this X_{AXL} , X_{AXL} , ..., F_{NN} etc.

The "Table of Parameters" is a listing of all variables and constants found in the equations of that system. Each variable is identified by its symbol, description, units, and "Type." The "Type" is listed as v, v(i), and v(o) depending on whether the variable is only used within the system, is received as an input from another system, or is an output to another system. Each constant is identified by its symbol, units, description, "type," and value. The "type" for each constant is always "c" and its value is that used with the F-lll antiskid system.

Table 1 lists the mathematical conventions utilized throughout this study.

Table 1 Explanation of Mathematical Convention

Convention	Description
×	A dot over a variable denotes differentiation with respect to time
Computer Notation	All variables are expressed in a form to harmonize with Fortran character utilization. Thus a variable W_{TK} would appear as WTE Also, in general, the following practice is adhered to. If X_{TT} is a variable, then XTT is its Fortran form. The symbol for \dot{X}_{TT} is XTTD. The symbol for \ddot{X}_{TT} is XTTDD. The initial condition is denoted by adding 0 (zero). Thus \dot{X}_{TT} at time \blacksquare 0 is denoted by XTTDO.
Z _{GD} < %>	The brackets "<> " are used exclusively to denote the position of a function argument. The script z is used to denote an arbitrary variable. The parentheses "()" are normally used to denote multiplication.
Parameter Type	Within each table of parameters is a column which lists the parameter "type."
	v a variable
	C a constant
	v(o) a variable used as output to another system.
	v(i) a variable received as an input from another system.

Table 1 Explanation of Mathematical Convention

Description	
For symbols appearing in equations the following conventions are used.	
I = Capital "i"	
= One	
<pre>♂ = Capital "Oh"</pre>	
O = Zero	
₹ = Capital "zee"	
2 = Two	
⊖ = Greek letter "Theta" but is treated in Fortran as capital .	
Placing a parameter symbol between two vertical bars denotes the absolute value of the parameter. The absolute value of a signed number N is defined as N when N is positive and as -N when N is negative. For example: 3 = 3 and -3 = 3.	
The braces preceded by "MIN" or "MAX" denote the value of the least (or largest) of the constant or the parameters enclosed within the braces.	

1. BRAKE SYSTEM

The conventional airplane brake consists of a series of discs which are alternately stators and rotors. The stators are restrained from rotating about the axle by splines or keyways. The rotors are similarly connected to the wheel and hence rotate with the wheel and tire. The brake torque is produced by axially compressing the disc stack; usually by hydraulically actuated pistons. Many brakes use return springs to release the brake stack against the return pressure of the hydraulic system.

A. Mathematical Description

In this analysis Xpwill denote the brake piston linear displacement. The pistons, rotors, and stators are treated as a single mass system in the axial mode (Xp direction). The forces acting on the brake mass in the axial mode are:

- a. Brake actuation force: equals(brake pressure) x(piston area)
- b. Force due to axial restraint
- c. Keyway friction force
- d. Brake piston seal friction force
- e. Brake return spring force
- f. Brake piston bottoming force

Figure 3 shows the brake system and the forces acting in the axial mode. Each of the axial forces is established as follows:

a. Brake Actuation Force

The brake actuation pressure P_{θ} is received as an input from the hydraulic system. The brake actuation force is given by P_{θ} $A_{\theta P}$, where $A_{\theta P}$ is the total brake piston area.

b. Force due to Axial Restraint

The axial restraining force reflects the elasticity in the brake discs, the back plate, and the piston housing and is a function of their cumulative displacements. A way to derive this characteristic is from a curve of brake volumetric displacement vs. brake pressure. This characteristic does not include friction or return spring effects.

Let Fp denote the force due to axial restraint. And be defined by

$$(1.1) \ F_{B} = F_{B1} + F_{B2}$$

$$(1.2) \ F_{B1} = \begin{cases} C_{B1} (X_{P} - S_{B1}) + D_{B1} \dot{X}_{P} & \text{if } X_{P} \ge S_{B1} \\ o & \text{if } X_{P} < S_{B1} \end{cases}$$

$$(1.3) \ F_{B2} = \begin{cases} C_{B2} (X_{P} - S_{B2}) + D_{B2} \dot{X}_{P} & \text{if } X_{P} \ge S_{B2} \\ o & \text{if } X_{P} < S_{B2} \end{cases}$$

c. Keyway Friction Force

Let the keyway friction characteristic be defined by a function, $G_{\textbf{F}}$, where:

$$(1.4) G_{F} = \begin{cases} 1.0 & \text{if } \dot{X}_{P} \stackrel{>}{=} V_{FS} \\ G_{FM} + (1 - G_{FM}) \dot{X}_{P} / V_{FS} & \text{if } V_{FS} > \dot{X}_{P} > 0 \\ 0.0 & \text{if } \dot{X}_{P} = 0 \\ -G_{FM} + (1 - G_{FM}) \dot{X}_{P} / V_{FS} & \text{if } 0 > \dot{X}_{P} > V_{FS} \\ \frac{1}{10} + V_{FS} \stackrel{>}{=} \dot{X}_{P} \end{cases}$$
wheel

$$F_{BR}$$

$$F_{B$$

Figure 3 Forces Acting on the Brake Discs

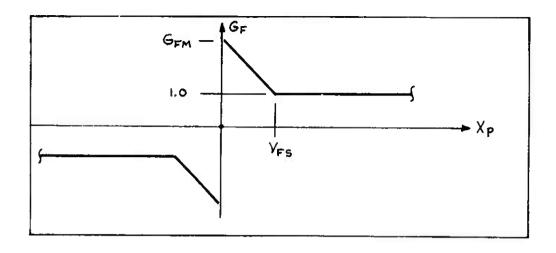


Figure 4 Keyway Friction Characteristic

The brake torque, T_{87} , is tranferred to the wheel and tire through the rotor keyways. Torque, T_{87} , is also transmitted to the axle. The major portion is transmitted through the stator keyways. The remaining portion of the torque is transmitted as piston side loading which results from friction between the pistons and the pressure plate. Let $100~H_{81}$ denote the percentage of brake torque transferred through the stator keyways and let $100~H_{82}$ denote the percentage of torque transferred through the pistons. Naturally, $H_{81}+H_{82}=1$. The normal force on the stator keys is thus $H_{81}/I_{81}/R_{81}$, while the normal force on the rotor keys is I_{81}/R_{80} . The total keyway friction force is then given by

d. Brake Piston Seal Force

Let F_{oR} denote the seal friction force. Then

e. Brake Return Spring Force

The piston return force Fee is given by

f. Brake Piston Bottoming Force

In the brake released condition, an axial force is developed between the pistons and housing to balance return spring preload. This piston bottoming force is defined as:

This concludes the discussion of the axial brake forces.

Let R_{NR} be the number of rotors. Let W_{B} be the relative angular velocity between the rotors and stators as received from the wheel and tire system. The brake torque T_{BT} is then given by

Where Ma is:

(1.10)
$$ll_{\theta} = \begin{cases} ll_{\theta}, + ll_{\theta} e^{-\alpha_{\theta} V_{\theta}} & \text{if } V_{\theta} > 0 \\ 0 & \text{if } V_{\theta} = 0 \\ -ll_{\theta}, - ll_{\theta} e^{-\alpha_{\theta} V_{\theta}} & \text{if } V_{\theta} < 0 \end{cases}$$

Where V_B is:

Summing the forces in the axial direction yields:

In Equation (1.12) $W_{\theta E}$ is the brake mass which experiences axial motion. Generally, $W_{\theta E}$ is the brake heat sink mass. Figure 5 shows the relationship of the brake system equations. Table 2 lists the system parameters.

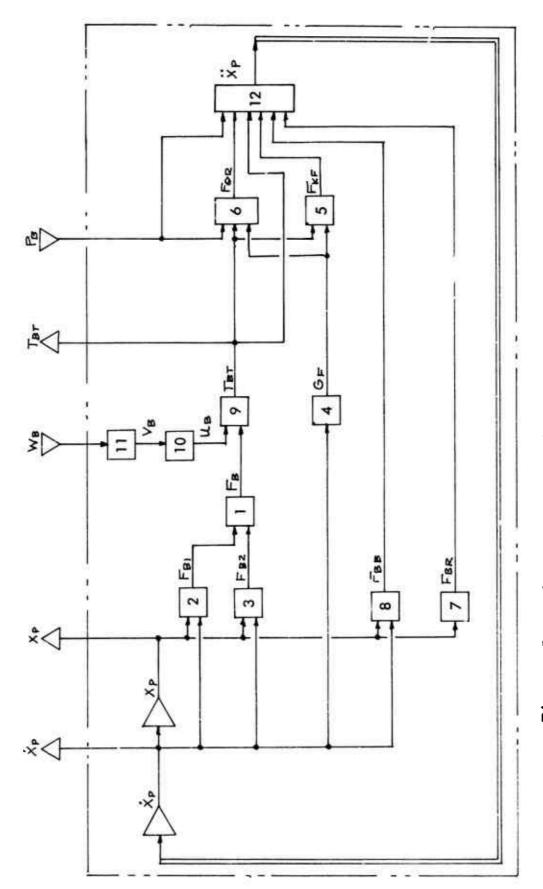


Figure 5 Brake System Equation Flow Diagram

B. Parameter Evaluation

Figure 6 shows a plot of brake piston displacement as a function of brake application pressure for a new brake.

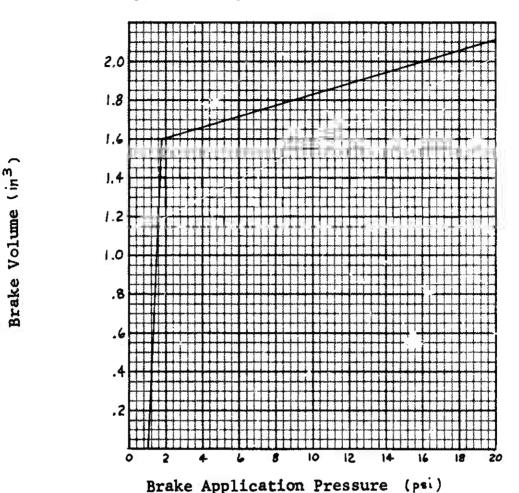


Figure 6 Brake Pressure Volume Characteristic

Assuming that no frictional effects are present, C_{BR} and C_{BI} can be derived as follows: Since the initial slope is due to spring return force only, then

(1.13)
$$C_{BR} = \left(\frac{\Delta P}{\Delta V}\right) A_{BP}^{z} = \left(\frac{80}{1.6}\right) (13.3)^{z} = 8850 \text{ lb/in}$$

From the other slope on the curve,

(1.14)
$$C_{BI} = \left(\frac{\Delta P}{\Delta V}\right) A_{BP}^2 = \left(\frac{1420}{.4}\right) (13.3)^2 - 8850 = 6.20 \times 10^5 \text{ lb/in}$$

For a new brake CBz = 0.

Assuming that the discs all move together, since the heat sink weight is 138 LBM, then $W_{6E} = 138/386 = .358$ LBF SEC²/IN. The natural frequency is then $W_{0} = \sqrt{\kappa/m}$ or $W_{0} = \sqrt{(6.2 \times 10^{5})/(.358)} = 1315$ RAO/SEC Assuming that $M_{0} = .01$ (see page 117),

(1.15)
$$D_{81} = \frac{\gamma C_{81}}{\omega_n} = \frac{(.01)(6.2 \times 10^5)}{(1315)} = 4.71 |bf sec / in$$

It is assumed that $X_p = 0$ when the brake pressure is 100 psi. Thus

(1.16)
$$F_{8P0} = A_{8P} P_8 = (13.3)(100) = 1330 16F$$

Since the brake piston displacement is 1.55 IN³ before the brake discs come into contact, then $S_{8l} = 1.55/13.3 = .1165$ in.

Since the F-111 brake has 8 stators with 14 rubbing surfaces, H_{81} cannot be greater than 1/14. A conservatively high value of H_{81} = 05 has been assumed and it follows that H_{82} = .95.

The brake piston seals are equivalent to MS28775-219. The seal friction force is established using the procedures described in Reference 4. The seal sliding friction force is a function of rubber compound hardness, amount of installed compression, length of rubbing surface, seal groove projected area and applied hydraulic pressure. For the MS28775-219 size seal having 10 percent installed compression and 70 degree Shore A hardness the sliding friction force is 2.88 lbf plus 0.02 lbf per psi applied pressure per seal. There are 10 pistons in the brake housing; therefore,

(1.17)
$$H_{OFC} = (10)(2.88) = 28.8$$
 lbf

(1.18)
$$HOFP = (10)(0.02) = 0.20 |bF/P5|$$

Conservatively high values for the friction coefficients $\mathcal{U}_{\mathcal{K}}$ and $\mathcal{U}_{\mathcal{KP}}$ are estimated as $\mathcal{U}_{\mathcal{K}}=15$ and $\mathcal{U}_{\mathcal{KP}}=.10$. G_{FM} is estimated to be 1.50.

Values for the following brake dimensional characteristics are then from the appropriate brake component drawings: $R_{\rm BT}$ = 4.40 IN, $R_{\rm BT}$ = 6.25 IN, and $R_{\rm BD}$ = 8.25 IN.

Observations of braking stops indicate that for an average F-111 brake lining,

$$\alpha_{\rm B}$$
 = .03 SEC/IN

Table 2 Brake System Parameters

Авь	TYPE	VALUE	ONITS	DESCRIPTION
	ပ	13.3	IN	Piston area per brake
8	ပ	0.03	SEC/IN	Brake lining friction parameter
CBI	ပ	6.2 × 105	LB/IN	Brake Disc spring rate characteristic
C 182	ပ	0.0	LB/IN	
Cab	ပ	1.0 × 10 ^S	LB/IN	Bottoming spring rate
Cea	ပ	8850.	~	Return spring rate
م ص	ပ	4.71		Rrake Disc damping coeff
DB2	U	0.0	LB SEC/IN	June Drac dempring corr.
Das	υ	400.	LB SEC/IN	Bottoming damping coeff.
u.	>		LB	Force between brake plates
الـ ا	>		LB	\ F F + F
~ L_	>		LB	7881. 9.∫
1 B	>		LB	Bottoming Force
1 de 1	>		LB	Return Force
F 80	ပ	1330.	LB	Return force when $Xp = 0$
) \ \ \ \	>		LB	Keyway friction force
T &	>		1b	"O-ring" friction force
O.	>			Friction breakout function
GFM	O	1.50	Dimensionless	Ratio of breakout friction to
				running friction
HBI	ပ	0.05	Dimensionless	Fraction of brake torque removed
				by stator keys
Hisz	ပ	96.0	Dimensionless	Fraction of brake torque removed
				thru pistons
HOFC	ပ	28.8	LBF	O-ring friction
Horp	O	0.20	LBF/PSI	

Table 2 (Continued)

SYMBOL	TYPE	VALUE	UNITS	DESCRIFTION
~	v (i)		LB/IN	Brake pressure
R H	U	4.40	IN	er
S. S.	ບ	8.25	NI	Radius to center of press on rotor key
Ret	U	6.25	IN	Radius to piston centers
N N N N N N N N N N N N N N N N N N N	O	7	Dimensionless	Number of rotors
S	ن	.1165	NI	Displacement of piston to engage CB
				Spring Rate
582	U	0.0	IN	Displacement of piston to engage Caz
				Spring Rate
SBB	U	0.0	IN	Value of Xp when bottoming occurs
1	(0)^		IN LB	Brake torque
U.B	>		Dimensionless	Brake lining friction coeff.
U, B:	υ	0.15	Dimensionless	D. 10 1 2 1 2 1 2 1 2 2 2 2 2 2 2 2 2 2 2
Lle2	U	0.10	Dimensionless	brake iining iriction characteristic
CL _K	υ	0.15	Dimensionless	Frict on coeff. of keyways (running)
UKP	υ	0.10	Dimensionless	Friction coeff. between pistons and
***************************************				walls (running)
/B	>		IN/SEC	Velocity of brake lining
VFS	Ü	0.10	IN/SEC	Friction breakout parameter
, w	v(<u>i</u>)		RAD/SEC	Rotational speed between stators and rotors
Was	J	0.358	LB SEC /IN	Brake mass
×	(o) >		IN	Brake piston displacement
X	Ú	0.0	IN	Brake piston displacement when t = o
××	(o) >		IN/SEC	Brake Piston Velocity
×Pc	ပ	0.0	IN/SEC	Brake piston velocity when $t = 0$
×:×	>		IN/SEC	Brake piston accel.
T			- Company of the Comp	

WITH THE CONTRACT OF THE PROPERTY OF THE PROPE

2. HYDRAULIC SYSTEM

The hydraulic system is the brake actuation power source and is made up of the four components as shown in Figure 7: the pilot's metering valve, the antiskid control valve, the control line, and the brake piston housing. The pilot's metering valve is a pressure regulator, usually having a mechanical input, which has a steady state output pressure (Pmv) at a level commanded by the pilot (Pcom). The antiskid valve is a pressure regulator which has a steady state output as dictated by the antiskid control device. For a modulated antiskid system, the control valve is a variable pressure servo type regulator and for an ON-OFF antiskid system the control valve is an ON-OFF valve. The control line is simply the fluid transmission line or containment vessel connecting the control valve to the brake housing. The brake housing is a collection of cylinders and pistons which act to compress the brake discs. From a hydraulic system aspect, the control valve is a variable area orifice, where the orifice area is a function of spool position. The control valve spool position is received as an input from computations described in a section devoted to the operation of the control valve.

In the description of the brake actuation system, there are two principal effects which should be accounted for. The first is the time lag which exists between the control valve output pressure (Pcv) and the actual brake pressure (Pb). This lag is caused by the fluid's resistance to flow due to inertia and friction and by the brake pressure's dependence upon fluid volume within the pressure cavity. The second effect is the instantaneous brake pressure intensity as influenced by fluid inertia and the combined elasticity of the fluid and the pressure cavity. Rapid valve operation can cause pressure overshoot and oscillation due to "water hammer" effects. This overshoot can cause excessive brake torque and may interfere with proper control valve The pilot's metering valve pressure drop and operation. response characteristics are included in the actuating system description so that these effects upon antiskid operation can be examined. To allow for a variety of brake actuation systems which might be encountered, provision is made to accommodate both hydraulic and preumatic actuation The line connecting the control valve and the brake can be treated as a separate fluid cavity or the effects of its volume may be lumped with the brake as would be appropriate for a short line.

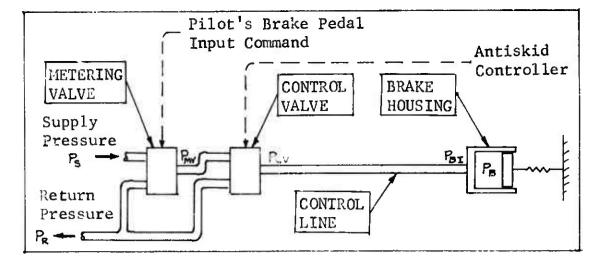


Figure 7 Hydraulic System Components

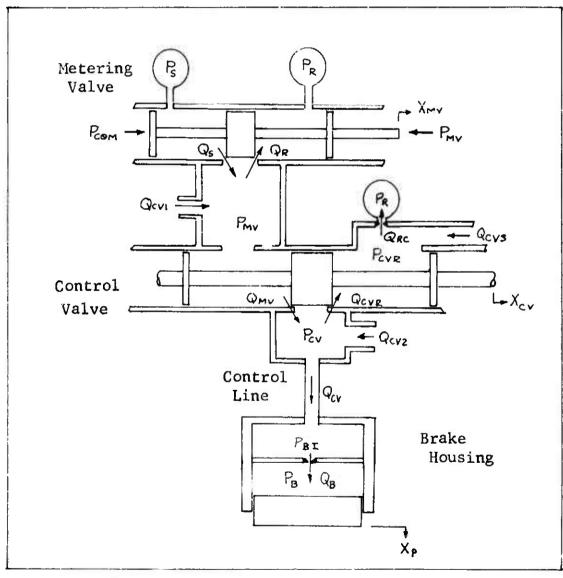


Figure 8 Hydraulic System Schematic

Mathematical Description

Figure 8 is a schematic of the brake hydraulic system. The analytical procedures of References 5 and 6 are utilized to mathematically describe the system.

Let $P_{\hbox{COM}}$ denote the brake pressure which is commanded by the pilot and define $P_{\hbox{COM}}$ such that it increases from a minimum value, PR, (reservoir pressure) to the desired steady state value PCP, as a linear function of time over an interval, TCP, as follows:

(2.1)
$$P_{com} = T(P_{cp} - P_R)/T_{cp} + P_R$$
 IF $0 \le T \le T_{cp}$
 P_{cp} IF $T_{cp} < T$

The metering valve attempts to maintain P_{MV} at the level of PCOM. The metering valve spool displacement XMV is defined by equations (2.2) and (2.3).

(2.3)
$$X_{MV} = \begin{cases} min \{ 0, V_{MV} \} \\ V_{MV} \end{cases}$$
 if $S_{MVL} \leq X_{MV} \leq S_{MVL}$

$$max \{ 0, V_{MV} \} \qquad \text{if } X_{MV} \leq S_{MVL}$$

Let $\phi(X,Y)$ be a function defined as follows:

(a) For hydraulic fluid

(2.4)
$$\phi(x,y) = SIGN(x-y) \sqrt{|x-y|}$$

(b) For compressible pneumatic fluids

(2.5) If X>Y and X \geq Y/Rerit WHERE
$$Rerit = \left[\frac{2}{(8a+1)}\right]^{\frac{d_a}{(7a-1)}}$$

$$\phi(x,y) = \chi \left[1 - (Rerit)^{\frac{3a-1}{2a}}\right]^{\frac{d_a}{2}} \left[(Rerit)^{\frac{3a-1}{2a}}\right]^{\frac{d_a}{2}}$$
If $X \ge Y$ and $X \le Y/Rerit$

$$\phi(x,y) = \chi \left[1 - \left(\frac{1}{x}\right)^{\frac{3a-1}{2a}}\right]^{\frac{1}{2}} \left(\frac{1}{y}\right)^{\frac{3a}{2a}}$$
If $Y \ge X$ and $Y \le X/Rerit$

$$\phi(x,y) = -\phi(y,x)$$
If $Y > X$ and $Y \ge X/Rerit$

$$\phi(x,y) = -\phi(y,x)$$
33

Let $A_{MV}(x)$ be defined by:

Let A_{mvs} and A_{mvR} be defined by:

Then

Let $\bigvee_{M \vee V}$ be the fluid volume from the output of the metering valve up to the input of the control valve. Then

Let $A_{cv}(x)$ be defined by:

Let A_{CVS} and A_{CVR} be defined by

$$(2.13) A_{cvs} = A_{cv} \langle X_{cv} - S_{cL} \rangle$$

Then

The volume of the cavity occupied by the brake actuation media is established by equation (2.19) as follows:

$$(2.19) V_B = V_{BO} + A_{BPS} X_P$$

(2.24a) Qa = Qcv

Three options for the control line mathematical description are provided to cover a variety of circumstances which may be encountered. The third option is representative of a typical aircraft installation and is used in analyzing the F-111 system.

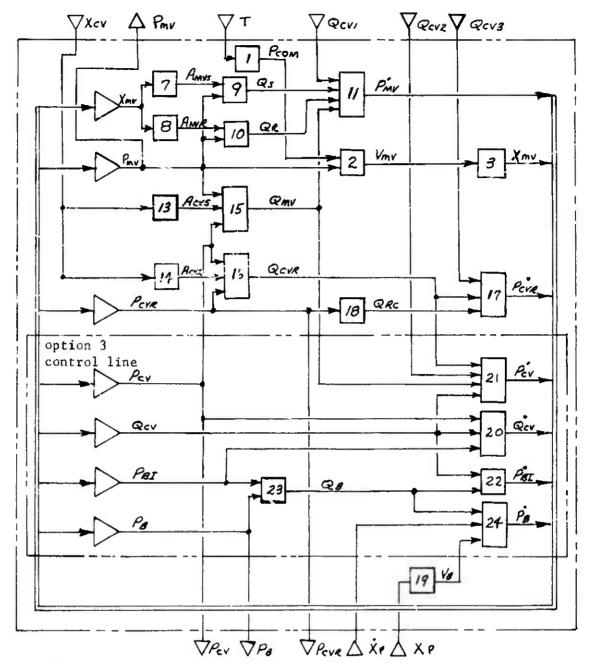
The first option is for a control line with hydraulic fluid considering volume effects only. This option will not predict 'water hammer' but is satisfactory for many cases, particularly for the case of a short control line 50 inches or less in length. The following equations describe the first option:

(2.20a)
$$Q_{CV} = Q_{MV} - Q_{CVR} + Q_{CVZ}$$

(2.21a) $\dot{P}_{CV} = (B_B/V_B)(Q_{CV} - A_{BPS} \dot{X}_P)$
(2.22a) $P_{BI} = P_{CV}$
(2.23a) $P_B = P_{BI}$

The following equations are applicable to the second option for the control line using compressible pneumatic fluid.

(2.20b)
$$Q_{cv} = Q_{mv} - Q_{cvR} + Q_{cve}$$
(2.21b)
$$P_{cv} = (B_B/V_B)(Q_{cv} - P_{cv} A_{BPS} \dot{X}_P/B_B)$$
(2.22b)
$$P_{BI} = P_{cv}$$
(2.23b)
$$P_{B} = P_{BI}$$
(2.24b)
$$Q_{B} = Q_{cv}$$



Note: Substitute partial equation flow diagram below for control line options 1 and 2.

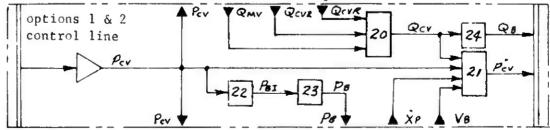


Figure 9 Hydraulic System Equation Flow Diagram

The third option is for a control line with hydraulic fluid where both volume and inertial effects are considered and is described by the following equations:

In this study the brake system hydraulic supply pressure, P_S , is treated as a constant. If P_S varies significantly due to operation of other aircraft hydraulic system equipment, this variable pressure defined as a function of time may be used.

B. Parameter Evaluation

For this study the third optional control line description as applied to the F-111 is of primary interest. For this case MIL-H-5606 hydraulic fluid is used. The hydraulic fluid properties for a mean temperature of 100°F and 1500 psi are:

- (1) Adiabatic bulk modulus: 8 = 248,000 psi
- (2) Density: $R_{HO}=.781 \times 10^{-4} LBF SEC^2/IN^4$
- (3) Kinematic viscosity: $\sqrt{=.0267 \text{ IN}^2/\text{SEC}}$

The system supply pressure is 3000 psi and the return pressure is 100 psi. Initially, all flows are zero and all pressures except the supply pressure are at 100 psi. The pilot's input command pressure P_{COM} is also 100 psi. The pilot's input P_{COM} will go from 100 to 1500 psi in 0.2 seconds. Thus T_{CP} = 0.2 sec and P_{CP} = 1500 psi.

Metering Valve

When the metering valve spool is centered, the flow area is essentially zero for both the return and supply lines. In this spool position $X_{MV} = 0.0$. From equation (2.3) the spool is constrained to stay between S_{MVL} and S_{MVU} .

For the metering valve, $S_{MVL} = -.06$ in and $S_{MVU} = .06$ in. However, when N_{MV} is at +.05, the valve area has reached its maximum for the flow Q_S . When $N_{MV} = -.05$, the area is maximum for the return flow Q_R . Thus $S_{MVU} = .05$. By actual measurement, with the valve full open (area = A_{MVU}) at 100° F, the flow is 9.23 in 3/sec. at 200 psi ΔP . Thus from (2.9) or (2.10).

In the F-111 system, the metering valve is situated next to the control valve so that the volume V_{MV} is quite small. V_{MV} was calculated from the valve drawing as being about 1.0 in³. Also, the valve body is considered to be much stiffer than the hydraulic fluid so that the effective bulk modulus is the fluid modulus. Thus, B_{M} = 248,000 psi. G_{MV} was estimated from analog studies to be about .05.

Control Valve

For the control valve, $X_{CV} = 0.0$ when the spool is centered. At this point the flow area is zero so that $A_{CV} = 0.0$. The flow area remains zero for $-0.05 \le X_{CV} \le 0.05$. Thus the valve has an overlap of .005 in. and $S_{CL} = 0.05$. An additional movement of .030 in. produces full area so $S_{CVO} = 0.030$. By actual measurement at this position at 100° F, the flow is 7.7 in³/sec. at 50 psi Δ P. Thus

The following values are estimates of the return characteristics of the control value: $\sqrt{c_{VR}} = 2.0 \text{ in}^3$, $\beta_{CVR} = 248,000 \text{ psi}$, $\beta_{RC} = 1.0 \text{ in}^4/(\text{sec})(\text{lbf})1/2$.

Control Line

The control line is 1/4 inch outside diameter steel tubing having 0.14 inch wall thickness and internal cross sectional area, β_{BL} , equal to .0386 in². Because of the thin wall, the tube elasticity greatly reduces the bulk modulus. The equivalent bulk modulus, β_{e} , may be calculated from

(2.27) Be = B
$$\left(\frac{1}{\left(\frac{B}{E}\right)\left(\frac{D}{E}\right)+1}\right)$$

Where B = Fluid bulk modulus

E = Young's modulus of tube material

D - Mean tube diameter

t = Tube wall thickness

Thus
$$(2.28) B_{BL} = \frac{248000}{(.248 \times 10^6)(.236)} = 217,700 PSI$$

$$(30 \times 10^6)(.014)$$

The control/line length, $S_{\rm BL}$, is 191 inches with various types of flow restrictors according to the following table.

Description	"K" Value*	Number n	nk
An815-4J Union	.54	1	. 54
AN832-4J Union	.54	1	. 54
AN821-4J Elbow (90°)	1.23	4	4.92
AN837-4J Elbow (45°)	.89	1	.89
90° Tube Bend	.01	12	.12
90° Hose Fitting	1.25	1	1.25
Total			8.26

Table 3 Control Line Restrictions

The "K" values in Table 3 were derived from information contained in Reference

Equation (2.20c) is the result of summing forces on the mass of fluid in the control line. The friction losses are depicted by a turbulent flow loss $D_{\text{TBL}} \mathcal{Q}_{\text{cv}}^2$ and a laminar flow loss $D_{\text{RBL}} \mathcal{Q}_{\text{cv}}$ It is assumed that all the turbulent flow losses come from elbows, etc., which are listed in Table 3. The loss due to the line itself is considered to be always laminar. This assumption of laminar flow for

^{* =} $KV^2/2g$ Where V is the velocity in the line.

the line is justified for two reasons: (1) the loss in the line is small compared to other losses in the system; (2) the flow is normally laminar anyway (Reynolds Number is less than 6000 for the F-111 system).

For the turbulent losses

(2.29)
$$\Delta P = \rho g \Delta h$$

$$= \kappa \rho \sqrt{2}/2$$

$$= (\kappa \rho / 2A^2) Q^2$$

Thus

(2.30) DTBL =
$$\frac{K p}{2 (ABL)^2}$$

= $\frac{(8.26)(.781 \times 10^{-4})}{2 (.0386)^2}$
= .216 1bt sec²/IN⁸

For laminar losses, at temperatures normally encountered, the "escillatory" friction is higher than the steady state friction. See Reference 9. The pressure loss can be written as

$$(2.31) \Delta P = R L (L/A^2) Q$$

For the steady state case as shown in Reference 6,

In Figure 10 values for this theoretical steady state R_L are compared over a range of temperatures to values from Reference 9 which were experimentally established for oscillatory flow. Since the hydraulic flow in the brake control line associated with antiskid operation is transitory, the laminar flow resistance base on experimental measurements for oscillatory flow is used.

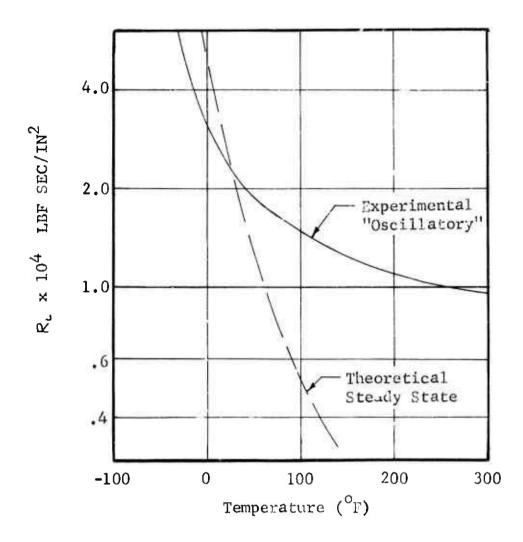


Figure 10 Hydraulic Fluid Damping Characteristic

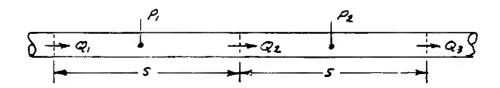
From Figure 10 at 100° F R for the experimental oscillatory case is 1.5 X 10° 4. LBF SEC/IN²

Therefore:

(2.33)
$$D_{RBL} = \frac{(R_L)(S_{BL})}{(A_{BL})^2} = \frac{(1.5 \times 10^{-4})(191)}{(.0386)^2}$$
$$= 19.22 \text{ /bf sec / in}^5$$

When a "lumped parameter" type anal sis as described by equations (2.20c), (2.21c) and (2.22c) is used for the control line the resulting natural frequency is somewhat lower than the actual line, if the actual line volume, V_{BL} , is used. The value of V_{BL} is adjusted as follows to achieve the correct natural frequency for the "lumped parameter" description.

Consider hydraulic fluid flowing through a line with cross sectional area, A, and divided into segments having equal length, S, as shown below.



If each segment is treated as a separate pressure vessel having volume, V, with a flow in and a flow out, and if equations of the form of (2.20c) (2.21c) and (2.22c) are written for these pressure vessels, neglecting friction, the following expressions are obtained:

(2.34)
$$\dot{Q}_2 = (A/\rho S)(P_1 - P_2)$$

$$(2.35) \qquad \dot{P}_i = (B/V)(Q_1 - Q_2)$$

(2.36)
$$\dot{P}_2 = (B/V)(Q_2 - Q_3)$$

By substituting equations (2.35) and (2.36) into equation (2.34) differentiated once with respect to time the following differential equation is formed:

(2.37)
$$\ddot{Q}_{z} = (A/\rho s)(B/v)[(Q_{1}-Q_{2})-(Q_{2}-Q_{3})]$$

or

(2.38)
$$\ddot{Q}_2 + 2(AB/\rho SV)Q_2 = (AB/\rho SV)(Q_1 + Q_3)$$

Equation (2.38) establishes that the natural frequency of each line segment is:

(2.39)
$$F_n = \frac{1}{2\pi} \sqrt{\frac{2AB}{\rho SV}} c_{PS}$$

However, vibration theory considering distributed mass and elasticity establishes the speed of sound, C, in the line as:

For fundamental mode oscillation in a closed end tube having length, S, the natural period, T_c , is:

(2.41)
$$T_c = 25/c$$
 SEC

Therefore, the natural frequency, g_n , of an actual tube segment is:

By equating the two expressions for natural frequency, equations (2.39) and (2.42), the volume of the line segment which will have the same natural frequency as the actual is established as:

$$(2.43) \qquad \forall = 2AS/\pi^2$$

Thus,

(2.44)
$$V_{BL} = \frac{2}{\pi^2} A_{BL} S_{BL} = \frac{(2)(.0386)(191)}{\pi^2} = 1.495 N^3$$

Brake Housing

The brake housing has ten pistons of 1.33 in² area each. Since the number of pistons serviced by one control line is five, then $A_3\rho s = 5(1.33) = 6.65$ in². The fluid volume in the brake housing with the pistons bottomed $(X\rho = O)$ is 8.00 in³. Thus VBO = 4.00 in³ or one-half the total volume. The orifice coefficient A_{BO} was estimated to be about 2.0 in⁴/sec /bf /2.

Operational Systems

The option 1 system neglects the line inertial effects. The parameters have the same value as the corresponding parameters for the option 3 system, escept that $\vee a_0$ should include any line volume. Thus, for the F-lll system, with the option 1 system, $\vee a_0 = 4.00 + .0386(191) = 11.36 \times 3$

The option 2 description is used for systems with compressible pneumatic fluid. The appropriate parameters will be evaluated for nitrogen at 100°F as the fluid media and isothermal processes are assumed except for orifice flow calculations. While the heat transfer characteristics of the brake system components have not been rigorously evaluated, the usual component installation is such that assuming isothermal processes is valid. The mathematical description of the brake actuation control system using compressible pneumatic fluid is written using equations of the same general form as for those describing the hydraulic system, thereby minimizing the

the number of equations and enhancing computation flexibility. Utilizing the hydraulic equations when pneumatic fluid is used requires that the appropriate parameters be expressed in suitable mathematically equivalent terms. Consider the characteristic equation of state for a perfect gas:

$$(2.45) \qquad P = \underbrace{MRT}_{V}$$

And the definition:

(2.46)
$$\frac{dP}{dt} = \frac{\partial P}{\partial m} \frac{dm}{dt} + \frac{\partial P}{\partial V} \frac{dV}{dt} + \frac{\partial P}{\partial T} \frac{dT}{dt}$$

For the assumed isothermal process, substitution of equation (2.45) into equation (2.46) gives:

(2.47)
$$\dot{\rho} = \left(\frac{RT}{V}\right)\dot{m} - \left(\frac{RT}{V}\right)\frac{m}{V}\dot{V}$$

For those cases, such as for the metering valve and control valve pressure cavities, where the volume is not changing, $\dot{\vee}$ is zero and equation (2.47) reduces to:

(2.48)
$$\dot{P} = \left(\frac{RT}{V}\right) \dot{m}$$

For hydraulic fluid, \dot{P} is described by equations having the form of equation (2.49) below. (See equation (2.11) for instance.)

$$(2.49) \quad \dot{p} = \left(\frac{3}{V}\right)Q$$

Noting the similarity between equation (2.48) and equation (2.49) it is obvious that if RT is used in place of B and if \dot{m} is used in place of Q, the "Hydraulic" equations can be used for computing performance of a system using oneumatic fluid. Thus, $B_{\theta} = B_{\text{CVR}} = B_{\text{mV}} = RT$. For nitrogen R = $662.4 \, \text{IN lbF/lbm°F}$ and at 100° F RT = $(662.4) \, (460 + 100) = 371 \, \text{x} \, 10^{6} \, \text{IN lbF/lbm}$.

Since P/RT = M/V, equation (2.47) can be written as

(2.50)
$$\dot{P} = \left(\frac{RT}{V}\right)\left[\dot{m} - \left(\frac{P}{RT}\right)\dot{V}\right]$$

Equation (2.21b) is obtained by substituting β_{θ} for RT, $A_{BPS} \dot{X}_{P}$ for \dot{V} , and Q for \dot{m} in equation (2.50), thereby accounting for the change in brake volume caused by piston movement.

Equation (2.51) below, from Reference 6, describes the mass flow rate of a gas from a container having high pressure, ρ_H , through an orifice of area, ρ_O , to a container having

low pressure, PL .

(2.51)
$$\dot{m} = \left(\frac{C_0 A_0}{R} \sqrt{\frac{2GC_P}{T}}\right) P_H \left(\frac{P_H}{P_L}\right)^{1/2} \sqrt{1 - \left(\frac{P_H}{P_L}\right)^{\frac{N-1}{2}}}$$

Equation (2.52) below, from Reference 6, describes the volumetric flow rate of hydraulic fluid through an orifice under similar circumstances.

Both equations (2.51) and (2.52) can be written in the form $Q = A_F \phi \langle P_H, P_L \rangle$ where $\phi \langle P_H, P_L \rangle$ is a flow function as defined by equations (2.4) and (2.5) for the appropriate circumstances and where A_F is a flow coefficient accounting for orifice and fluid properties. For the case of hydraulic fluids a value of $Co \sqrt{2/\rho} = 103.5 \text{ m}^2/16F^{1/2}$ sec has been established by experience as being representative of an average orifice (i.e., $Co \approx 0.65$). The metering valve flow coefficient, A_{MVO} , previously computed is $0.653 \text{ Im}^4/\text{Sec}/\text{bf}^{1/2}$; therefore, the apparent actual orifice area, A_O , for the metering valve is $A_O = 0.653/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5 = 0.63/103.5$

For the case of the pneumatic system with nitrogen at 100° F as the working fluid and using $C_{\rho} = 2300$ in $1bf/1bm^{\circ}$ F, and R = 662.4 in $1bf/1bm^{\circ}$ F:

(2.53)
$$A_{mvo} = \frac{CoA_o}{R} \sqrt{\frac{2GC_P}{T}}$$

= $\frac{(.8)(.631\times10^{-2})}{662.4} \sqrt{\frac{(.2)(386)(2300)}{560}}$
= 0.43×10^{-3} | lbm in 2 /lbf sec

Using the same procedure establishes that:

$$Acvo = 0.716 \times 10^{-3} \text{ lbm in}^2/\text{lbf sec}$$

 $Arc = 0.658 \times 10^{-3} \text{ lbm in}^2/\text{lbf sec}$

Table 4 Hydraulic System Parameters

OP* 1 2 3 DESCRIPTION	X Cross sectional area of brake		×	×	X X X Control valve flow area function	X X Control valve leakage flow coeff.	×	X X Control valve full open flow coeff.	×	X X Control valve return flow coeff.	×	X X Control valve supply coeff.	×	X X X Metering valve flow area function.	X X Metering valve leakage coeff.	×	X X Metering valve full open flow coeff.		X X Metering valve return flow coeff.	×	X X Metering valve supply flow coeff.		X X Control valve return line restriction.	X	X X Bulk modulus within the brake housing.	X Temp X gas constant.
UNITS	6 IN ²	4	IN' SEC LBF	IN ₂	_	IN"/SEC LBF2		IN4/SEG LBF2	.715X10 ⁻³ LBW IN ² /LBF ₁ SEC	IN4/SEG LBF2	LBM IN /LBF, SEC	/SEC LBF2	LBM INZ/LBF SEC		IN4/SEC LBF2	LB	IN4/SEG LBF2	.429X10 LBM IN / SEC, LBF	IN"/SEÇ LBF2	LBM IN2/SEC, LBF		LBM IN / SEC, LBF	IN4/SEG LBF2	LBM	LBF/IN	371X10 ⁶ IN LBF/LBM
TYPE VALUE	c .0386	(c 2.00	c 6.65	- F	c 0.00	00.00	c 1.09	.715	>		Δ		- F	c 0.00	0.00	c .653	.429	>		>		c 1.00	.658	c . 248)	c .371)
SYMBOL	A		ABG	Ages	Acv (x)) A	,	Acvo		Acve	;	Acvs	;	Amv (x)	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \) }	Amvo		AMVR		AMVS		ARC		BB	

*See page 37

ί	6
+	J
5	3
•	٠
	†
,	1
F	9
-	1

	ontrol line.		g valve outlet.			ŕf.			$\lambda_{\alpha} = (c_{p}/c_{v})$.0.		e press.		me : 0		e inlet press.		ess.	ess.	time = 0.	_
DESCRIPTION	Fluid bulk modulus in control line.	Temp. X gas constant	Bulk modulus at metering valve outlet.	Temp X gas constant	Laminar line loss coeff	Turbulent line loss coeff.	Metering valve gain		Ratio of specific heats /a = (cp/c_v)	Brake Pressure	Brake pressure at time = 0.		Time derivative of brake press.	Press. at brake inlet.	Brake inlet press at time =		Time derivative of brake inlet press.	Pilot's command press.	Steady state command press.	Control valve output press.	Control valve press at time	
0px 1 2 3	× ×	*	X X Bt	X	X	-	X	×	X	X X X Br	X Bı	×	×		X	××	×	×		×	×	-
UNITS	LBF/IN ² 1 RF/IN ²	,BM		IN LBF/LBM	LBF SEC/IN ²	LBF SECZ/INO		IN3/SEC LBF	Dimensionless		LBF/IN2		LBF/INZ SEC		LBF/IN2		LBF/IN SEC	•				/
VALUE	.218 X 10 ⁶	X 10	X 10	x 10	19.22	.216	.05	.05	1.40		100				100				1500		100	
TYPE	v	, _U	ပ	ပ	ပ	ပ	ပ	ပ	ပ	(o) A	ပ	>	>	^	ပ	>	>	>	ပ	(o) A	ပ	
SYMBOL	98	× \	BMV		DRBL	Drei	GMV		کمر	حي ا	96 86		۵.	Par	PBIO		Per	ص آ	Pcp	مي	Pcvo	

Table 4 (Contd)

				OP		
SYMBOL	TYPE	VALUE	UNITS	1 2	3	DESCRIPTION
O,	(0) A		LBF/TN ²	×	×	Return press in cont. valve.
x (100	1.RF/TN ²	_	_	Refurn control valve press at time = 0
))	υ	14.7	LBF/IN ²	<u>×</u>		
Pove	>		LBF/IN ² SEC	×	×	Return control valve press. time derivative
Ø(x,y)	44		· ·	×	×	Flow function
رم ک	(0) ^		LBF/IN2	×	×	Metering valve output press.
PMVO	υ	100	LBF/IN	×	×	Metering valve press at time = 0.
	ပ	14.7	LBF/IN2	×		
Σ.	>		LBF/IN, SEC	×	:<	Time derivative of metering valve press.
۵,	υ	100	LBF/IN,	×	×	Return pressure
•	ပ	14.7	LBF/IN	×		
σ.	ပ	3000	LBF/IN ²	×	×	System supply pressure.
ð	>		IN3/SEC	٠4	×	Flow into brake (per line)
			LBM/SEC	×		
OC.	>		IN3/SEC	×	×	Flow out of control valve
	>		LBM/SEC	×		
Qc vo	၁	0.0	IN3/SEC		×	Control valve flow at time $= 0$
	>		IN ³ /SEC	×		
•	>		LBM/SEC	×		
Ş	>		IN3/SEC		×	Time derivative of control valve flow.
Q _C V ₁	v(i)		IN ³ /SEC	×	×	
			LBM/SEC	×		
ď	v(i)		IN3/SEC	×	×	Feedback flows from
	,		LBM/SEC	×	_	control valve.
Qcv3	v(i)		IN3/SEC	×	×	
			LBM/SEC	×	-	

Table 4 (Contd)

		Return flow in control valve		Metering valve flow		Return flow from metering valve		Return flow from control valve		Flow into system		Critical pressure ratio	Fluid density	Control line length	Control valve overlap	Spool distance from full closed to	full open (C.V)	Min. Neg. spool travel (met. valve)	Spool travel from full closed to	full open (met. valve)	Max. Pos. Spool travel (met. valve)	Time	Time for Pcom = Pcp	(per line)	Brake fluid volume when $Xp = 0$	Corrected line volume	
	m	×		×		×		×		×			×	×	×	×		×	×		×	×	×	×	×	×	
5	7 (4		×		×		×		×		> :	×			×	×		×	×		×	×	×	×	×		
-		×		×		×		×		×			×		×	\times		×	×		×	\sim	×	\sim	~	_	
	UNITS	IN ³ /SEC	LBM/SEC	IN3/SEC	LBM/SEC	IN3/SEC	LBM/SEC	IN3/SEC	LBM/SEC	IN ³ /SEC	LBM/SEC	Dimensionless	LBF SEC ² /IN ⁴	NI	NI	ZI		NI	IN		NI	SEC	SEC	IN3	IN	IN ³	
	VALUE											++	.781X10-4	.91.0	.005	.030		060	.050		090.		.200		4.00	1,495	
	TYPE	>		>		>		>		>		ပ	ပ	ပ	ပ	U		ပ	ပ		υ	v(i)	໌ ບ	>	ပ	ပ	
	SYMBOL	QCVR		ر م		Q		QRC		Š		REPET	DX	Set	Scr	0,0%		Smri	Smyo		Smru	-	Tcp	>	/ Bo	\ \ \ \	

F Calculate from δ_{α} , see Equation (2.5)

Table 4 (Contd)

SYMBOT	тург	VALIE	STINII	0P ↑	0₽ × 2 3	DESCRIPTION
>	į		1.03	>	>	Control value return volume
VCVR	ن		TIN	<u>ধ</u>	<	Colletor varve recutit votame.
>	>		IN/SEC	×××	×	Metering valve control variable.
\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	v	1.00	IN3	×	×	Volume between metering & control valve.
X	v(i)			×	×	Control valve spool position.
×	` >		NI	×	×	Metering valve spool position.
×	Ü	0.0	IN	×××	×	Metering valve spool position at time = O
•×	>		IN/SEC	×××	×	Metering valve spool velocity.
×	v(i)		NI	×××	×	Brake piston displacement
·×	v(1)		IN/SEC	XXX	×	Brake piston velocity
				_		

*An x denotes application in option 1, 2, or 3 as explained on page 35-37.

Brake actuation system using hydraulic fluid where the control line description considers volume effects only. Option 1

Brake actuation system using compressible pneumatic find. Option 2

Brake actuation system using hydraulic fluid where the control line description considers both volume and inertia effects. Option 3

3a AIRPLANE SYSTEM (FLYWHEEL)

Figure 11 shows the model for the airplane system as it might be simulated with a dynamometer flywheel set-up. The mass W_A is supported by the tire and is determined by the percentage of the airplane weight carried on one main gear. The mass W_{AR} represents some part of the airplane structure which could vibrate in sympathy with certain ground discontinuities such as wing mounted fuel tanks or armament. The forces F_{LO} and F_{AL} act on W_A because of gravity and aerodynamic lift, respectively.

A. Mathematical Description

The shock strut stroke is denoted by Z_{SM} . This stroke is determed by Z and Z_{WM} .

(3a.1)
$$Z_{SM} = Z_{WM} - Z$$

The shock strut force F_{VM} is given by equation (3a.3)

Let Z_{GO} and Z_{GOP} denote the height and slope of the ground (or flywheel surface). Let S_m denote the tire deflection. Then S_m and S_m are determined by

The force FNM acting vertically upward on the tire is then given by

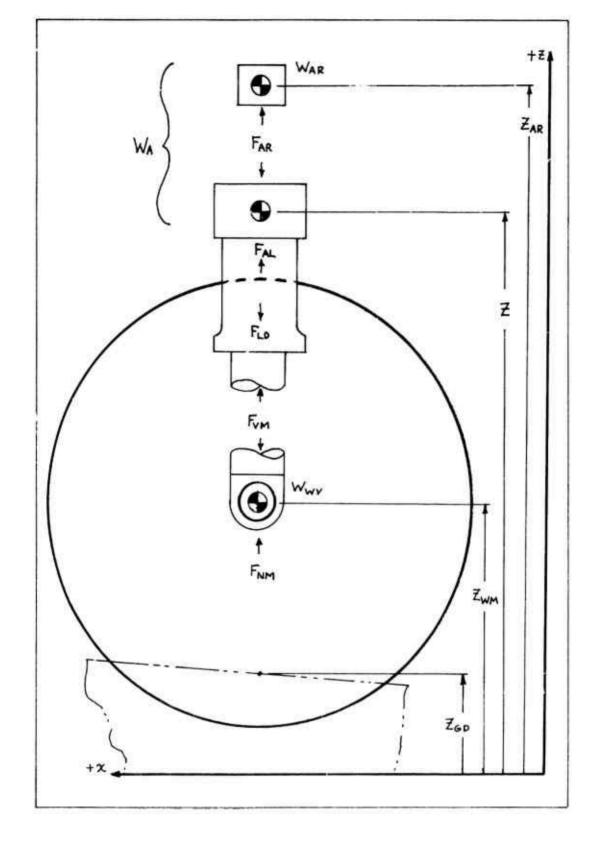


Figure 11 Flywheel System Model

Summing forces in the vertical direction on the unsprung mass W_{wv} , there follows:

Where F_{eRV} is the tire unbalance force. For the mass W_{AR} , summing forces vertically gives:

(3a.8)
$$W_{AR} \ddot{Z}_{AR} = F_{AR}$$

(3a.9) $F_{AR} = C_{AR} (Z - Z_{AR}) + D_{AR} (\dot{Z} - \dot{Z}_{AR})$

The aerodynamic lift and drag forces F_{AL} and F_{AD} are defined as follows:

$$(3a.10) F_{AL} = C_{AL} V_F^2$$

(3a.11)
$$F_{AD} = C_{AD} V_F^2$$

The equation which determines Z is given as

The equation for the flywheel velocity is given by

Where F_{TH} is a force equivalent to engine thrust and W_{AT} is the airplane mass. The aircraft's longitudinal displacement is established by

(3a.14)
$$X_F = \int V_F dt + X_{FO}$$

The equation flow diagram for the airplane system (flywheel) is shown on Figure 12.

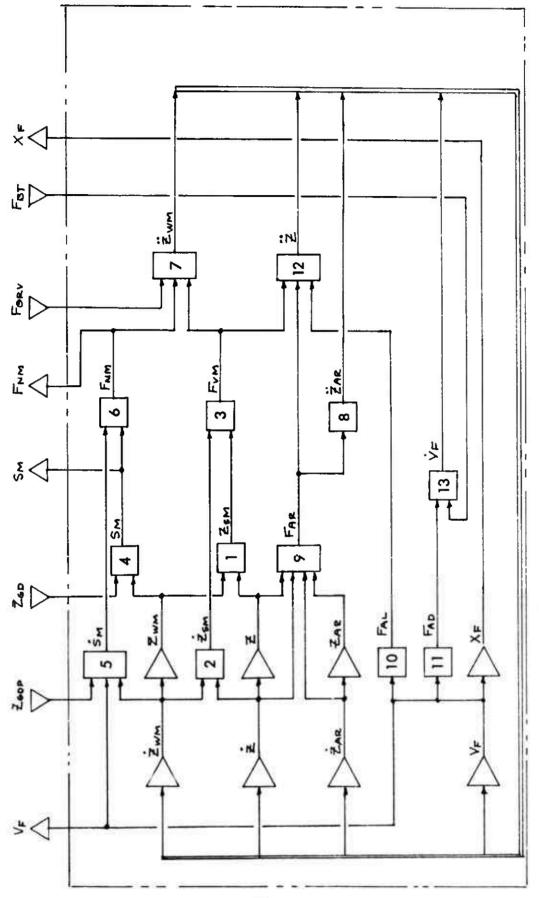
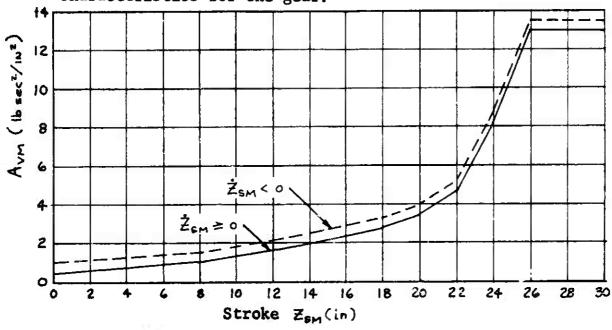


Figure 12 Airplane System (Flywheel) Equation Flow Diagram

B. Parameter Evaluation

Shock Strut Characteristics

Figures 13 and 14 show the main gear load and damping characteristics for one gear.



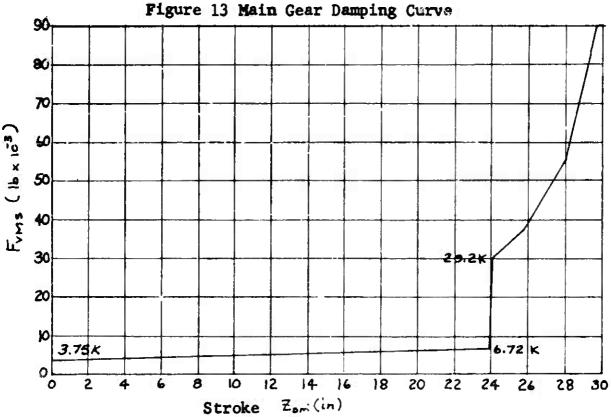


Figure 14 Main Gear Air Load Curve

Vertical Tire Characteristics

In equation (3a.6) it has been assumed that the tire loading characteristic is given by an equation of the form

(3a.15)
$$F = S(C+O\dot{S})$$

Let the following terms be defined for a tire:

FR = Rated load

 P_R = Rated pressure

 S_R = Rated deflection

If P is the actual pressure, then obviously the tire spring rate, C , is

(3a.16)
$$C = \frac{P}{P_R} \frac{F_R}{S_R}$$

From reference 1 (Equation 132) the damping force, F_p , is established as:

(3a.17)
$$F_0 = \left(\frac{\eta c}{\omega}\right) \dot{s}$$

It is assumed that the damping force is related to the undamped natural frequency at rated conditions. The undamped natural frequency, ω , is established as:

(3a.18)
$$\omega = \sqrt{\frac{K}{m}} = \sqrt{\frac{FRG}{S_R F_R}} = \sqrt{\frac{G}{S_R}}$$

Where G = 386 IN/SEC². Also from Equations 137 and 138 of Reference 1:

(3a.19)
$$\eta = 2 \eta_R / [1 + (P/P_R)]$$

Where $\eta_R = 0.1$.

The main landing gear shock strut linear damping coefficient, O_{VM} , is set equal to zero for the example problem.

The unsprung mass, W_{wv} , experiencing vertical motion is 6.44 lbm. Thus, $W_{wv} = (644)/386 = 1.667$ lbf sec^2/in .

As previously assumed in Equation (3a.15), $F_0 = 505$ Equating the two expressions for F_0 at rated deflection

$$(3a.20) \quad \frac{\eta C}{\omega} = SRD$$

0r

(3a.21)
$$D = \frac{\eta C}{w S_R} = \frac{\eta F_R}{(S_R)^2} \left(\frac{\rho}{\rho_R}\right) \sqrt{\frac{S_R}{G}}$$

For the 47 x 18 - 18 26 ply rating F-111 main tire, $P = P_R = 150$ psi

$$F_R = 38,100 \text{ lb.}$$
 and $S_R = 4.00 \text{ IN.}$

Thus

(3a.22)
$$C_{MT} = \left(\frac{P}{F_R}\right)\left(\frac{F_R}{S_R}\right) = \frac{(150)(38100)}{(150)(4.00)} = 9530 \, lbf/lN$$

(3a.23)
$$D_{MT} = \left(\frac{P}{P_R}\right) \left(\frac{\eta F_R}{S_R^2}\right) \sqrt{\frac{S_R}{G}}$$

$$= \frac{(150)}{(150)} \frac{(.1)(38100)}{(4.00)^2} \sqrt{\frac{4.0}{386}} = 24.24 \text{ lbf sec/IN}^2$$

Aircraft Characteristics

For the example problem, an airplane weight of 57,000 lb. is used. The static vertical load on one main gear is 25,200 lbs. so that

(3a.24)
$$W_A = 25,200/G = 65.0 \text{ lbf sec}^2/IN.$$

For a velocity of $V_F = 2400$ IN/SEC and a representative tire-to-runway braking coefficient of .45 at the main wheel, the tire load is 21,400 lbs. Thus $F_{LD} = 21,400$ lb.

The total aircraft mass is $W_{AT} = 57000/G = 147.8 \text{ lbf sec}^2/\text{IN}$.

The mass W_{AR} is used to simulate some airplane resonant effect. For illustrative purposes, it is assumed that $W_{AR} = 1000$ LBM = 2.59 LBF SEC 2 /IN and has a natural frequency of 12 cps. Therefore, since $\omega = 2\pi(12) = 75.4$ rad/sec and $k = m\omega^2$,

(3a.25)
$$C_{AR} = \omega^2 W_{AR} = (75.4)^2 (2.59) = 14,720 lb/in$$

Using 3 percent critical damping gives

(3a.26)
$$D_{AR} = (.03) 2 \sqrt{C_{AR} W_{AR}} =$$

= (.03) $2 \sqrt{(14,720)(2.59)} = 11.72 |bsec/in$

The initial conditions are calculated for equilibrium. At time = 0, let $X_f = 0$ so that $Z_{GD} \langle X_F \rangle = 0$ since $Z_{GD} \langle 0 \rangle$ is always 0. Let $V_{FO} = 1200$ IN/SEC and assume that $C_{AL} = C_{AD} = 0$

From equation (3a.6),

$$(3a.27)$$
 S_m = F_{NM} / C_{Mr} = 21,400/9530 = 2.245 in

From equation (3a.4),

$$(3a.28)$$
 $\Xi_{wmo} = -2.245$ in.

From figure 14, when Fyms = 21,400 lb.,

 $Z_{SM} = 23.98$ in and from equation (3a.1),

$$(3a.29)$$
 $Z_o = Z_{wmo} - Z_{SM} = -2.245 - 23.980 = -26.225 IN.$

For the example problem the effects of aerodynamic forces are not included in the flywheel simulation; therefore, $C_{A0} = 0.0$ and $C_{AL} = 0.0$.

The unsprung mass moving vertically, W_{wv} , is the same as W_{Gw} described in the Section 4a Wheel and Tire System (Flywheel) for horizontal motion. Therefore, $W_{wv} = 1.60$ lbf \sec^2/in .

The average engine idle thrust is 1000 lbf. Therefore, $F_{TH} = 1000$ lbf.

Table 5 Airplane System (Flywheel) Parameters

SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
Ave	*>		1b sec²/in²	Shock strut damping characteristic.
CAD	O	0.0	16 sec2/in2	Aerodynamic drag coefficient.
O. A.	O	0.0	1b sec2/in2	Aerodynamic lift coefficient.
CAR	U	14,720	1b/in	Spring rate associated with mass War
CMT	U	9530	lb/in	Tire vertical spring rate
DAR	U	11.72	1b sec/in	Damping coeff. associated with mass W.
DMT	v	38.8	16 sec/in²	WAR Tire damping coefficient
٥	O	0.0	16 sec/in	Shock strut linear damping coeff.
AD	>		<u>a</u>	Aerodynamic drag force on airplane.
FAL	>		٩	Aerodynamic lift force on airplane
FAR	>		4	Force associated with mass WAR
T	v(1)		41	Braking force
F	v	21,400	9	Static force on tire
F ØRV	v(1)		91	Tire unbalance force (vertical)
2	(0)^		4	T're normal force
T T	υ	0001	<u>a</u>	Engine thrust
٤	>		9	Shock strut force .
TVMS	***		<u>م</u>	Shock strut force with $\mathbb{Z}_{sM} = 0$
S	(0)^		ż.	Tire deflection
·Ω·	>		in/sec	Rate of tire deflection
N N	>		in/sec	Flywheel velocity
VFO	υ	2400	in/sec	Flywheel velocity at time = 0

*Point plot input see Figure 13 **Point plot input see Figure 14

Table 5 (Contd)

SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
WA	υ	65.0	lb sec 2/in	Airplane mass carried on main gear.
WAR	Ü	2.59	16 sec2/in	Mass of airplane substructure.
WAT	0	147.8	16 sec2/in	Total airplane mass
Mw/	U	1.667	16 sec2/in	Unsprung mass
×	(0)^		ċ.	Flywheel surface distance traveled.
XFO	Ü	0.0	· i	Flywheel distance at time = 0.
4	>	and become the	. 5	Vertical location of equivalent apl. mass
				C.G.
7°	υ	-26.225	.£.	Vertical location of equivalent mass at
•				time = 0
M.	>		in/sec	Velocity of apl. mass
7.	υ	0.0	in/sec	Velocity of apl mass at time = 0
17.1	>		in/sec ²	Acceleration of apl mass
ZAR	>	dika for decomp	2.	Auxiliary mass location
7, ,,0	o	-26.225	. 2	Auxiliary mass location at time = 0
ZAR	>	Bild warr 1	in/sec	Auxiliary mass velocity
ZARO	o	0.0	in/sec	Auxiliary mass velocity at time = 0
ZAR	>	N depart	ir:/sec2	Auxiliary mass acceleration
Zed	v(i)		, u,	Ground height
Zipp	v(i)		in/in	Ground slope
Zsm	>		2.	Shock Strut Stroke
H.	>		in/sec	Shock strut stroke velocity
				The state of the s

Table 5 (Contd)

見のからはながる。 Participation のでは、 P

DESCRIPTION	Axle location (vertical) Axle location at time = 0 Axle velocity (vertical) Axle location at time = 0 Axle acceleration
UNITS	in sec in sec in sec in sec
VALUE	-2.245
TYPE	> 0 > 0 >
SYMBOL	7 7 7 7 7 7 X X X X X X X X X X X X X X

3b. AIRPLANE SYSTEM (3 DEGREE)

The three degree airplane system is built around a rigid body airplane which is allowed to move vertically, horizontally (parallel to the runway centerline), and rotationally in the pitch mode. This model provides for the interaction of the anti-skid system with those effects which are related to airplane pitch. This includes such pitch effects as change in the aerodynamic lift, drag, and moment due to change in wing angle of attack, change in the aerodynamic lift, drag, and moment due to changes in elevator deflection as dictated by the stability augmentation system (pitch mode), change in tire loading due to braking pitch moment, and the effect of ground slope and roughness as reacted through both the main and nose gears.

A. Mathematical Description

表がない。文化の大学の一般のでは、大学の一般のでは、大学の一般のできない。これは、「一般のできない」という。「一般のできない」という。「一般のできない」という。「一般のできない」という。「一般のできない」という。

Figure 15 shows the three coordinates which describe the airplane position relative to reference points on the earth's surface.

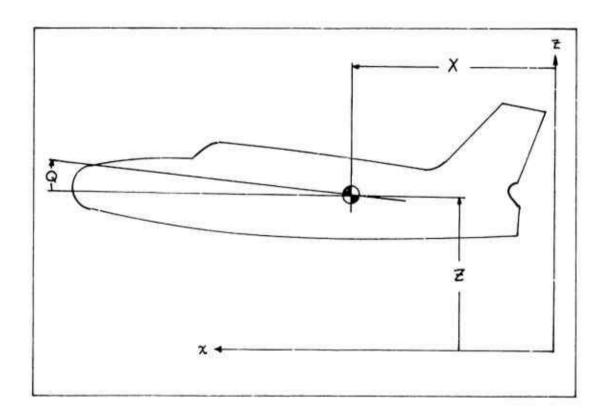


Figure 15 Airplane Coordinates

Figure 16 shows the gear extended dimensions as measured in the airplane's water line-fuselage station reference system.

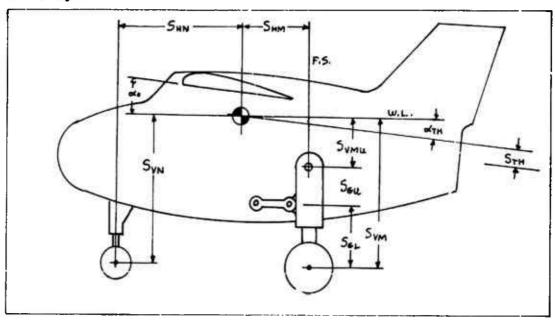


Figure 16 Airplane Geometry

Let $Z_{GD}(x)$ denote the runway profile height and let $Z_{GDP}(x)$ denote the runway profile slope.

Nose Gear

Let Z_{SN} and \dot{Z}_{SN} denote the nose strut stroke and stroke velocity. From Figure 17, Z_{SN} and \dot{Z}_{SN} are given by

The mose gear shock strut force is then given by

 F_{NN} , the normal ground force at the nose gear is given by

where S_N is the nose tire deflection. S_N and \mathring{S}_N are given by:

Summing vertical forces on the nose wheel,

Main Gear

Let \vec{Z}_{SM} and $\dot{\vec{Z}}_{SM}$ denote the main gear stroke and stroke velocity:

The main gear shock strut force is given by:

Let S_M denote the main gear tire deflection. Then the tire normal force is given by:

Summing vertical forces on the main wheel,

Figure 18 shows the model of the main gear. With the assumption that the gear weight is much less than the airplane weight (that is, $W_u << W_A$), it follows that:

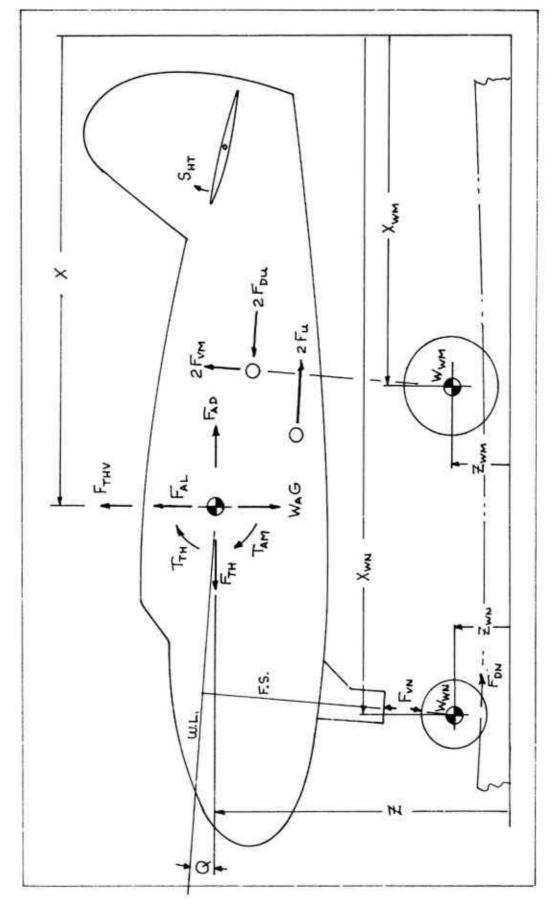


Figure 17 Airplane Dynamics

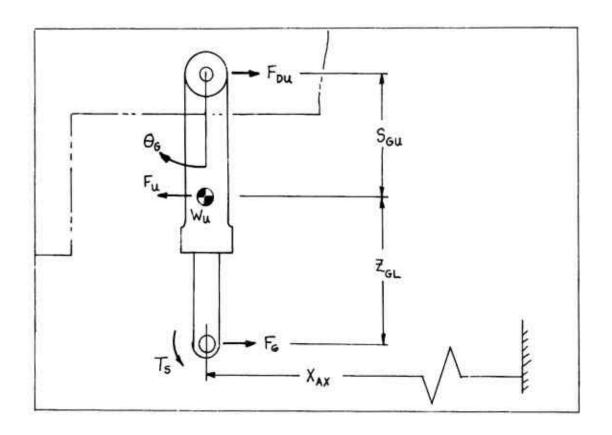


Figure 18 Main Strut Model

where Z_{GL} is determined by:

Fou can then be computed from

where

 T_s and F_G are outputs from the tire and wheel system. The horizontal axle reference location is denoted by X_{AX} . X_{AX} is given by:

Thrust

Referring to Figures 16 and 17 , if \overline{r}_{TH} is the thrust, then

Aerodynamics

The dynamic Air Force Q is given by:

The aerodynamic lift, drag, and moment are then given by:

If α_{w} denotes the wing angle of attack relative to the air, then:

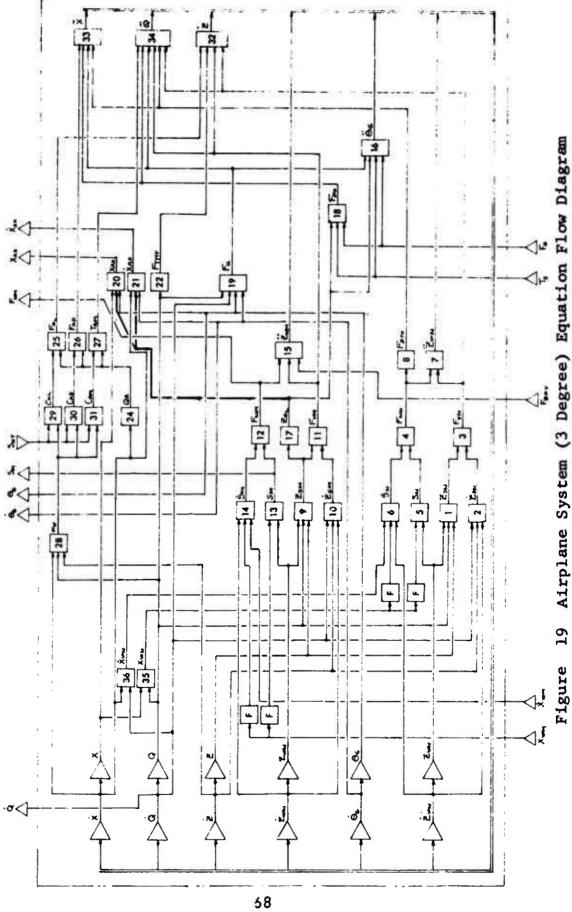
$$(3b.28) \propto_W = \propto_o + (180/\pi)(Q - \dot{Z}/\dot{X})$$

Let S_{HT} denote the horizontal tail deflection. Then the aerodynamic coefficients are given by:

Dynamics

Referring to Figure 17,

(3b.33)
$$W_A X = F_{TH} - F_{AD} + 2F_{DU} - 2F_U - F_{DN}$$



where

(3b.35)
$$\dot{X}_{WN} = \dot{X} + \dot{S}_{HN} + \dot{S}_{VN} \dot{Q}$$

(3b.36) $\dot{\dot{X}}_{WN} = \dot{\dot{X}} + \dot{S}_{VN} \dot{\dot{Q}}$

Figure 19 shows the system flow diagram.

B. PARAMETER EVALUATION

Shock Strut Characteristics

Figures 20 and 21 show the nose gear load and damping characteristics.

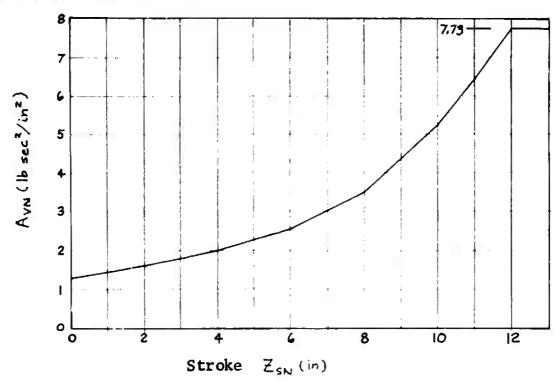


Figure 20 Nose Gear Damping Curve

Nose Tire Characteristics

See also page 57 of the flywheel system. The $22 \times 6.6-10$ 16-ply rating nose tire has a rating of 9150 lbs. at 190 psi. The deflection is 1.50 inches. The operating pressure is 190 psi. Since these are two nose tires,

(3b.37)
$$C_{NT} = \left(\frac{P}{PR}\right) \frac{F_R}{S_R} = \left(\frac{190}{190}\right) \left(\frac{2}{(1.50)}\right) = 12,200 \text{ lb/in}$$

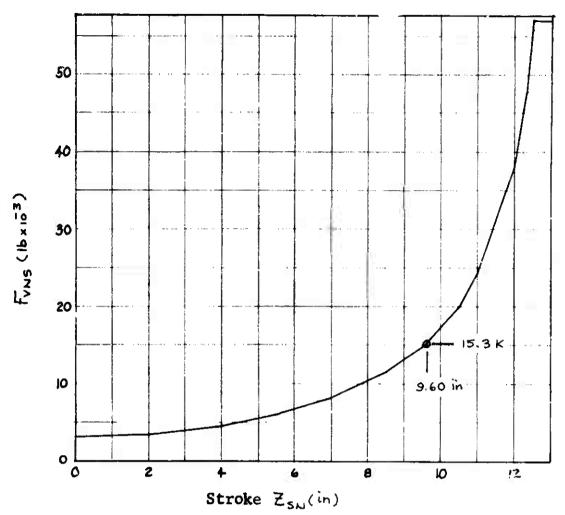


Figure 21 Nose Gear Air Load Curve

Since $\gamma = 0.1$,

(3b.38)
$$C_{NT} = \frac{72}{5R^2} \left(\frac{P}{P_R}\right) \sqrt{\frac{S_R}{6}}$$

= $\frac{(.1)(2)(9.50)}{(1.50)^2} \left(\frac{190}{190}\right) \sqrt{\frac{1.50}{386}} = 50.6 \frac{16 \text{ sec}}{10^2}$

The nose tire rolling resistance coefficient is U_{RRN} = .020 and the unsprung nose tire mass (mass of tires, wheels, axle, and lower shock strut) is W_{WN} = 175/386 = .453 LBF SEC /IN. The nose tire undeflected radius, Rerw. is 10.8 in.

Main Tire Characteristics

The main tire undeflected radius, Rorm, is 23.32 inches. The other main tire characteristics are computed as shown on page 56.

Main Gear Characteristics

The F-lll main gear spring rate parameters were computed from load-deflection data recorded during structural testing and correlated with data from jig drop tests and from flight tests.

Figure 22 shows the model which has the same form as that described in equations (3b.16) through (3b.21) and in the wheel and tire system. The rotational spring rate of one main gear about its pivot is 26×10^6 in 1b/rad. The remaining values are calculated (at static position) as:

(3b.39)
$$\begin{cases} S_{GU} = 21.0 \text{ in} \\ W_{U} = 279 \text{ lbm} = .723 \text{ lb } \text{Sec}^{2}/\text{in} \\ W_{GW} = W_{WM} = 644 \text{ lbm} = 1.667 \text{ lbf sec}^{2}/\text{in} \\ C_{G} = 200,000 \text{ lb/in} \end{cases}$$

Thus from figure 22 , (u) is given by

The first mode natural frequency of the model is 21.84 cps. Assuming that γ is .054 (about 3% critical), then evaluating the damping at $4c = (2\pi)(2i.64) = 137.5$ rad/sec there follows:

(3b.41)
$$D_G = \chi C_G = \frac{(.054)(200,000)}{(137.5)} = 78.6 \text{ lb sec}$$

(3b.42)
$$D_0 = \eta C_0 = \frac{(.059)(.55, ccc)}{(.137.5)} = 23.2 lb sec (137.5)$$

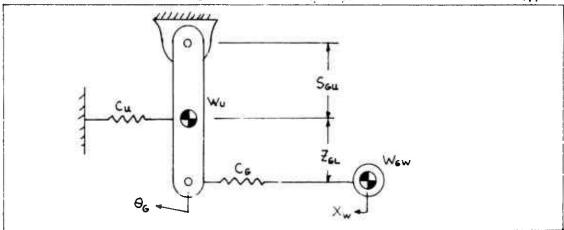


Figure 22 Main Gear Strut and Wheel Model

Aerodynamic Data

For finding the aerodynamic data, the F-111A is landing with flaps at 34° , wings swept to 26° , and spoilers applied. An equilibrium airplane condition of $\propto_{\rm w} = 2^{\circ}$ and $S_{\rm HI} = 5^{\circ}$ is assumed. For these conditions,

The aerodynamic reference point is F.S. 526.8, WL 197.2. Assuming the airplane C.G. at F.S. 519.0, WL 180.0, if Δx and Δy are given by:

$$(3b.46) \Delta x = FSA - FSCG = 526.8 - 519.0 = 7.8 inches$$

Then if $\overline{C} = 108.5$ inches is the length of the M.A.C., then $C_m\overline{C}$ at the airplane C.G. is given by:

$$(3b.48) C_{m} \bar{C} = C_{mA} \bar{C} - C_{L} \Delta X + C_{D} \Delta Y$$

$$= (0.0)(108.5) - (0.13)(7.8) + (.258)(17.2) = 34.24 \text{ Inches}$$

Also,

$$(3b.49) \frac{\partial C_{M} \bar{c}}{\partial u} = \frac{\partial C_{M} \bar{c}}{\partial u} - \frac{\partial C_{L}}{\partial u} \Delta x + \frac{\partial C_{D}}{\partial u} \Delta v$$

$$= (-.025)(108.5) - (.128)(7.8) + (0.0)(17.2) = -.371$$

Thus from equations (3b.29), (3b.30), and (3b.31),

(3b.51)
$$C_{AL} = C_{L} = 0.13$$
 $B_{AL} = (\partial C_{L}/\partial x_{W}) = .128 \text{ deg}^{-1}$
 $E_{AL} = (\partial C_{L}/\partial S_{HT}) = .022 \text{ deg}^{-1}$

(3b.52) $B_{AD} = (\partial C_{D}/\partial S_{HT}) = .0036 \text{ deg}^{-1}$
 $E_{AD} = (\partial C_{D}/\partial S_{HT}) = -.0036 \text{ deg}^{-1}$
 $E_{AD} = (\partial C_{D}/\partial S_{HT}) = -.0036 \text{ deg}^{-1}$
(3b.53) $B_{AM} = (\partial C_{MC}/\partial x_{W}) = -.371 \text{ in/deg}$
 $E_{AM} = (\partial C_{MC}/\partial S_{HT}) = -3.759 \text{ in/deg}$
(3b.54) $G_{AL} = C_{AL} - B_{AL} \times w - E_{AL} S_{HT}$
 $= .013 - (.128)(2) - (.022)(-5.0) = -.016$
(3b.55) $G_{AD} = C_{AD} - B_{AD} \times w - E_{AD} S_{HT}$
 $= .258 - (0.0)(2) - (-.0036)(-5) = .240$
(3b.56) $G_{AM} = C_{AM} - B_{AM} \times w - E_{AM} S_{HT}$
 $= 3.424 - (-.371)(2) - (-.3759)(-5) = 2.286 \text{ IN}$

initial Conditions

Assume that at time = 0.0 seconds the airplane velocity is 2400 in/sec = \dot{X} o. The airplane is shown in Figure 23 with brakes off.

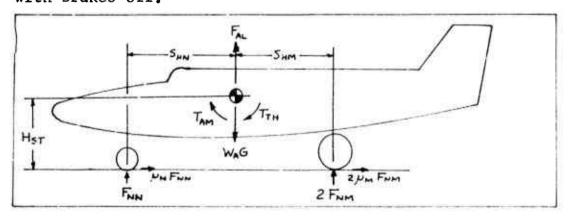


Figure 23 Airplane Initial Equilibrium Forces

Assume that $\propto w = 3^{\circ}$ and $S_{HT} = -5^{\circ}$, then from equations (3b.29) (3b.30) and (3b.31), there follows:

$$(3b.57)(AL = (-.016) + (.128)(3) + (.022)(-5) = 0.222$$

$$(3b.58)$$
 $C_{AM} = (2.286) + (-.371)(3) + (-3.759)(-5) = 19.973$

Since $S_{HN} = 258.9$, $S_{HN} = 32.6$ inches, $\overline{I}_{TH} = 20,000$ in/1b., and if the estimated value for H_{ST} is 97.2 inches, then

Now from equations (3b.24), (3b.25), and (3b.26),

$$(3b.60) Q_{A} = (2400)^{2} (525) (,00238) / 288 = 25000 | b$$

Thus,

(3b.63)
$$F_{NM} = \frac{1}{2} \left(\frac{(515304) + (257)(57000 - 5500)}{(45.1) + (97.2)(0)} \right)$$

So

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and

$$(3b.65) F_{NN} = W_{AG} - F_{AL} - 2 F_{NM}$$

= 57000 - 5500 - 2(22988) = 5524 lb

Assume that when time = 0 that $X_{WM} = 0.0$ inches, then $Z_{GD} \langle X_{WM} \rangle = 0.0$. Then $X_{WN} = 295.1$ inches so that $Z_{GD} \langle X_{WN} \rangle = (9.676-9.703)12 = -.32$ inches. Refer to the runway system for values of Z_{GD} . From equation (3b.12):

$$(3b.66)$$
 $S_{M} = (22988)/(9530) = 2.41 in$

Thus from equation (3b.13)

$$(3b.67)$$
 $Z_{wmo} = 23.32 - 2.41 = 20.91 in$

From Figure 14 in the flywheel system, if $F_{vms} = 22,950$ lbs, then $Z_{5m} = 24.00$ inches. Now, from equation (3b.4)

$$(3b.68)$$
 $S_N = (5524)/(12,200) = .46 in$

From equation (3b.5), there follows:

$$(3b.69)$$
 $\angle_{WNO} = (-.32) + (10.80) - (.46) = 10.02 in$

Also, from Figure 21, if $\Gamma_{VNS} = 5,600$ lbs. then: $Z_{SN} = 5 \, \mu$

Rearranging equations (3b.1) and (3b.9)

Solving these two equations,

Finally,

The values of the following parameters as listed in Table 6 are established by the airplane's dimensional and mass characteristics: α_0 , α_{FH} , A_{REF} , S_{EL} , S_{HM} , S_{HM} , S_{VM} , S_{VM} , S_{TH} , W_A and W_{IQ} .

For the example problem the density of air at standard conditions, sea level and 59.6° F, is assumed. Thus, $R_{HA} = .00238 \ S/uqs / Ft^{3}$

The shock strut linear damping coefficients, Dvs for the nose gear and Dvm for the main gear, are set equal to zero for the example problem.

Table 6 Airplane System (3 Degree) Parameters

SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
×	ပ	00	429	Incidence
٨	ပ	052	٢٠٩٩	Angle between Thrust & and W.L.
3	>		George	
A و ا	U	525	£ ₇ 2}	Wing Ref. Area
A	*>		16 sect/in2	M.G. Shock Strut Damping Charac-
A	*>		16 sec / in2	N.G. Shock Strut Damping Charac-
•				
BAD	υ	0.0	مرودي ا	Aero Drag Parameter
B _{AL}	υ	.128	2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2	Aero Lift Parameter
BAM	υ	371	11 / deg	Aero Moment Parameter
CAR	>		1	Aero Drag Coefficient
(a)	>		1	Aero Lift Coefficient
Q A A	!>		, <u>,</u>	Aero Moment Coefficient
(N1F	υ	553c	lb/in	
- Z	ဎ	12,200	1b/in	N.G. Tire(s) Vertical Spring Rate
CL	O	59,000	16/11	Drag Brace - Strut Spring Rate
DAT	υ	38.8	16 sec/in2	Tire Vertical Damping
DNI	U	50.0	16 sec/ir.2	Tire Vertical Damping
2	υ	23.2	16 5ec / in	Brace - Strut
~ ^ C	ပ	0.0	16 section	Strut Damping
D	υ	0.0	16 sec/in	N.G. Strut Damping Coefficit
EAU	ပ	6636	deer	Aero Drag Coefficient
EAL	U	.622	, , , ,	Ŭ
E A P	ပ	-3.755	in deep	Aero Moment Coefficient
FAD	>		0	Aero Drag
FAL	>		a _l	Aero Lift
NO	>		٩١	
TO	>		٩	Horizontal Load at M.G. Pivot

Point Plot Input

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		Tabl	Table Conta)	
SYMBOL	TYFE	VALUE	UNITS	DESCRIPTION
Π	(I) ^		, م	Horizontal Load on M.G. Axle
2 2	(o) ₀		91	
2.7	>		4	N.G. Tire Normal Load
F _T H	υ	1000	<u></u>	Engine Thrust
>H_T	>		4	Vertical Component of Engine
ł				Thrust
7	>		4	Load in Fictitious Drag Brace
FVP1	>		<u>ē</u> .	Shock Strut Loag (M.G.)
* \$147 L	>		<u>a</u>	Shock Strut Air Load (M.G.)
2>11	>		<u>.a</u>	Shock Strut Load (N.G.)
• v: Z >	>		ना	Shock Strut Air Load (N.G.)
·S	ပ	38c	in/sec2	Gravitational Constant
GAB	O	.240	1	Aero Drag Parameter
رعالا	U	310	1.	Aero Lift Parameter
(5.9M)	ပ	2.286	2	Aero Moment Parameter
s Oc	(0) ^		7.34	M.G. Rotation from Vertical
J. 6.0	ပ	.0329	rad	Go at Time = 0 Sec.
Θ_{c}	(0) ^		rad/sec	Angular Velocity of Main Gear
• 1				Strut
0000	ပ	0.0	rad/sec	Q at Time = 0 Sec.
s S	>		rad/ >ec 2	Angular Acceleration of Main
1				Gear Strut
PARV	(I)^		9	Tire Vertical Unbalance
œ	>		٠٠ عرا	Angle of APL W.L. to Horizontal
((Pitch)
3°	ဎ	.0329	rad	Q at Time = 0.0 Sec.
g.:	(0)^		rad/56c	APL Pitch Rate
ŝ	ပ	0.0	rad/ sec	APL Pitch Rate at Time = 0.0 Sec.
	Ī			

Point Plot Input

Table 6 (Contd)

,		754	יים כל כני בכן	
SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
•				
O	>		rach/sec2	APL Pitch Acceleration
Q	>		a.	Aerodynamic Pressure x AREF
Z Z	υ	,00238	51cq/H3	Air Density
Roim	υ	23,32	, 5	M.G. Tire Undeflected Radius
Retz	ပ	10.80		N.G. Tire Undeflected Radius
56.	Ü	26.50		334333111333133313331333133313331333133
Seu	υ	21.00	S	*
5.1	ပ	36.20	2.	*
225	ပ	258.80	, c,	*
SHT	v(I)		daes	Horizontal Tail Deflection
5m	(0)^		יי מי	M.G. Tire Deflection
S.	>		10/20C	M.G. Tire Deflection Rate
SVAK	Ü	36.74	.2	*
ς. Υ.	>		. 5	N.G. Tire Deflection
2	>		in/sec	
SVM	v	84.24	in	
SVN	v	78,58	.5.	*
574	>	20.00	د.	*
TAM MA	>		q1 ui	Aero Moment
-5	(I)^		٠. م	Moment on M.G. Axle
-1. 1.	ပ	20,000	ا من	Moment at C.C. due to Thrust
UREN	ပ	.020	1	N.G. Tire Rolling Resistance
				Coefficient
× ×	ပ	147.6	16 Section	APL Mass
Wig	ပ	3.66 ×106	15 sectin	APL Pitch Moment of Inertia
				About C.G.
Y X	ပ	.723	16 sectin	M.G. Upper Strut Mass
Www	U	1.99.1	16 sec2/in	M.G. Unsprung Mass

* See Figure 16

Table 6 (Contd)

SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
N. N.	v	.453	16 sectin	N.G. Unsprung Mass
×	>		74	Horizontal C.G. Location of APL
×	ပ	34.20	4.1	C.G. Location at Time = 0
•×	>		in/sec	APL Velocity
·×	υ	2400	in/sec	APL Velocity at Time = 0
×	>		in/sec ²	APL Acceleration
XAX	(0)^		2	M.G. Axle (Undeflected) Location
××××	(0)^		in/sec	M.G. Axle Velocity (Undeflected)
XXX	v(I)		د. 2	
×.×.	(I) ^		,n/sec	Axle Velocity
2 3 ×	>		2,2	
2 ×	>		in/sec	N.G. Axle Velocity
7	>		.5.	Vertical Location of APL C.G.
Zo	Ü	82.36	.5.	Vertical Location of APL C.G.
•				at Time = 0
M	>		in/80c	APL Vertical Velocity
.พื	U	0.0	in/sec	APL Vertical Velocity at Time = 0
Z.	>		in/sec ²	APL Vertical Acceleration
260	(I)^		2	Runway Contour Height
Z602	v(I)		in/in	Runway Contour Slope
Lor	>		ż	Distance from Mass Wu to Strut
				Axle
7.5 M	>		5.	M.G. Stroke
ZSM	>		in/sec	M.G. Stroke Velocity
255	>			
Zz.	>		in / scc	N.G. Stroke Velocity
Kwn	>		ני	M.G. Axle Height

Table 6 (Contd)

DESCRIPTION	M.G. Axle Height at Time = 0 Sec.	M.G. Axle Vertical Velocity at	M.G. Axle Vertical Acceleration	N.G. Axle Height at Time = 0	N.G. Axle Vertical Velocity N.G. Axle Vertical Velocity at	N.G. Axle Vertical Acceleration
UNITS	. 2	in/sec	in/sec2	<u> </u>	in/sec in/sec	in/sec²
VALUE	20.91	0.0		10.02	0.0	
TYPE	υ:	> U	>	> 0	> U	>
SYMBOL	Zwmc	0 × 3 × 3 × 3 × 3 × 3 × 3 × 3 × 3 × 3 ×	Zwm	N N 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	H. W. N. O.	W.

3c. AIRPLANE SYSTEM (6 DEGREE)

The six-degree airplane system is built around a rigid body airplane which is allowed to move vertically and horizontally (both parallel and perpendicular to the runway centerline). Also, the airplane's yaw, pitch, and roll effects are considered. This model considers all the effects found in the three-degree airplane system. The purpose of the six-degree airplane is primarily two-fold: the first is to evaluate the effects of the anti-skid system on the airplane's directional stability; the second is to evaluate any anti-skid system degradation caused by airplane yaw and side drift movement.

For the nose gear, the model considers the tire and strut characteristics in the vertical direction. Also, the nose tire's yawed rooling characteristics are included. The steering loop is closed by providing a "pilot" function which provides an input to the nose tire. The "pilot" function depends on the airplane's yaw angle. The two main gears are treated as two distinct systems except for any structural coupling which may exist between the two. Provisions are made for side wind perturbation and for aerodynamic effects caused by airplane yaw and roll.

A. Mathematical Description

Figure 24 shows the six coordinates which describe the airplane position relative to reference points on the earth's surface.

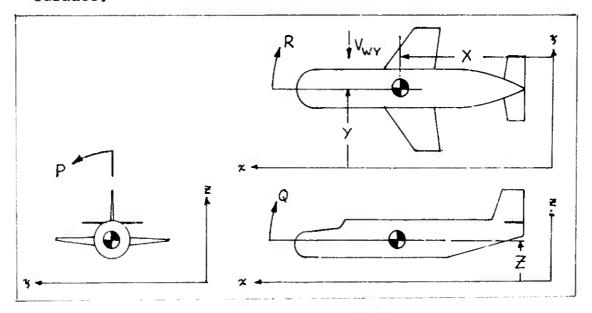


Figure 24 Airplane Coordinates

 V_{WY} is a crosswind. The runway is oriented so that its centerline coincides with the x axis for 0 inch runway heights ($Z_{\text{GD}} = 0$). This analysis assumes that the pitch (Q) and roll (P) angles are small. Let $Z_{\text{GD}}\langle x,y\rangle$ denote the runway profile and let $Z_{\text{GDP}}\langle x,y\rangle$ denote the runway slope ($Z_{\text{GDP}}\langle x,y\rangle = \partial Z_{\text{GD}}\langle x,y\rangle/\partial x$). Figure 25 shows the airplane as measured in the fuselage station-water line reference system.

Nose Gear

でもととなる。などのなかな、このでも、たち、女父女女女女を、女父女子を名、他の女女女女女の

の場合ということには、関係などのなどとなる。

Let Z_{5N} and Z_{5N} denote the nose gear stroke and stroke velocity. Then we have that:

The mose gear shock strut force F_{v_N} is then given by:

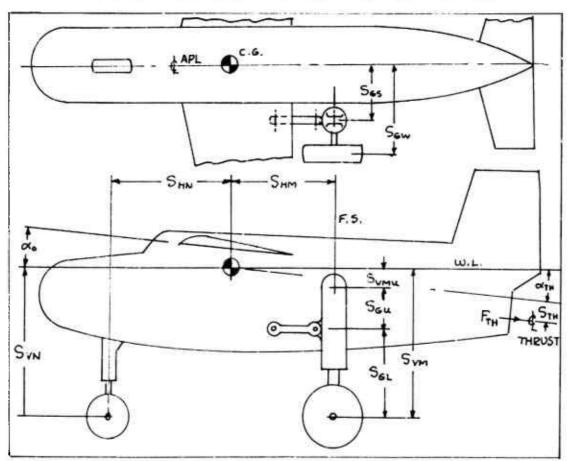


Figure 25 Airplane Geometry

Figures 26, 27, and 28 show the forces acting on the airplane as seen in the different planes. Let F_{LN} denote the lateral force on the nose wheel at the axle. Then:

Where F_{SNS} is the lateral component of the sliding or cornering force of the nose tire. The load F_{LN} is caused by the nose wheel trying to move laterally relative to the airplane. If this lateral displacement is denoted by Y_{DLN} , then:

Now F is given by:

where

Summing vertical forces on the nose gear unsprung weight:

Assume that the pilot positions the nose wheel with a rate proportional to the airplane yaw angle. Thus:

$$(3c.12) \dot{\theta}_{N} = \begin{cases} \min\{0, -G_{PIL}R & \text{if } \Theta_{N} \geq \Theta_{NMAX} \\ -G_{PIL}R & \text{if } |\Theta_{N}| \leq |\Theta_{NMAX}| \end{cases}$$

$$\max\{0, -G_{PIL}R & \text{if } |\Theta_{N}| \leq -\Theta_{NMAX} \}$$

 Θ_N gives the yaw angle of the nose wheel with respect to the airplane φ . The yaw angle of the tire with respect to its direction of motion is given by Θ_{YAW} .

$$(3c.13) \theta_{YAW} = \theta_N + R - (\dot{Y}_N / \dot{X}_{WN})$$

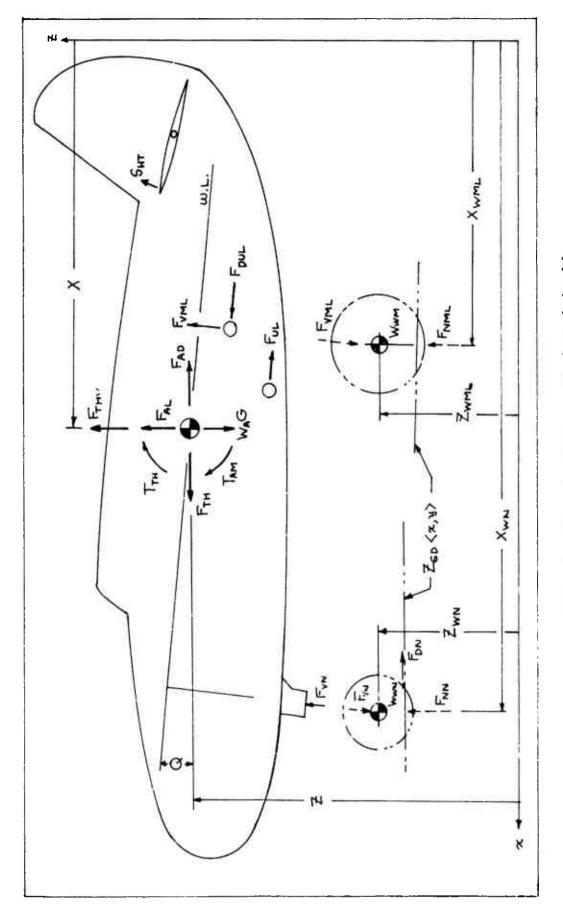


Figure 26 Airplane Dynamics (Pitch)

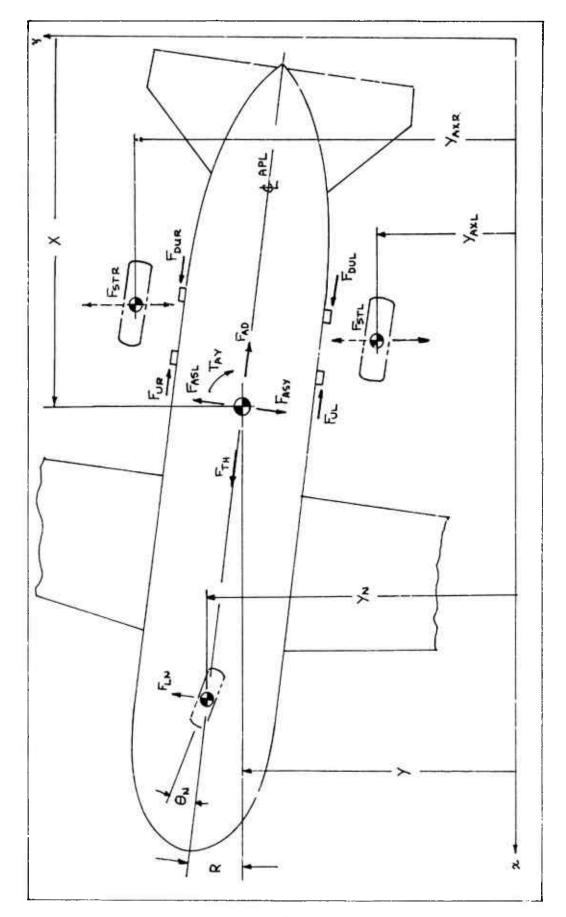


Figure 27 Airplane Dynamics (Yaw)

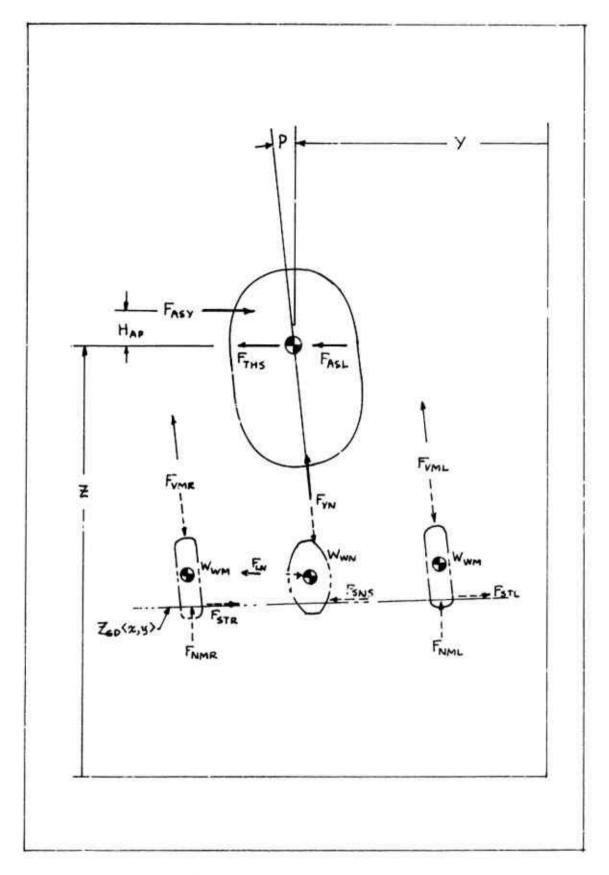


Figure 28 Airplane Dynamics (Roll)

The steering characteristic is developed from Reference 1 (p. 30). Let $U_{\rm NTF}$ be the coefficient of friction between the nose tire and the ground. Then the maximum force normal to the tire in the plane of the ground is $F_{\rm NTF}$ where:

Using equation (79) and 80) from Reference 1:

(3c.15)
$$U_{RT} = \begin{cases} P_{WC} \Theta_{YAW} / F_{NTF} & \text{if } F_{NTF} > 0 \\ 0 & \text{if } F_{NTF} \leq 0 \end{cases}$$
(3c.16) $F_{NCFS} = \begin{cases} F_{NTF} & \text{if } U_{RT} \geq 1.5 \\ F_{NTF} & \text{if } U_{RT} > 1.5 \end{cases}$

$$= \begin{cases} F_{NTF} & \text{if } U_{RT} \geq 1.5 \\ F_{NTF} & \text{if } U_{RT} \leq -1.5 \end{cases}$$

Thus, F_{NCFS} corresponds to $F_{\Psi,r,e}$ in Reference 1 and Pwc is the cornering power given by:

(3c.17)
$$P_{WC} = \begin{cases} C_{P1}S_N - C_{P2}S_N^2 & \text{if } S_N \leq S_{P1} \\ C_{P3} - C_{P4}S_N & \text{if } S_N > S_{P1} \end{cases}$$

The actual normal cornering force F_{NCF} is not F_{NCFS} , but lags F_{NCFS} because of the tire relaxation length. The expression for F_{NCF} is given by:

Having obtained F_{NCF} , then from Figure 29,

(3c.19)
$$F_{SNS} = F_{NCF} \cos \langle \Theta_N + R \rangle - U_{RRN} F_{NN} \sin \langle \Theta_N + R \rangle$$

(3c.20) $F_{DN} = F_{NCF} \sin \langle \Theta_N + R \rangle + U_{RRN} F_{NN} \cos \langle \Theta_N + R \rangle$

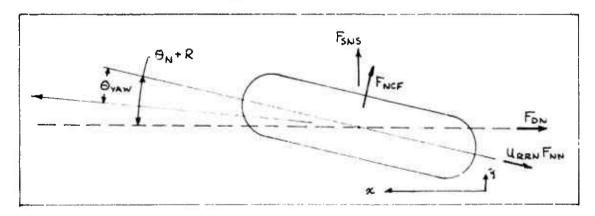


Figure 29 Nose Tire Cornering Force

Main Gear

Let Z_{SM} and Z_{SM} denote the stroke and stroke velocity. The additional subscripts L and R refer to the left and right side of the airplane (looking forward).

The main gear shock strut forces are then given by:

Let S_M denote the main gear tire deflection and let F_{NM} be the associated load. Thus, in the vertical direction, the relation between the load and tire deflection is given as follows:

Summing forces in the vertical direction on the main gear wheels,

Figure 30 shows a side view of the left hand main gear. With the assumption that $W_u << W_A$, Θ_{GR} and Θ_{GL} are described by:

$$(3c.35)W_{u}S_{6u}^{z}\ddot{\theta}_{GR} = S_{GU}F_{UR} + (S_{6U} + Z_{GLR})(F_{TL} - F_{TR} - F_{GR}) - T_{SR}$$

$$(3c.36)W_{u}S_{6u}^{z}\ddot{\theta}_{GL} = S_{GU}F_{UL} + (S_{GU} + Z_{GLL})(F_{TR} - \overline{F}_{TL} - F_{GL}) - T_{SL}$$

where

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The forces F_{TR} and F_{TL} are used to impart the correct moment into the gear.

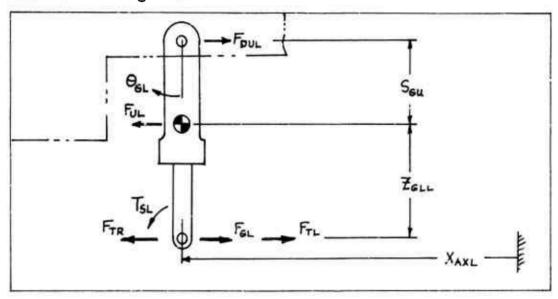


Figure 30 Side View of the Main Gear Strut

The overall gear system model is shown in Figure 31. In order to transmit torque properly, the forces F_{TRO} and F_{TLO} are applied equal and opposite on different sides of the gear. Thus,

If it is assumed that 100 $\rm H_A$ percent of this torque is taken directly into the airplane, then 100 $\rm H_G$ = 100-100 $\rm H_A$ percent is transmitted through the gear. Thus,

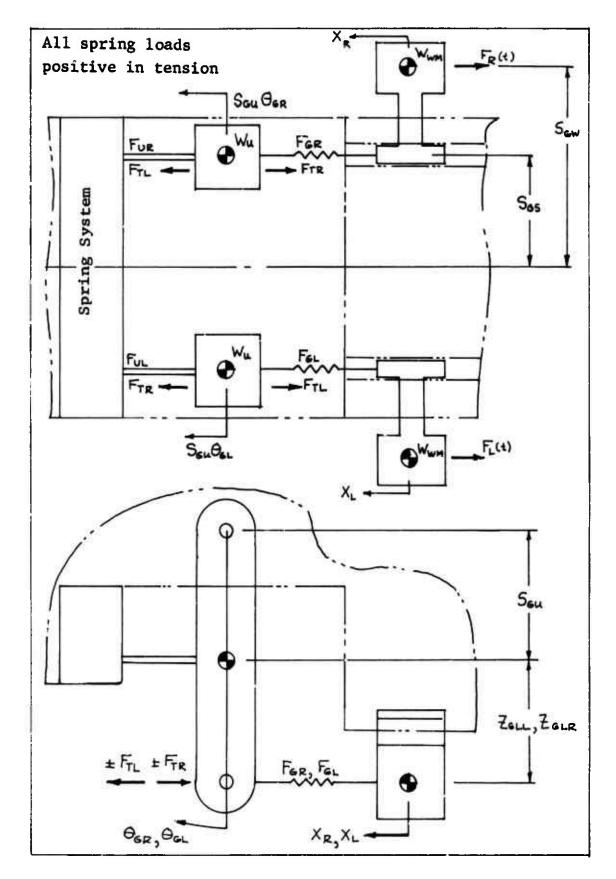


Figure 31 Main Gear Model

Let Q_R and Q_L be the difference between the gear rotation and the airplane rotation. That is,

$$(3c.43)$$
 $Q_R = Q - \Theta_{GR}$

$$(3c.44) Q_{L} = Q - \theta_{GL}$$

$$(3c.45)\dot{Q}_{R} = \dot{Q} - \dot{\theta}_{GR}$$

Then we can find constants C_{u_1} , C_{u_2} , D_{u_1} , and D_{u_2} such that:

It then follows, assuming negligible strut moment of inertia that:

As outputs to the tire and wheel systems we need to compute X_{AX} and Y_{AX} . X_{AX} is shown in Figure 30. Y_{AX} is assumed to be the undeflected tire footprint position in the y direction.

Engine Thrust

Referring to Figures 26 and 27, if F_{TH} is the engine thrust, then

Aerodynamics

The following eight equations apply as in the three-degree model.

$$(3c.62)$$
 $Q_A = \dot{X}^2 A_{REF} R_{HA} / z_{BB}$

$$(3c.66) \propto w = \propto_0 + (180/\pi)(Q - \frac{2}{x})$$

Let V_{WY} denote the wind gust velocity as shown in Figure 24 If Ψ and β are defined by:

$$(3c.70) \Psi = (\bigvee_{w_{Y}} + \dot{y}) / \dot{x}$$

$$(3c.71)$$
 $\beta = (180/\pi)(\Psi - R)$

Then β is the angle of sideslip.

Let Q_{AT} denote the dynamic air pressure (including side wind) multiplied by the reference area. Then:

$$(3c.72) Q_{AT} = ((V_{WY} + \dot{Y})^2 + \dot{X}^2) A_{REF} R_{HA} / 288$$

Then the aerodynamic yaw moment is given by:

and the aerodynamic side force is given by:

Finally, an aerodynamic force F_{ASL} due to a combination of lift and pitch is:

Refer to Figure 27 as to the direction of these forces.

Dynamics

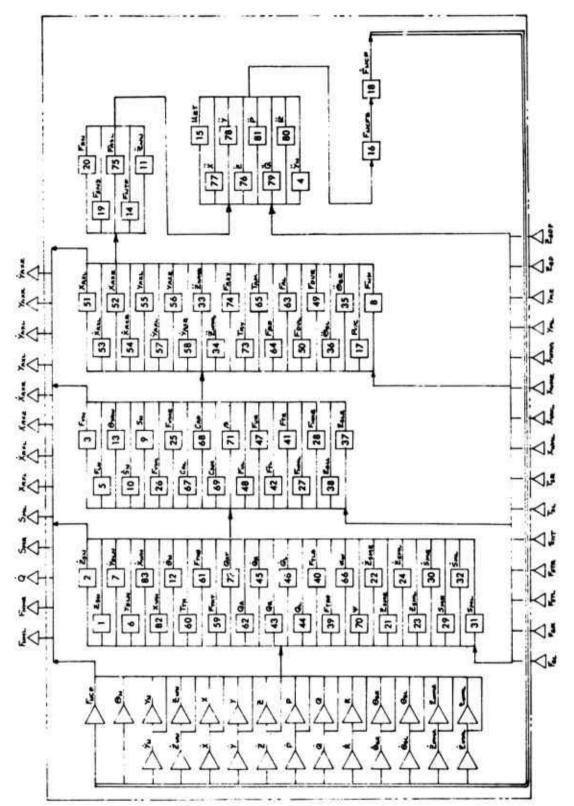
Referring to Figures 26 and 27, summing forces in the x, y, and z direction,

Summing moments about the C.G. we have:

$$(3c.81)_{W_{IP}} \ddot{P} = (F_{VML} - F_{VMR}) S_{GW} + F_{ASY} H_{AP} - (Z - Z_{GP}(X, Y)) (F_{STR} + F_{STL} + F_{LN})$$

$$(3c.82) \times_{WN} = X + S_{HN} + S_{VN}Q$$

$$(3c.83) \dot{x}_{WN} = \dot{x} + S_{VN} \dot{Q}$$



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Airplane System (6 Degree) Equation Flow Diagram 32 Figure

В. Parameter Evaluation

Nose Gear Characteristics

Based on a nose gear lateral natural frequency of 12 cps, we have $\omega_n = 2\pi(12) = 75.5$ RAD/SEC. Since $W_{WN} = .435$, then:

$$(3c.84) C_{LN} = W_{WN} \omega_{n}^{2} = .435 (75.5)^{2} = 2480 \text{ lb/in}$$

Using $\eta = .054$ as in the calculation of D_G in the threedegree model.

(3c.85)
$$D_{Liu} = \gamma C_{LN}/\omega_n = (.054)(2480)/75.5 = 1.78$$
 lb sec/in

The steering or cornering characteristic parameters are obtained from Reference 1. Based on Figure 44(a) in Reference 1, the value for UNTE is:

Using equation 82 from Reference 1, if $K = (P + .44P_R)w^2 = (1.44)(190)(6.6)^2 = 11,920$ lb. then:

shows that the equation which describes the curves in Figure 43 is given by:

(3c.92)
$$F_{y,r} = (1 - e^{-\alpha/Ly}) F_{y,r,max} \langle \Theta_{y,pw} \rangle$$

where Ly is the tire yawed rolling relaxation length. Differentiating this equation, there follows:

(3c.93)
$$\frac{dF_{y,r}}{dx} = \frac{e^{-x/Ly}}{L_y} F_{y,rmax} \langle \Theta_{yAw} \rangle$$

Eliminating e^{-x/L_y} results in:

(3c.94)
$$F_{y,r} + L_y \frac{dF_{y,r}}{dx} = F_{y,r} \frac{dF_{y,r}}{dx} = F_{y,r} \frac{dF_{y,r}}{dx}$$

Equation (3c.18) is obtained by using:

(3c.95)
$$\frac{dF_{y,r}}{dx} = \frac{dF_{y,r}}{dt} / \frac{dx}{dt} \approx \frac{\dot{F}_{NCF}}{\dot{X}_{WN}}$$

where it is assumed for large airplane velocities that $\dot{X}_{WN} = dx/dt$. We see that the parameter S_{YRL} is the relaxation length. From Figure 39 of Reference 1, for most conditions, S_{YRL} is obtained from:

(3c.96)
$$S_{YRL} = .6w(2.8 - .8 P/P_r)$$

= (.6)(6.6)(2.8 -.8) = 7.92 in

Main Gear Characteristics

For many airplanes which have a conventional strut arrangement (similar to a B-58) most of the moment about the shock strut ϕ is taken out through the shock strut. In this case equations (3c.41) and (3c.42) would use $H_G = 0.0$. In the case of the F-111 gear the opposite result occurs so that $H_G = 1.0$ and $H_A = 0.0$. The following values apply to the F-111 gear:

(3c.97)
$$\begin{cases} W_{u} = .723 \text{ lb sec}^{2}/\text{in} \\ W_{wM} \cdot W_{wv} = 1.667 \text{ lb sec}^{2}/\text{in} \\ S_{Gu} = 21.00 \text{ in} \\ S_{Gw} = 60.00 \text{ in} \\ S_{GS} = 20.00 \text{ in} \\ H_{G} = 1.0 \\ H_{A} = 0.0 \end{cases}$$

If loads $F_R(t) = F_L(t) = F_0$ are applied as shown in figure 31, then because of symmetry, the result will be that $Q_R = Q_L$. But then equation (3c.47) says that $C_{UI} - C_{UZ} = F_{UR} / S_{GU} Q_R$ but $C_U = F_{UR} / S_{GU} Q_R$ as shown in the 3 degree model. Thus

With the main gear at static, if a drag load of 18,000 lb. is applied to the left gear at the ground and -18,000 lb. is applied to the right gear at the ground the observed deflections with Q = 0 are $Q_1 = .0236$ rad and $Q_R = -.0236$ rad. (Assuming a lateral beam torsional spring rate of 43.0×10^6 in lb/rad).

In the equations which describe the gear loading T_{SR} and T_{SL} can be chosen as 0 if Z_{GLL} and Z_{GLR} are the dimensions to the ground instead of the axle. Thus $Z_{GL} = Z_{GLL} = Z_{GLR} = 2.2 + 12.9 = 21.4$ in. Equations (3c.35), (3c.36), (3c.39), (3c.40), (3c.41) and (3c.42) can then be combined to give

(3c.99)
$$F_{UR} - F_{UL} = \left(\frac{S_{GU} + Z_{GL}}{S_{GU}}\right) \left(F_{GR} - F_{GL}\right) \left(1 + H_G\left(\frac{S_{GW} - S_{GS}}{S_{GS}}\right)\right)$$

= $\left(\frac{21.0 + 21.4}{21.0}\right) \left(-36000\right) \left(1 + \left(\frac{60 - 20}{20}\right)\right) = -212,000$

Subtracting equation (3c.48) from (3.47) results in

So that

$$(3c.101)$$
 $C_{k1} + C_{k2} = \frac{-212000}{(2)(21.0)(-.0236)} = 214,000 \text{ lb/in}$

Adding and subtracting equations (3c.98) and (3c.101) results in

$$(3c.102)$$
 Cui = $\frac{59000 + 214000}{2} = 136,500 \text{ lb/in}$

$$(3c.103)$$
 $C_{UZ} = 214,000 - 59000 = 77,500 lb/in$

At a fore and aft natural frequency of 137.5 rad/sec, the damping coefficients D_{u_1} and D_{u_2} are given as

(3c.104)
$$D_{u1} = \chi C_{u1} / \omega = \frac{(.054)(1.36 \times 10^5)}{(137.5)} = 53.4 \text{ ib sec/in}$$

(3c.105)
$$D_{u2} = \gamma C_{u2}/\omega = \frac{(.054)(.775 \times 10^5)}{(137.5)} = 30.5$$
 lb sec/in

Aerodynamic Characteristics

The coefficients for equations (3c.62) thru (3c.69) have been derived in the 3 degree model. For the F-111A in the landing configuration and wings swept to 26 degrees as described in the 3 degree system, $C_{N/3} = .0014$ and $C_{y/3} = -.021$. Then the coefficient C_{Ay} is calculated from

Let \triangle X = FSA - FSCG as in the 3 degree system where FSA = 526.8 and FSCG = 519.0. Let b be the wing span. If b = 756 in., then

(3c.107)
$$C_{AN} = b C_{N/3} - \Delta X C_{Y/3}$$

(3c.108) $C_{AN} = (756)(.0014) - (7.80)(-.021) = 1.222 in/deg$

Airplane Characteristics

The parameters listed in Table 7 describing the airplane's dimensional and mass characteristics are those previously derived in the 3 degree model or simply a listing of the appropriate values applicable to the F-111 for which no derivation or computation is required.

Table 7 Airplane System (6 Degree) Parameters

では、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、10mmのでは、1

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DESCRIPTION	Wing Angle of Incidence	Angle between Thrust & W.L.	Wing Angle of Attack	Reference Area	Shock Strut Damping	N.G. Shock Strut Damping Coeff.	Aero Drag Parameter	Aero Lift Parameter	Aero Moment Parameter	Angle of Sideslip	Aero Drag Coefficient	Aero Lift Coefficient	Aero Moment Coeff. (Pitch)	Aero Moment Coeff. (Yaw)	Aero Side Force Coeff.	Nose Gear Lateral Spring Rate	M.G. Tire Vertical Spring Rate	N.G. Tire(s) Vertical Spring Rate		Parameters for Pwc			Drag Brace Characteristic	Spring Rates	Nose Gear Lateral Damping Coeff.	M.G. Tire Vertical Damping Coeff.	N.G. Tire(s) Vertical Damping	Coefficient
UNITS	deg	r'a d	gap	42	lb sec²/in²	16 sec2/in2	deg_!	des	in / dea	deg	b I	t	.5	in/deg	dee	15, in	15/in	lb/in	lb/rad in	16/radina	1b/rad	16/rad in	1b/in	14/50	lb sec/in	ib sec/in2	16 sec/in2	
VALUE	1.00	052		525.0			0.00	.128	371					1.222	.021	2480	9530	12,200	37,060	12,353	45,794	10,500	1.365 × 10 ⁵	.775×10E	1.78	38.8	50.6	
TYPE	v	υ	>	U	*>	*^	v	v	v	>	>	>	>	υ	v	v	v	υ	v	v	U	ပ	Ų	o	ပ	Ų	Ų	
SYMBOL	૾ૢ	A TH	ά ¥	Ager	AVM	Ave	BAD	BAL	DAN	C	CAD	7	Σ Σ	200	ر ک	2	C A	Cr	رة	C _{P2}	C P3	7	ر ر	Ckz	O	DmT	DNT	

Table 7 (Contd)

DESCRIPTION	Drag Brace Characteristic) Damping Coefficient	M. G. Shock Strut Linear	Damping Coefficient	N. G. Shock Struc Linear	Dampire Coefficient	Aero Drag Ccefficient	Aero Lift Coefficient	Aero Moment Coefficient	Aero Drag	hero Lift	Side Force Due to Aero Lift	Side Force Due to Yaw	N. G. Rolling Resistance	\ Horizontal Load at M. G. Pivot		Horizontal Load on M. G. Axle		Lateral Nose Gear Load	Normal Cornering Force	Normal Cornering Force at Time	0 #	Time Derivative of Normal	Cornering Force	Steady State Normal Cornering	Force	M. G. Tire Normal Load	
UNITS	ib sec/in	16 sec/in	16 sec/in		lb sec/in		deg_	1 600	in/deg	, વ	<u>a</u>	<u>a</u>	<u>a</u>	9	<u>a</u>	9	41	<u> </u>	<u>a</u> .	<u>a</u>	9		lb/sec		<u>-a</u>		9	ib
VALUE	53.4	30.5	0.0		0.0		0036	.022	- 3.759												0.0							
TYPE	U	υ	U		υ		U	U	υ	>	>	>	>	>	>	>	v(I)	v(I)	>	>	υ		>		>		(o) x	(o) _A
SYMBOL	Dui	D _{44,2}	Dym		Dvz		E, AD	F. A.	FA A	FAD	FAL	FASL	FASY	2 الد	ייסר. העסר	ירן סטו <i>צ</i>	For	الـ بى	۳ 5	IL OZ	FUCFO		FNCF	١	PACES.		T NM L	الايم الايم

Table 7 (Contd)

DESCRIPTION	N.G. Tire Normal Load	Nose Tire Friction Force	Nose Tire Lateral Force	M. G. Lateral Tire Force		M. G. Loads for Torque	Takeout Correction		_	Engine Thrust	Vertical Component of Engine	Thrust	Side Component of Engine Thrust) M. G. Loads in Ficticious Drag	} Brace		M. G. Shock Strut Load			N. G. Shock Strut Load	N. G. Shock Strut Air Load Curve	Gravitational Constant	Aero Drag Parameter	Aero Lift Parameter	Aero Moment (Pitch) Parameter	Pilot's Steering Gain	Torque Adjustment Parameter	TA + T6 " -	$\mathbf{\circ}$	ADOVE C. G.
UNITS	<u>a</u>	9	ī.	ھ	91	4	41	<u>-a</u>	ব	╼	4		ف	٩		٩	<u>=</u>	<u>a</u>	4 1	4	9	in/sec ²	1	ı	. <u>e</u>	sec_	ı		ri,	
VALUE										1000.												386	240	910'-	2,286	9.0	0.0		0.0	
TYPE	>	>	>	v(I)	v(I)	>	>	>	>	U	>		>	>		>	>	>	*	>	*	O	ပ	ပ	O	U	U		ပ	
SYMBOL	Γ. Σ	η η η	FSNS	FSTL	FSTR	بر ر	FTLO	7,78	F 7 7 8 9	Į.	F _{TH} \		FTHS	$F_{\nu_{\rm L}}$		با. م	T VML	FVMR	FVMS	۳. چ:پ	Fras	ტ	GAD	GAL	GAM	GPIL	ĭ		a d	

*Point Plot Input

Table 7 (Contd)

1.0	SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
V	I	υ	0.1	١	Torque Adjustment Parameter
0.0 rad/sec v rad/sec	o O	>		P. C.	Nose Wheel Turn Angle Relative
C					to Aprile.
Vad /seco329	Φ.	v	o o	rad	$\Theta_{\rm N}$ at Time = 0
V .0329 rad co .0329 rad sec .0329 rad sec .0329 rad sec .000 rad sec	O _N	>		rad / sec	d θ_N/dt
V .0329 rad (sec0329 rad / sec0329 rad / sec0329 rad / sec	O.R.	>		rad) M. G. Strut Rotation from
C .0329 rad c .0329 rad / sec .0329 rad / sec .0329 rad / sec .000 rad .000					Horizontal
C .0329 rad / sec .0329 rad / sec .0329 rad / sec .0329 rad / sec .000 rad / sec	96,	>		rad	
C 0329 rad / sec. V 0.0 rad / sec. C 0.0 rad / sec. V 0.7 rad / sec. V 0.7 rad / sec. V 0.7 rad / sec. V 0.0 rad / sec. V 0.0 rad / sec. V 0.0 rad / sec. (b) rad rad / sec. 16 / rad rad / sec. 17 / rad rad / sec. 18 / rad rad / sec. 19 / rad	0,00	υ	,0329	rad	\ \theta_c at Time = 0
Yad sec	OGRO	υ	,0329	rad	•
C	6 6L	>		rad / sec	Angular Velocity of M. G. Strut
C 0.0 rad/sec rad/sec rad/sec rad/sec rad/sec rad sec rad ra	OGR	>		rad/sec	-
C 0.0 rad/sec rad/sec rad/sec rad/sec rad sec rad	Ó ero	U	0.0	rad/sec	} ⊖ at time = 0
v v v v v v v v v v v v v v v v v v v	OSEO	υ	0.0	rad/sec	
v v rad rad v v v v v v v v v v v v v v v v v v v	ğ.	>		rad/sect) Angular Acceleration of M. G.
v					Strut
C 0.7 rad rad rad 5ec 0.0 rad/sec rad/sec 0.0 rad 0.0	Θ_{er}	>		rad/sec ²	
V	Bumax	υ	0.7	rad	Maximum Nose Wheel Turning Angle
C 0.0 rad rad sec rad	BYAW	>		rad	Nose Wheel Turning Yaw Angle
C 0.0 rad / sec C 0.0 rad / sec V rad / sec V rad / sec² V rad / sec² Ib / rad C .0329 rad	→	>		rad	Angle of Relative Wind
C 0.0 rad/sec V rad/sec V rad/sec V rad/sec V rad/sec C .0329 rad	۵.	>		rad	Airplane Roll Angle
C 0.0 rad/sec V rad/sec V lb/rad V rad C .0329 rad	œ.	v	0.0	7.5	P at Time ≈ 0
C 0.0 rad/sec V rad/sec ² (b/rad V rad C .0329 rad	۵.	>		rad/sec	Airplane Roll Rate
v	·o°	υ	0.0	rad/sec	Pat Time = 0
v rad rad c0329	ıo.	>		rad/sec2	Roll Acceleration
c ,0329 rad	مٍ م	>		16/rad	Nose Tire Cornering Power
c .0329 rad	œ	>		ræd	Airplane Pitch Angle
	අ	v	6280'	rad	Q at Time = 0
V(0)	.თ	(0)^		rad/sec	Pitch Rate

Table 7 (Contd)

DESCRIPTION	Q at Time = 0	Pitch Acceleration	Aero Press X Aref	Aero Press X Aref (Includes Vwy)	Angular Position and Velocity	of M. G. Relative to the Airplane		-	Airplane Yaw Angle	R at Time = 0	Yaw Rate	Řat Time ≈ 0	Yaw Acceleration	M. G. Tire Undeflected Radius	N. G. Tire Undeflected Radius	Air Density	4	++	++	#	{}	++	Horizontal Tail Deflection	M. G. Tire Deflection		\ M. G. Tire Deflection Rate		N. G. Tire Deflection	N. G. Tire Deflection Rate
UNITS	rad/sec	rad/sec ²	<u>4</u>	91	rad	rad/sec	740	rad/sec	78.0	rad	rad/sec	rad/sec	rad/ sec 2	2.	43	slug/ft3	ç	۲,	.5.	.2	.2	£	deg	in	'n	in/sec	in/sec	ن	in/sec
VALUE	0,0									0.0		0.0		23.32	10.80	.00238	26.50	20.00	21.00	60.00	36.20	258,90							
TYPE	U	>	>	>	>	>	>	>	>	O	>	Ú	>	Ú	υ	Ů	υ	O	υ	ပ	ပ	ပ	v(I)	(o) ^	(o) _A	>	>	>	>
SYMBOL	-ලු	፦ଫ	ð	PAT	O.	.ઌૺ	Q	·ở	2	ϡ	·œ	·œ	:œ	Retw	Roth	RHA	SeL	565	Seu	S6×	Sin	2 1 %	SHT	SAR	S	SmR	·Ω Σ	S	S,

≠ See Figure 25

Table 7 (Contd)

5 P-1 5 7+4 5 VM 5 VM 5 VM	The second secon	CTTMO	DESCRIFILON
5 THY 5 VM 5 VM 5 VM 5 VM 5 VM 6	1.925	Ē.	Parameter of Cornering Power Pwc
Symu Symu Symu Symu Symu Symu Symu Symu	20.00	'n	#
SVMU	84,24	ç,	#
Syal	36.74	ć,	#
Syrt	82.86	2.	+
	7,92	ŗ	Nose Tire Relaxation Length (Yaw)
TAM		d ni	Aero Pitching Moment
TAY		d! n3	Aero Yawing Moment
1)a ^[\sim	વા પા	Moment on M. G. Axle
Tse v(I		41 H	-
7,7	20,000	ظار: ط	Thrust Moment about C. G.
U.N.T.E.	.553	1	Nose Tire Friction Coefficient
	20.	1	Nose Tire Rolling Resistance
			Coefficient
		1	Nose Tire Cornering Parameter
\^^\		in / sec	Crosswind
V.	147.6	16 sec2/in	Airplane Mass
£.	1.465×106	16 sec2 in	Roll Moment of Inertia
	3.66×106	16 sectin	Pitch Moment of Inertia
WIE	4.93×10°	15 sectin	Yaw Moment of Inertia
Www	1.667	1b sect/in	M. G. Unsprung Mass
	.453	lb sec²/in	N. G. Unsprung Mass
N. C.	.723	16 sect/in	M. G. Upper Strut Mass
> ×		ć,	Horizontal Position of APL C.G.
×	36.20	۶.	X at Time = 0
·×		in/sec	Airplane Velocity in the x
			Direction
°××	2400	in/sec	
> :×		in/sec ²	Airplane Acceleration in the X
	1112		Discrion

*Point Plot Input

Table 7 (Contd)

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	in /sec	
	in / sec.	M.G. Axle Undeflected Location
	.2.	(* Direction) M.G. Axle Undeflected Velocity
· · · · · · · · · · · · · · · · · · ·		
	in / sec	M.G. Tire Footprint Location
	٠, 3	and Velocity in the α direction
	in/sec	
	ri	N.G. Tire Location (X direction)
	in /sec	N.G. Tire Velocity (X direction)
THE PERSON NAME AND ADDRESS OF	2.	M.G. Undeflected Axle Location
		$(\times \text{ Direction})$
	in / sec	M.G. Undeflected Axle Velocity
		(x Direction)
>	ţ	Horizontal C. G. Location
		(Y Direction)
0.0	2.	Y at Time = 0
>	in / sec	Airplane C.G. Velocity in
		Y Direction
0.0	in/sec	Y at Time = 0
>	in /sec2	Airplane C.G. acceleration in
		/ Direction
(o) A	u,	
γ×ν ν(0)	in sec	M.G. Undeflected Axle Location
v(0)	2.	and Velocity in the Y Direction
ý _{9x2} v(0)	in/sec	
∨	Ę	N.G. Lateral Deflection
Y. V. C.	in/sec	N.G. Lateral Delta Velocity
νης ν(Ι)	Ë	M.G. Tire Footprint Location
YMR V(I)	.5	J In the Y Direction

Table 7 (Contd)

DESCRIPTION	N.G. Lateral Location	(Y Direction)	√ at Time = 0	N.G. Lateral Velocity	Ϋ́ν at Time = 0	N.G. Lateral Acceleration	Height of Apl C.G. above ground	ref.	2 at Time = 0	Apl vertical velocity	z at Time = 0	Apl Vertical acceleration	Runway contour height	Runway contour slope	(α Direction)	Distance from Wu position to	\ Axle	^		M.G. Strut Velocity and Stroke			N. G. Stroke	N.G. Stroke Velocity	\ M. G. Axle Height) M.G. Axle Height at Time = 0) M.G. Axle Velocity	
UNITS	in		. £	in/sec	in/sec	in/sec ²	٤.		ŗ,	in /sec	in /sec	in / sec ²	, L 3	in/in	•	.5		£.	43	in/sec	£ .	in/sec	. <u>ç</u>	'n/sec	<u></u>	Ċ.	ĉ	c,	in/sec	in/sec
VALUE			0.0		0.0				82.36		0.0																20.91	20.91		
TYPE	>		υ	>	υ	>	>		ပ	>	υ	>	(I)^	v(I)		>		>	>	>	>	>	>	>	>	>	ပ	ပ	>	>
SYMBOL	>2		ν,	·>	Ý.	:> 2	, H		20	·M·	Z,	:N3	Zeo	Zaop		Zerr		ZGLR	Zsmr.	ZsmL	Sm.R.	CA SA PA	17 × × ×	ry SS	Zwmc	Zivme	F.w. M.Co	H. M. RO	1 W W 12	Ewmiz

Table 7 (Contd)

DESCRIPTION	M.G. Axle Velocity at Time = 0		M.G. Axle Vertical Acceleration		N. G. Axle Vertical Location	\mathcal{Z}_{wv} at Time = 0	N.G. Axle Vertical Velocity	$\vec{z}_{\mu\nu}$ at Time = 0	N. G. Axle Vertical Acceleration	M. G. Tire Unbalance					
UNITS	in/sec	in/sec	in / sec ²	in/sec2	٤.	<u>2</u> .	in/sec	in/sec	in/sec ²	, 4 1	ન:				
VALUE	0.0	0.0				10,02		0,0							
TYPE	υ	v	>	>	>	υ	>	U	>	v(I)	(I)^				
SYMBOL	Zwalo	Zwmro	Z. M.	74: 7w MB	141 141	Zwao	144.	Źwno	17: 3	F	Forya				

4a. WHEEL AND TIRE SYSTEM (FLYWHEEL)

Figure 33 shows the components of the wheel and tire system.

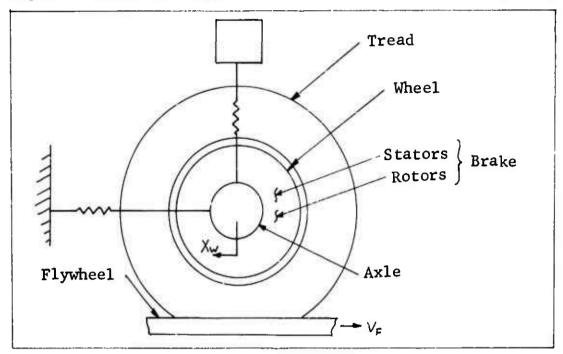


Figure 33 Components of the Wheel and Tire System

In the vertical, or Z direction, the axle, brake, wheel, tire, and lower shock strut are combined and operate as a single mass point. A description of this mode is found in the airplane system. The airplane system furnishes various inputs to the tire and wheel: V_F the airplane (flywheel surface) velocity; F_{NM} , the vertical load between the tire and pavement; S_M , the tire deflection. The brake torque T_{BT} is an input from the brake system.

The horizontal displacement of two mass points is considered. One mass point is made up of the axle, brake, wheel, and the inner part of the tire and its location is designated as $X_{\rm w}$. The other mass point is the tire tread and its location is designated as $X_{\rm rr}$.

والمارية والمحاكلات المتاريخ والمعارضة والمعار

In rotation, there are three mass points: the axle and stationary brake elements make up the first; the brake rotors, wheel, and inner tire make up the second; and the tire tread makes up the third. The angular positions of these three mass points are denoted respectively as $\Theta_{\rm S}$, $\Theta_{\rm W}$, and $\Theta_{\rm T}$. Let $F_{\rm G}$ be the horizontal force acting on the

axle and let F_{TT} be the net horizontal force between the wheel and tire tread. Figure 34 shows the location of these forces. F_{BT} is the horizontal force between the tire and the flywheel surface.

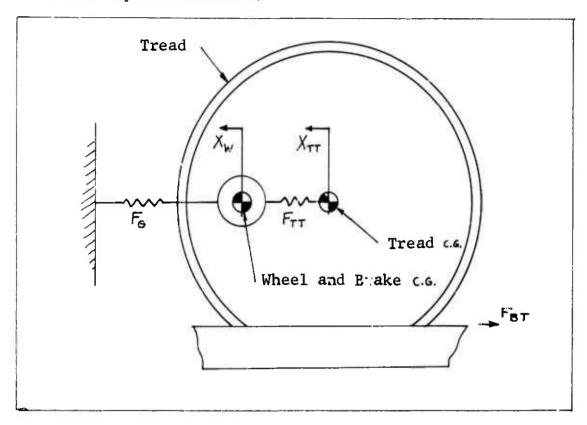


Figure 34 Tire Horizontal Model

A. Mathematical Description

Equations describing the tire and wheel behavior are developed by referring to Figure 34 . Forces F_6 and $F_{\tau\tau}$ are defined by equations (4a.1), (4a.2), and (4a.3) as follows:

(4a.1)
$$F_6 = -C_{GH} X_w - D_{GH} \dot{X}_w$$

(4a.2) $F_{TT} = C_{TT} (X_{TT} - X_w) + E_{TT} (X_{TT} - X_y)$
(4a.3) $D_{TT} (\dot{X}_v - \dot{X}_w) = E_{TT} (X_{TT} - X_y)$

Equations (4a.2) and (4a.3) describe a type 2 springdamper system as defined by Figure 38 and discussed in the parameter evaluation. Let W_{GW} denote the mass of the axle, wheel, brake and inner part of the tire. Let W_{TE} denote the appropriate tire tread mass. Summing forces in the horizontal direction gives:

$$(4a.4) W_{GW} \ddot{X}_{W} = F_{G} + F_{GT}$$

Where F_{or} is a force produced by tire unbalance, the corresponding vertical part of this unbalance force is denoted by F_{or} . These two forces are given in equations (4a.6) and (4a.7).

(4a.6)
$$F_{\Theta RH} = \hat{K}_{KO} W_T^2 sin \langle \Theta_T \rangle$$

 W_{τ} and Θ_{τ} are the rotational speed and position of the tire tread.

The rotational schematic of the wheel and tire system is shown in Figure 35 .

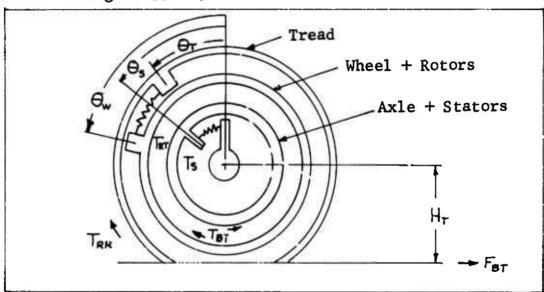


Figure 35 Tire Rotational Model

Let T_{RT} and T_{S} be defined by equations (4a.8), (4a.9), and (4a.10) as follows:

(4a.8)
$$T_{RT} = C_{RT}(\Theta_W - \Theta_T) + E_{RT}(\Theta_W - \Theta_Y)$$

(4a.9)
$$D_{RT}(\dot{\theta}_{V} - \dot{\theta}_{T}) = E_{RT}(\theta_{W} - \theta_{V})$$

(4a.10)
$$T_S = C_{RS} \theta_S + D_{RS} \dot{\theta}_S$$

Let H_T be the height of the axle above the ground. Let T_{RR} be the torque on the tire that produces rolling resistance. These two quantities are given by:

$$(4a.11) H_T = R_{eT} - S_M$$

$$(4a.12) T_{RR} = \begin{cases} S_M (D_{SR} + D_{VR} W_T) & \text{if } W_T > 0 \\ 0 & \text{if } W_T = 0 \\ S_M (-D_{SR} + D_{VR} W_T) & \text{if } W_T < 0 \end{cases}$$

If T_{GT} is the brake torque, then torques can be summed to obtain the following three equations:

(4a.13)
$$W_{IS}\ddot{\Theta}_{S} = T_{BT} - T_{S}$$

(4a.14) $W_{IW}\ddot{\Theta}_{W} = -T_{ET} - T_{BT}$
(4a.15) $W_{IT}\ddot{\Theta}_{T} = H_{T}F_{BT} + T_{RT} - T_{RR}$

The rolling radius of the tire is obtained using the methods of Reference 1. Denoting the rolling radius as R_{τ} , it is defined as:

(4a.16)
$$R_T = R_{OT} - \frac{1}{3} S_M - U_{RR} (X_{TT} - X_W)$$

Let V_{RS} denote the velocity of the tire footprint. Relative to the flywheel surface with $W_{T} = 0$, let V_{R} be the relative velocity including W_{T} .

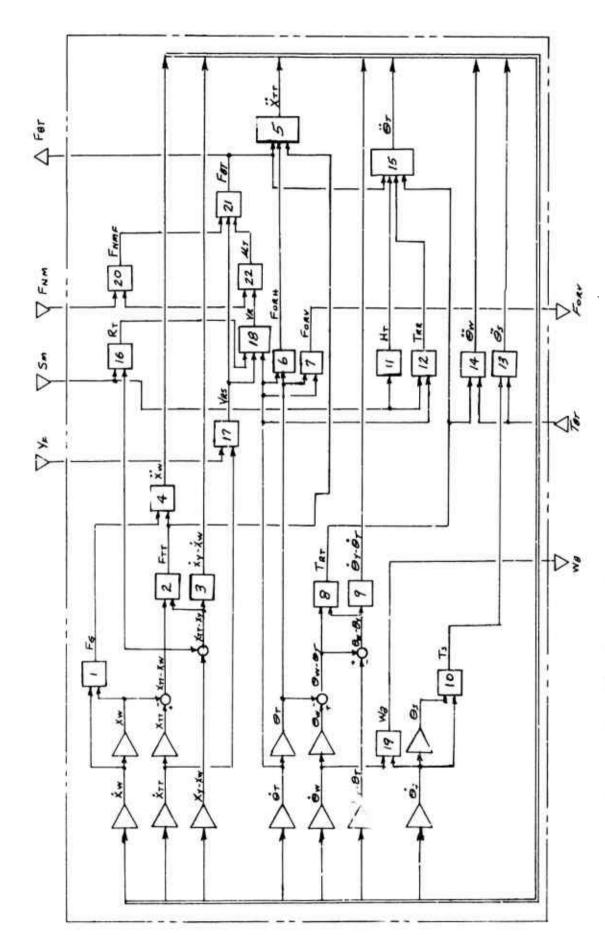
(4a.17)
$$V_{RS} = V_F + \dot{X}_{TT}$$

(4a.18) $V_R = V_{RS} - R_T W_T$

Here V_F is the velocity of the flywheel surface. Adopting the convention, $W_T = \dot{\Theta}_T$; $W_S = \dot{\Theta}_S$; and $W_W = \dot{\Theta}_W$, the relative angular velocity between the stators and rotors is denoted by W_B and is established by:

$$(4a.19) W_B = W_W - W_S$$

When a tire is moving over a runway with any appreciable amount of standing water or slush, a hydrodynamic "wedge"



Wheel and Tire System (Flywheel) Equation Flow Diagram Figure 36

of water starts separating the tread and runway surface. It is assumed that the length of this "wedge" is proportional to V_{RS}^2 and at hydroplaning speed, V_{HY} , the tread is completely separated from the runway. In equations (4a.20) and (4a.20) the coefficients C_{HY} and D_{HY} are used to define hydroplaning effects and water drag on the wheel. For dry runway conditions, C_{HY} and D_{HY} are zero. The horizontal force between the tire tread footprint and the runway surface is established by equations (4a.20), (4a.21), and (4a.22) as follows:

(4a.20)
$$F_{NMF} = F_{NM} (1 - C_{HY} (V_{RS} / V_{HY})^2)$$

(4a.21) $F_{BT} = F_{NMF} U_{\Gamma} + D_{HY} V_{RS}^2$
(4a.22) $U_{T} = U_{T_1} + (U_{T_2} - E_{T} V_{RS}) e^{-\alpha V_{R}}$ if $V_{R} > 0$
 $U_{T_1} - (U_{T_2} - E_{T} V_{RS}) e^{-\alpha V_{R}}$ if $V_{R} < 0$

Figure 36 is an equation flow diagram showing the relation between equations (4a.1) through (4a.22).

B. Parameter Evaluation

Gear Characteristics

The mass W_{GW} is made up of the mass of half the shock strut, half the lateral beam, the axle, the wheel, the brakes, and all but one-third of the tire tread. The sum of the masses of these components totals 616 LBM. Thus, $W_{GW} = \frac{616}{386} = 1.60$ Hb $_{Sec}^2/_{in}$. The fore and aft natural frequency of the gear (as calculated from deflection data) is $21.84\,\mathrm{cps} = \frac{137.5\,\mathrm{rad/sec}}{137.5\,\mathrm{rad/sec}}$. Using the gear mass, with all of the tire included (644 LBM), the spring rate C_{GH} can be calculated as:

$$(4a.23)$$
 $C_{GH} = m\omega_n^2 = \left(\frac{644}{386}\right)^2 = 31,500 \text{ lb/in}$

A typical approach to estimate the damping coefficient is to use 3% critical. Thus,

(4a.24)
$$D_{GH} = (.03) 2 \sqrt{mC_G} = (.06) \sqrt{\left(\frac{.44}{386}\right) 31500} = 13.8 \frac{16}{10}$$

Tire Tread Characteristics

The principle underlying the calculation of the tire friction coefficient is that compared to the rest of the tire, the tire "footprint" is totally inelastic. (The tire "footprint" is that portion of the tire tread which is in contact with the ground). Thus, if the valuatity of the footprint and the friction vs. velocity curve for the rubbersurface interface are defined, the tire friction coefficient is established. In order to predict the motion of the footprint, the tire tread is assumed to behave like an inelastic ring which is supported on the wheel as shown in Figure 37.

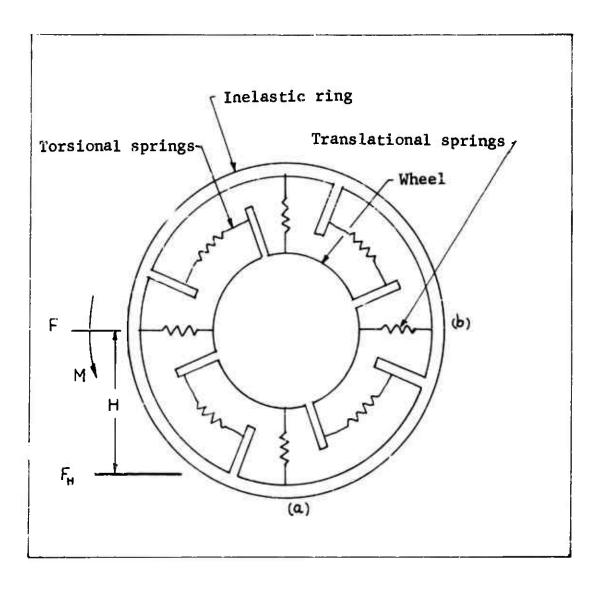


Figure 37 Tire Tread Model

The horizontal position of the footprint is assumed to be the same as the horizontal position of the ring center of gravity. A frictional force F_H applied at the ground can be resolved into a translational force $F = F_H$ acting at the ring C.G., plus a moment $M = F_H \cdot H$ acting about the ring C.G.

For an actual tire with distributed mass and elasticity approximately one-third of the tire would move with the foot-print in response to force, $F_{\rm H}$. Therefore, it is assumed for translation the mass of the ring, $W_{\rm TE}$, is one-third of the tire tread mass, which is 84 LBM. Thus, $W_{\rm TE} = (84)/(3 \times 386) = 0.0725$ LBF SEC²/IN.

For rotation the total tire tread mass is assumed to move in response to moment, M. Thus, the moment of inertia about its center of gravity is $W_{IT} = MR^2 = (84/386) (23^2) = 115 \text{ LBF SEC}^2/\text{IN}$.

References 1 (page 22) and 10 (Figure 8) are used to obtain values for the torsional and translational spring rates as shown in Figure 37. Under the application of the force F_{μ} , the peripheral movement at point b is about 20% of the peripheral movement at point a (Figure 37 above). The expression for the footprint spring rate from Reference 1 is:

$$(4a.25) K_x = .6d (P+4Pr) \sqrt[3]{So/d}$$

Where for the F-111 with a vertical tire load of 25,000 lb,

d = 46.65 in. = Tire diameter

P = 150 psi = Tire operating pressure

Pr = 150 psi - Tire rated pressure

So = 2.75 in. = Operating (static) deflection

Thus,

の重要などの対抗な関係の対抗が必要をおおけば自己のできたがあるがある。

$$(4a.26) K_x = (.6)(46.65)(5)(150) \sqrt[3]{2.75/46.65} = 8150 lb/in$$

The application of F_H = 8150 lb. causes the footprint to move one inch. At point b, the movement is .2 inches. Assuming that the movement at point b is all due to rotation, the apparent torsional spring rate is:

(4a.27)
$$C_{RT} = \left(\frac{d}{2}\right) \frac{H}{(.2)} = \frac{(23.32)(20.57)(8150)}{(.2)} = 19.5 \text{ m/bF/red}$$

Since .8 inches of the 1.0 inch footprint motion is due to tread C.G. fore and aft translation, the apparent spring rate is:

$$(4a.28)$$
 $C_{TT} = \frac{F_H}{8} = \frac{8150}{8} = 10,200 \text{ lb/in}$

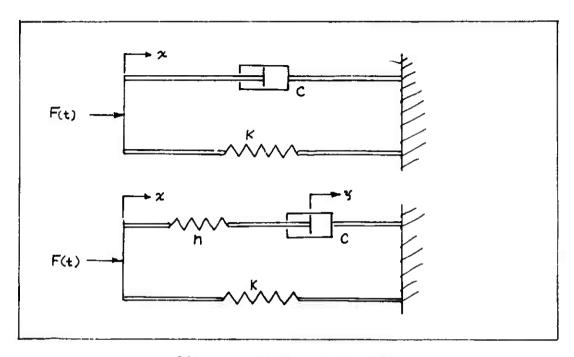


Figure 38 Tire Damping Models

It is well publicized and generally accepted that the elastic and damping characteristics of tires and other structural devices are not accurately described by the mathematically convenient linear spring-viscous damper representation over a wide frequency range. The behavior of rubber-like materials is particularly different than that described by the conventional model. To establish suitable mathematical descriptions of the various damping forces for tires and other elements of this study, several models were explored. Figure 38 depicts the two types of elastic systems which are used. The Type 1 model is a conventional system with viscous damping and Type 2 is a visco-elastic system, having elasticity and damping which varies with frequency. To compare the two, consider the effects of driving each with a variable force F(t) = Fo coe wt . In each case, the resultant deflection is $x = x_0 \cos(\omega t - \varphi)$

The loss coefficient, β , is defined by $\beta = \cos \varphi$. For a conventional system (Type 1 with ϵ and k constant), the loss coefficient which is a measure of the damping is

given by:

$$(4a.29) \beta = c\omega/k$$

Reference 1 assumes that c is of the form $c = \eta k/\omega$ where η and k are constant. From this:

$$(4a.30) \beta = \gamma$$

Reference 8 seems to indicate (p. 55) that the loss coefficient for tire tread rubber is somewhere between the above two values.

For the Type 2 system, shown in Figure 38, with c, n, and k constant, the loss coefficient is given by:

$$(4a.31) \beta = \left(\frac{c\omega}{k}\right) / \left(1 + \left(\frac{c\omega}{n}\right)^{2} \left(1 + \frac{n}{k}\right)\right)$$

To represent a tire, the values $(c/k) = 1.56 \times 10^{-3}$ sec. and (n/k) = 0.520, were used to compute values of β for a range of frequencies. β versus ω is shown in Figure 39 for both Type 1 and Type 2 models, along with values of β taken from References 1 and 8. The value from Reference 1 is shown constant at all frequencies because the value is not identified with any frequency. The above values of (c/k) and (n/k) were chosen because they gave β values in best agreement with authoritative data.

Figure 39 shows both Type 1 and Type 2 models have relatively poor correlation with both data sources. Reference 8 indicates β is highly dependent upon temperature and tire rubber compound as might be expected. During damping model exploration, both Type 1 and Type 2 systems were examined dynamically on an analog computer. It was found that differences in their behavior were observable; however, since the damping forces are relatively small compared to the other forces, this difference was small. Either model is equally satisfactory for evaluating anti-skid operation. The Type 2 system is used for the tire because it is in closer agreement with recorded observations. The peak in the β versus frequency curve for the Type 2 system is in keeping with most of the contour plots for rubber-like materials as shown in Reference 7 and 8.

The tire elastic and damping coefficients are:

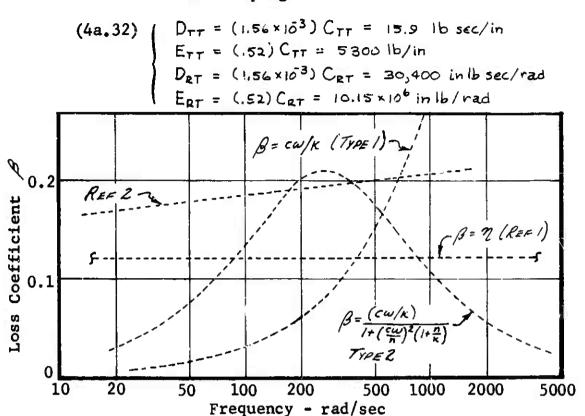


Figure 39 Model Loss Factors

The equation (4a.16) for the rolling radius R_T is a restatement of equation (76 b) of Reference 1. To allow for circumferential decay length other than those equal to the outside free tire radius, a coefficient U_{RR} is provided. For this study U_{RR} is set equal to 1.0.

Axle Parameters

The observed torsional natural frequency of the axle (with brake stators) is 125 cps. The calculated value for its moment of inertia is 16.8 LBF SEC 2 /IN. Thus, the torsional spring rate, C_{RS} , is established as:

$$(4a.33)$$
 $C_{RS} = (2\pi 125)^2 (16.8) = 10.4 \times 10^6$ in lb/rad

For the steel axle, a value for η (in the Type 1 system in Figure 38) is probably something less than .01 (Reference 7). Thus, at resonance, if $c\omega/k = \eta$, then the damping coefficient is established as:

Tire Rolling Resistance

From Figure 17a of Reference 2, the rolling resistance coefficient, μ_r is given by $\mu_r = .012 + 1 \times 10^{-5} \text{v}$ where v is the axle speed in INCHES/SEC. Thus,

Or alternately, =
$$(.012 + 1 \times 10^{5} \dot{\Theta}_{\Gamma} R_{T}) (F_{gg}/\S)(\S) R_{T}$$

Since $F_{RR}/\delta = C_{MT}$, the rolling resistance coefficients are established as:

(4a.36)
$$D_{SR} = .012 C_{MT} R_T = (.012)(9530)(20.57) = 23501b$$

Figure 40 shows the friction coefficient for a tire sliding (i.e. full skid) on a dry concrete runway as a function of velocity. This data is taken from Reference 3 and is applicable to a typical runway contaminated with rubber deposits from previous airplane operations. Table 8 below lists the appropriate coefficients for equation (4a.22) which apply for dry and wet runway surface conditions.

WET DRY SYMBOL UNITS CONCRETE CONCRETE .050 .200 u_{r_1} .180 .450 U_{T2} SEC/IN $.065 \times 10$ $.065 \times 10$ Eт SEC/IN 1.0×10 2.5×10

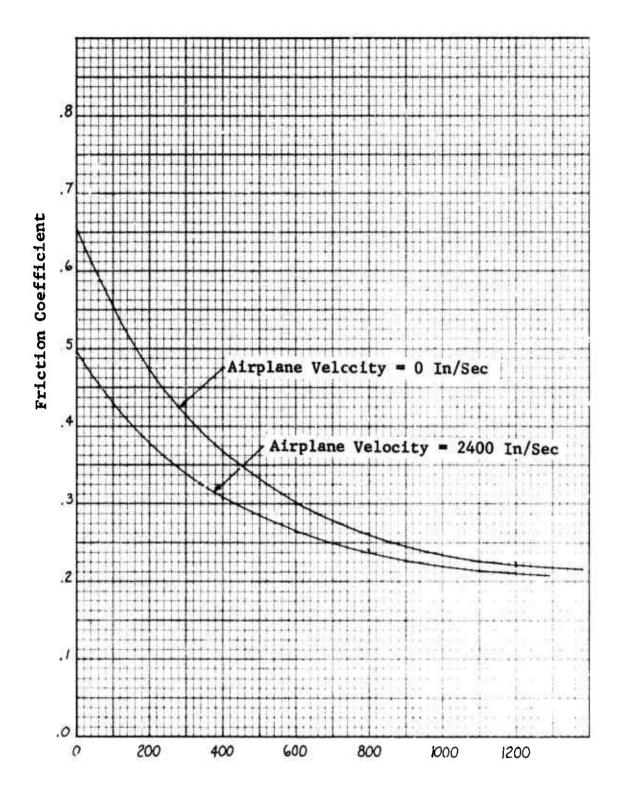
Table 8 Runway Friction Characteristics

Initial Conditions

All initial conditions, except wheel and tire rotational speed, will be set to zero. From the airplane system at time = 0, V_F = 2400 and S_M = 2.245. Using equation (4a.16) results in:

(4a.38)
$$R_T = R_{0T} - \frac{1}{3}S_M = 23.32 - \frac{1}{3}(2.245) = 22.67 in$$

In order that V_R be zero, equations (4a.18) and (4a.19) show that:



Tire Footprint Valocity (in/sec)

Figure 40 Tire Sliding Friction Coefficient

(4a.39) $\dot{\Theta}_{TO} = \dot{\Theta}_{WO} = V_F/R_T = 2400/22.67 = 105.9 \text{ rad/sec}$

Table 9 Wheel and Tire System (Flywheel) Parameters

DESCRIPTION	Tire Friction Parameter	Fore and Aft Spring Rate at Axle	Axle Rotational Spring Rate	Tire to Wheel Rotational Spring	Rate	Controls Hydroplaning Influence	Tread to Wheel Spring Rate	Fore and Aft Damping Coefficient	at Axle	Water Resistance Coefficient	Gear to Axle Rotational Damping	Coefficient	Tire to Wheel Rotational Damping	Coefficient	Rolling Resistance Parameter	Tread to Wheel Damping Coefficient	Rolling Resistance Parameter	Tire to wheel Coupling Spring Rate	Tire Friction Correction Coeff.	Tread to Wheel Coupling Spring Rate	Horizontal Force on Tire Foot-	print from Ground	Horizontal Force at Axle	Horizontal Wheel Unbalance Force	Vertical Wheel Unbalance Force	Vertical Force between Time and	Ground	Vertical Force not Supported by	water Film
UNITS	sec/in	16/in	in 16/rad	in lb/rad		1	1b/in	1b sec/in		1b sec/in	in 16 sec/rad		in 16 sec/rad		ৰ	16 sectin	16 sec/rad	in 16/rad	Sec/im	lb/in	٩		91	વા	م!	<u>ء</u>	•	9/	
VALUE	2.5 × 10-3	3/500	10.4 × 106	19,5 × 10 ⁴		0.0	10,200	13.8		0,0	0.261		30,400		2350	15,9	40.3	10.15 × 10	.65×10+	2300									
TYPE	υ	υ	U	ပ		U	U	υ		v	U		U		Ų	ပ	U	υ	ပ	ပ	(o) n	-	>	>	(o) ^	v(I)		>	
SYMBOL	8	Cer	Crs	CRT	(CH.	CTT	Den	-	ر ت	DRS	1	Der	(Dsr	Drr	DvR	FRT	Ē	ETT	FBT	ı	Fo	Гови	FORV	7. 2x.		r R	

Table 9 (Contd)

DESCRIPTION	Net Force Between Tread & Wheel	Axle Height Above Ground (Hr & Rgr)	Axle Rotation	Axle Rotation at Time = 0	Axle Rotational Speed	Axle Rotational Speed at Time = 0	Axle Rotational Acceleration	Tire Tread Rotation	Tire Tread Rotation at Time = 0	Tire Tread Rotational Speed	Tire Tread Rotational Speed at	Time = 0	Tire Tread Rotational Accelera-	tion	Wheel Rotation	Wheel Rotation at Time = 0	Wheel Rotational Speed	Wheel Rotational Speed at	Time = 0	Wheel Rotational Acceleration	Dummy Variables used to	Simulate Visco-elastic Tire) Characteristic	Unbalance Coefficient	Undeflected Tire Radius	Tire Rolling Radius	Tire Deflection	Brake Torque
UNITS	9]	Ē	rad	rad	rad/sec	rad/sec	rad/sec ²	per	7.20	rad/sec	rad/sec		rad/sec ²		rad	١٩٦	rad/sec	r2d/ sec		rad/sec²	rad	العن	rad/sec	16 sec2/rad2	2.	<u>2</u> .	. <u>r</u>	di ni
VALUE				0.0		00			0.0		105.9					0.0		105.9				0.0		0,0	23,32			
TYPE	>	>	>	U	>	υ	>	>	υ	>	υ		>		>	υ	>	υ		>	>	υ	>	U	ပ	>	(I)^	(I)^
SYMBOL	LL.	İ	θs	980	\$ 0	o. So	. SO	9+	Θ _{To}	· @·	Θ̄το	;	Θ _τ		0	9~0	3	φ×ο	•	3	Φ,	Θχο	φ́	Rko	Rot	RT	S	TBT

Table 9 (Contd)

SVMBOT	ТУРЕ	VATITE	PLINIT	DECOPTON
				אסידו דיינט טינט
Trr	>		ol ri	Torque Producing Rolling Resist-
TRT	>		91 m	Torque between Tire (Tread) and
				Wheel
- ا	>		ن. الأ	Axle Torque
LRE	υ	0.7	1	Rolling Radius Parameter
μ	>		1	Tire Friction Coefficient
UTI	υ	.20	1	Tire Friction Parameters
Ur2	υ	.45	,	
\ F	(I)^		in/sec	Flywheel Surface Velocity
/н^	υ	2400	in/sec	Tire Hydroplaning Speed
/R	>		in/sec	Velocity of Tire Footprint
				Relative to Flywheel
. es	>		in/sec	Same as VR except Rotational
				Effects Ignored
₩B	(0)^		rad/sec	Relative Rotational Speed Be-
				tween Stators and Rotors
Wew	υ	1.60	!b sec2/in	Effective Tire, Wheel, and
				Brake Mass
×1×	υ	6.8	in lb sectrad	Axle Moment of Inertia (+ Stators)
Wat	υ	0.511	in 16 sect/rad	Tread Moment of Inertia
WIW	υ	0.99	in 16 sect/rad	Wheel & Rotors Moment of Inertia
Ws	>		rad/sec	Ws = Os
1	>		rad/sec	Wr = Or
Wre	υ	.0725	1b sectin	Equivalent Tire Tread Mass
×××	>		rad/sec	Ww = Ow
X	>		. ĉ	Tread
XTTO	U	0.0	č	
				at Time = 0
	1			

Table 9 (Contd)

DESCRIPTION	Tread C.G. Velocity	Tread C.G. Velocity at Time = 0	Tread C.G. Acceleration	Horizontal Axle Location	Horizontal Axle Location at	Time = 0	Horizontal Axle Velocity	Horizontal Axle Velocity at	Time = 0	Horizontal Axle Acceleration	Dummy Variables Used to	Simulate Visco-elastic Tire) Characteristic	
UNITS	in/sec	in/sec	in/sect	2.	ē		in/sec	10/500		1n/sec ²		5	in/sec	
VALUE		0.0			0.0			0.0				0.0		
TYPE	>	O	>	>	O		>	υ		>	>	υ	>	
SYMBOL	Ϋ́ττ	Xrro	Li.X	3 ×	× ×		·×	°3××		3 ×	××	X	××	

4b. WHEEL AND TIRE SYSTEM (3 DEGREE)

Figure 41 shows the components of the wheel and tire system. The wheel and tire system

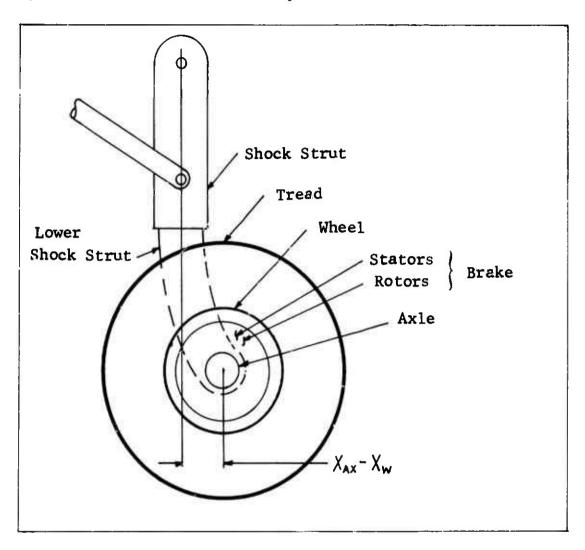


Figure 41 Components of the Wheel and Tire System

for the 3 degree airplane system is essentially the same as for the flywheel model. The Airplane System still furnishes the tire deflection $S_{\mathbf{M}}$ and the tire vertical load $F_{\mathbf{NM}}$. The ground speed, however, is no longer furnished by the Airplane System, but is found by summing forces on the tire, wheel, brake, and axle mass. The horizontal force exerted on the axle by the airplane is calculated by obtaining the translational $(X_{\mathbf{AX}})$ and rotational $(\theta_{\mathbf{G}})$ gear positions from the Airplane System.

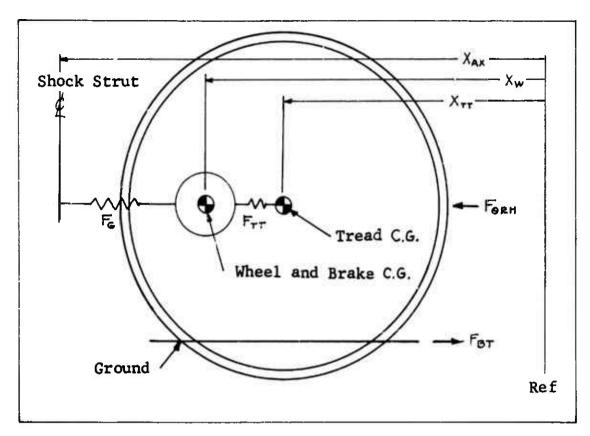


Figure 42 Tire Horizontal Model

Referring to Figure 42 equation (4a.1) in the flywheel system changes to

$$(4b.1) F_G = C_G (X_{Ax} - X_w) + D_G (\dot{X}_{Ax} - \dot{X}_w)$$

Equations (4b.2) through (4b.9) are listed for completeness, although they are the same as (4a.2) through (4a.9).

(4b.2)
$$F_{TT} = C_{TT}(X_{TT} - X_w) + E_{TT}(X_{TT} - X_y)$$

$$(4b.3) D_{TT} (\dot{X}_{y} - \dot{X}_{w}) = E_{TT} (X_{TT} - X_{y})$$

Figure 43 shows the rotational model of the wheel, tire, axle, and lower strut with the gear rotation Θ_G added. Including the effect of Θ_G there follows:

$$(4b.8) T_{RT} = C_{RT} (\Theta_{W} - \Theta_{T}) + E_{RT} (\Theta_{W} - \Theta_{y})$$

$$(4b.9) D_{RT} (\dot{\Theta}_{y} - \dot{\Theta}_{T}) = E_{RT} (\Theta_{W} - \Theta_{y})$$

$$(4b.10) T_S = C_{RS} (\theta_S - \theta_G) + D_{RS} (\dot{\theta}_S - \dot{\theta}_G)$$

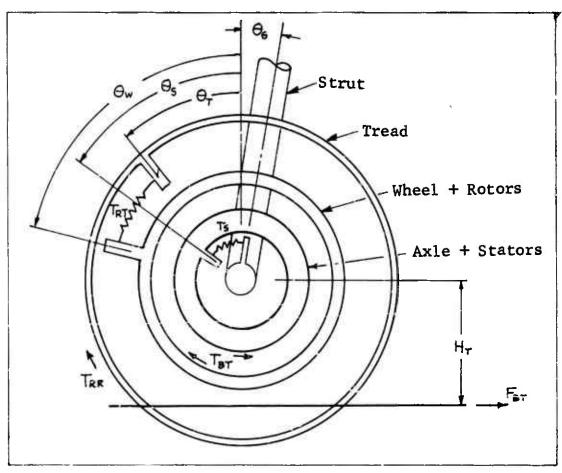


Figure 43 Tire Rotational Model

Equations (4b.11) through (4b.16) are the same as (4a.11) through (4a.16).

(4b.11)
$$H_T = R_{eT} - S_M$$

(4b.12) $T_{RR} = \begin{cases} S_M (D_{SR} + D_{VR} W_T) & \text{if } W_T > 0 \\ C & \text{if } W_T = 0 \\ S_M (-D_{SR} + D_{VR} W_T) & \text{if } W_T < 0 \end{cases}$

$$(4b.13) W_{IS} \ddot{\Theta}_{S} = T_{BT} - T_{S}$$

$$(4b.14) W_{IW} \ddot{\Theta}_{W} = -T_{RT} - T_{BT}$$

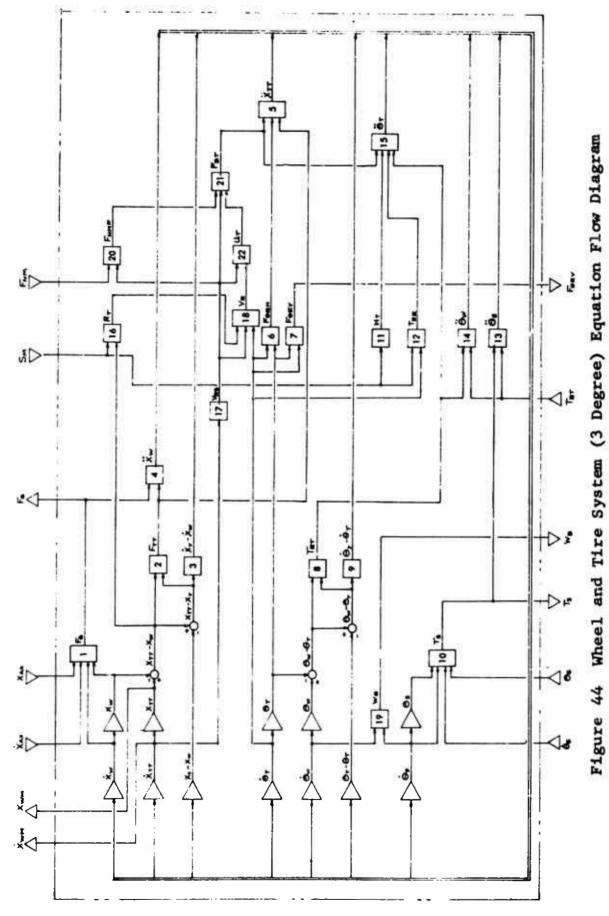
$$(4b.15) W_{IT} \ddot{\Theta}_{T} = H_{T} F_{ST} + T_{RT} - T_{RR}$$

$$(4b.16) R_{T} = R_{BT} - \frac{1}{3} S_{M} - U_{RR} (X_{TT} - X_{W})$$

Because the ground is now stationary equation (4a.17) becomes

The remaining equations are unchanged except for noting that the outputs X_{wm} and \dot{X}_{wm} required for the Airplane System are obtained by renaming X_{TT} . Thus $X_{wm} = X_{TT}$ and $\dot{X}_{wm} = \dot{X}_{TT}$. Continuing,

$$(4b.19) W_{B} = W_{W} - W_{S}$$



B. Parameter Evaluation

The parameter values for this system are essentially the same as for the wheel and tire system that corresponds to the flywheel system. One difference is the values for C_6 and D_6 which are derived in the Airplane System (3 degree). These values are

(4b.23)
$$C_G = 200,000 \text{ lb/in}$$

 $D_G = 78.6 \text{ lb sec/in}$

Since this system moves with the airplane the initial conditions should match the Airplane model. Thus

(4b.24)
$$\begin{cases} X_{TTO} = 0.0 & \text{in} \\ X_{TTD} = 2400 & \text{in/sec} \end{cases}$$

(4b.25)
$$\begin{cases} X_{wo} = 0.0 & \text{in} \\ \hat{X}_{wo} = 2400 & \text{in/sec} \end{cases}$$

From equation (4b.16)

$$(45.26)$$
 $R_T = R_{eT} - \frac{1}{3}S_M = 23.32 - 80 = 22.52$ IN

Thus for a "spun up" tire, we have from equation (18)

$$(4b.27)$$
 Wr = V_{RS}/R_T = 2400/22,52 = 106.7 rad/sec

Then

(4b.28)
$$\Theta_{TO} = \Theta_{WO} = 106.7 \, \text{rad/sec}$$

Also from equation (10), choose Θ_{50}

Horizontal Force on Tire Footprint from Ground Vertical Force Not Supported by Water Film Tire to Wheel Rotational Damping Coeff. Gear To Axle Rotational Damping Coeff. Force Between Tire and Ground Tire to Wheel Rotational Spring Rate Tread to Wheel Spring Rate Fore and Aft Damping Coeff. at Axle Tread to Wheel Coupling Spring Rate Tire to Wheel Coupling Spring Rate Net Force Between Tread and Wheel Controls Hydroplanning Influence Horizontal Wheel Unbalance Force Fire Friction Correction Coeff. Wheel and Tire System (3 Degree) Parameters Vertical Wheel Unbalance Force Tread to Wheel Damping Coeff. Rolling Resistance Parameter Rolling Resistance Parameter Fore and Aft Spring Rate at Axle Rotational Spring Rate Horizontal Force at Axle Tire Friction Parameter Water Resistance Coeff. DESCRIPTION Jertical n 16 sec/rad in 16 sec/rad b sec/rad bsect/in2 in 16/rad it sec/in b sectin in 16/ rad n 1b/rad sec/in sec/in u) / وا UNITS un / 91 n / 91 9 -9 2.5×103 10,15×106 65×104 Table 10 2.CA103 15.5×104 0,4×10° 30,400 002'OI 2350 ANTVA 0,0 5230 40.3 5,9 78.6 0,0 32 (0) ^ (O) A TYPE SYMBOL FORH PNMF TO BEV ٤ ک FBT DHY DVR ERT CIT - 25 Dry と 7. DRS Det Dsz الم <u>ا</u>

Table 10 (Contd)

	<pre>11 = Part </pre>
NOILLION	Axle Rotation Axle Rotation at Time = 0 Axle Rotational Speed at Time = 0 Axle Rotational Speed at Time = 0 Axle Rotational Speed at Time = 0 Axle Rotational Acceleration Tire Tread Rotation Tire Tread Rotational Speed Tire Tread Rotational Acceleration Wheel Rotational Speed Wheel Rotational Acceleration Chael Rotational Acceleration Simulate Visco-Elestic Tire Simulate Visco-Elestic Tire Characteristic. Unbalance Joeff. Undeflected Tire Radius Tire Rolling Radius Tire Deflection
UNITS	rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec rad/sec
VALUE	.0329 0.0 0.0 0.0 0.0 0.0 23.32
TYPE	
SYMBOL	I Q Q Q Q Q Q Q Q Q Q Q Q Q Q Q Q Q Q Q

Table 10 (Contd)

SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
}	(5)			Broke Craise
-81	(1)		9	דומטע וסילתר
TRE	>		<u>وا</u> د.	Torque Producing Kolling Resistance
TRT	>		9 4:	Torque Between Tire (Tread) and Wheel
ر ا	(0)^		ط ا ا	Axle Torque
ų,	U	0,	1	Rolling Radius Parameter
עד	>		1	Tire Friction Coefficient
u _T ,	O	02.	1	Tire Friction Parameters
UTZ	U	. 45	1	
×H.Y	ပ	2400	in/sec	Tire Hydroplanning Speed
\ \	>		in/sec	Velocity of Tire Footprint Relative to Flywheel
\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	>		in / sec	Same as We except Rotational Effects Ignored
3	(0) ^		rad/sec	Relating Rotational Speed Between Stators & Rotors
Wer	()	9:	16 sec2/in	Effective Tire, Wheel, & Brake Mass
MIS	υ	16.8	in 1b sec2/rad	Axle Moment of Inertia (+ Stators)
WTT	U	115.0	in 10 sec2/rad	Tread Moment of Inertia
WIM	U	66.0	in 16 sec2/rad	Wheel and Rotors Moment of Inertia
×8	>		rad/sec	Ws = @s
^	>		rad/sec	Wr = Gr
WTE	O	.0725	16 sectin	Equivalent Tire Tread Mass
: 3	>		rad/sec	Ww = 0w
× + 1	>		2.	Location of Tire Tread C.G.
XTTO	၁	0,0	, c,	Location of Tire Tread C.G. at Time = 0

Table 10 (Contd)

	1			
SYMBOL	TYPE	VALUE	CNITS	JESCRIPTION
×	۲		in/sec	Tread 3.G. Velocity
×	0	2400	in/sec	Tread C.G. Velocity at Time = 0
X	>		in/sec 2	Tread 0.6. Acceleration
* ×	>		. 5	Horizontal Axle Location
3 X	Ç	0.0	.5.	Horizontal Axle Location at Time = 0
3	>		IN /SPC	Horizontal Axle Velocity
××	O	2400	in/sec	Horizontal Axle Velocity at Time = 0
3 :×	ز		In / Sec	Horizontal Axle Acceleration
× ×	>		. 47) Dummay Variables Used to
0 X	O	0.0	.41	Simulate Visco-Elastic Tire
•×	>		in / sec	J Characteristic.
90	v(i)		Cad	Gear Rotation
$\Theta_{\boldsymbol{\varsigma}}$	v(i)		rad/sec	Gear Rotational Velocity
X	v(i)		'n	Undeflected Axle Position
. < . ×	v(1)		in /sec	Undeflected Axle Velocity
X	(0)^		.2.	Footprint Location (x Direction)
₹ •×	(0) ^		in /sec	Footprint Velocity (x Direction)
	_			

4c. TIRE AND WHEEL SYSTEM (6 DEGREE)

The wheel and tire system for the six degree problem is the same as that described in the three degree system except for inclusion of the lateral mode. Equations (4c.1) through (4c.17) are the same as (4b.1) through (4b.17) in the three degree system.

A. Mathematical Description

(4c.1)
$$F_6 = C_6 (X_{Ax} - X_w) + D_6 (\dot{X}_{Ax} - \dot{X}_w)$$

(4c.2)
$$F_{TT} = C_{TT}(X_{TT} - X_w) + E_{TT}(X_{TT} - X_y)$$

(4c.3)
$$D_{\tau\tau}(\dot{X}_{y} - \dot{X}_{w}) = E_{\tau\tau}(X_{\tau\tau} - X_{y})$$

(4c.8)
$$T_{RT} = C_{RT}(\Theta_W - \Theta_T) + E_{RT}(\Theta_W - \Theta_Y)$$

(4c.9)
$$D_{RT}(\dot{\Theta}_{y} - \dot{\Theta}_{f}) = E_{RT}(\Theta_{w} - \Theta_{y})$$

(4c.10)
$$T_s = C_{RS}(\Theta_S - \Theta_G) + D_{RS}(\dot{\Theta}_S - \dot{\Theta}_G)$$

(4c.12)
$$T_{RR} = \begin{cases} S_{M} (D_{SR} + D_{VR} W_{T}) & \text{if } W_{T} > 0 \\ 0 & \text{if } W_{T} = 0 \\ S_{M} (-D_{SR} + D_{VR} W_{T}) & \text{if } W_{T} < 0 \end{cases}$$

(4c.13)
$$W_{IS}\ddot{\Theta}_{S} \approx T_{BT} - T_{S}$$

$$(4c.14) W_{IW} \ddot{\Theta}_{W} = -T_{RT} - T_{gr}$$

(4c.17)
$$V_{RS} = \dot{X}_{TT} = \dot{X}_{WM}$$
 also $X_{WM} = X_{TT}$

Equation (4b.18) which gives the relative velocity between the footprint and the ground is changed to account for the lateral footprint velocity \dot{Y}_{M} .

(4c.18)
$$V_R = \sqrt{V_{RX}^2 + \dot{Y}_M^2}$$

Equations (4b.19) and (4b.20) are unchanged.

$$(4c.19)$$
 $W_B = W_W - W_S$

(4c.20)
$$F_{NMF} = F_{NM} (1 - C_{HY} (V_{RS} / V_{HY})^2)$$

Now \forall_{RX} is the relative velocity in the x direction so

$$(4c.21) \quad V_{ex} = V_{es} - R_T W_T$$

Thus, the angle \mathcal{C}_T which defines the friction force direction as shown in figure 45is given by

(4c.22)
$$\beta_T = tari\langle \dot{y}_M / V_{RX} \rangle$$

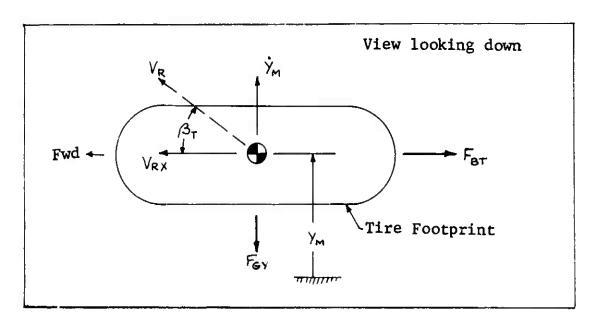
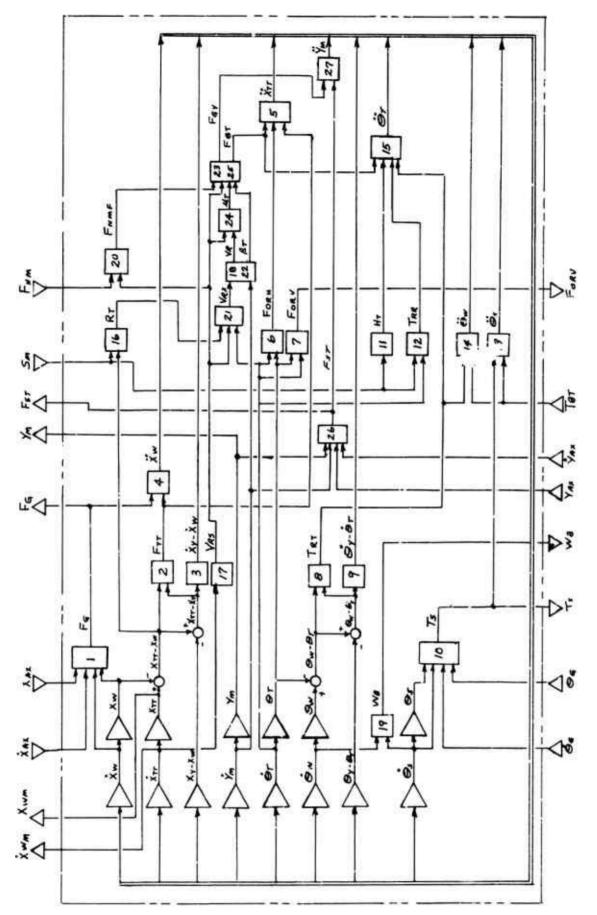


Figure 45 Footprint Friction Components



Wheel and Tire System (6 Degree) Equation Flow Diagram Figure 46

Thus, F_{BT} is now given by

and

$$(4c.24) U_T = \begin{cases} U_{T1} + (U_{T2} - E_T V_{RS}) e^{-\alpha V_R} & \text{if } V_R > c \\ 0 & \text{if } V_R \le 0 \end{cases}$$

The lateral friction force For is given by

The airplane product a lateral position Y_{AX} of the axle. If Y_{M} is the lateral ocation of the footprint, then a lateral force F_{ST} is produced and

$$(4c.26) F_{ST} = C_{ST} (Y_{AX} - Y_{M}) + D_{ST} (\mathring{Y}_{AX} - \mathring{Y}_{M})$$

Finally, forces can be summed laterally on the footprint to obtain

B. Parameter Evaluation

Wheel and Tire System Parameters

Most of the parameter values were derived in the wheel and tire system that was used with the flywheel. The only addition is the evaluation of $C_{\rm ST}$ and $D_{\rm ST}$

From reference 1 (p.15)

Assuming that $\delta_0 = 2.245$ in., then

$$(4c.29) C_{st} = (2)(18)(1.24)(150)(1-.7(2.245/18))$$

Using
$$\omega_n = \sqrt{K/m} = \sqrt{6460/.0725} = 298.4$$

Using $\eta = .1$ (from page 50 of kef. 1) results in

Initial Conditions

The only difference between this and the three degree system is evaluating Y_{MO} and \dot{Y}_{MO} . It should be that $Y_{MO} = Y_{AX}(\circ)$ Since this system is used for both right and left sides, then Y_{MO} will differ. Assume that this system is used as the right wheel and tire. Then, $Y_{MO} = Y_{AXR}$ as in equation (4c.56). From this equation at Time = 0, (since R = P = 0), then

$$(4c.32) Y_{MO} = Y_{AXR} = Y_0 + S_{GW} = 0 + 60 = 60 in$$

Similarly

Wheel and Tire System (6 Degree) Parameters Table 11

DESCRIPTION	Tire Friction Parameter	Tire Footprint Friction Angle	Fore and Aft Spring Rate at Axle	Axle Rotational Spring Rate	Tire to Wheel Rotational Spring Rate	Controls Hydroplanning influence	Tire Lateral Spring Rate	Tread to Wheel Spring Rate	Fore and Aft Damping Coefficient at Axle	Water Resistance Coefficient	Gear to Axle Rotational Damping Coeff.	Tire to Wheel Rotational Damping Coeff.	Rolling Resistance Parameter	Tire Lateral Damping Coefficient	Tread to Wheel Damping Coefficient	Rolling Resistance Parameter	Tire to Wheel Coupling Spring Rate	Tire Friction Correction Coefficient	Tread to Wheel Coupling Spring Rate	Horizontal Force on Tire Footprint	from Ground	Horizontal Force at Axle	Lateral Tire Load (On Ground)	Horizontal Wheel Unbalance Force	Vertical Wheel Unbalance Force
UNITS	sec/in	rad	lb/in	in 16/rad	in 16/ rad	1	1b/in	lb/in	16 sec/in	16 secting	in 16 sec/rad	in 16 sec/rad	91	lo sec/in	ib sec/in	16 sec/rad	in 16/rad	sec/in	lb/in	<u>a</u>		۹/	ام	ব	9
VALUE	N. 5 × 10 1 W		2.0 × 105	10.4 × 104	19.5 × 106	0.0	6460	10,200	7.8.6	0	132	30,400	2350	5.165	15.9	40.3	10.15 × 10 2	401×59.	5300						
TYPE	U	Þ	U	U	U	U	U	U	U	U	U	U	U	U	U	υ	U	ပ	U	>		(o)^	>	>	(0)^
SYMBOL	К	37	ა ()	CRS	() PR	C _H	Cst	CTT	De	DHY	DRS	DRT	DSR	Dsr	Drr	DVR	n T	Ē	ETT	F 69		IT _O	Fax	FORH	FORY

Table 11 (Contd)

DESCRIPTION	Vertical Force between Tire and Ground		Lateral Tire Load (On Apl)	Net Force between Tread and Wheel	Axle Height Above Ground	Gear Rotation	Gear Rotational Velocity	Axle Rotation	Axle Rotation at Time = 0	Axle Rotational Speed	Axle Rotational Speed at Time = 0	Axle Rotational Acceleration	Tire Tread Rotation	Tire Tread Rotation at Time = 0	Tire Tread Rotational Speed	Tire Tread Rotational Speed at Time = 0	Tire Tread Rotational Acceleration	Wheel Rotation	Wheel Rotation at Time = 0		Rotational	Wheel Rotational Acceleration	Dummy Variables used to	Simulate Visco-Elastic Tire	Characteristic
UNITS		<u>a</u>	<u>:</u>	વ	. <u>\$</u>	rad	rad/sec	, a d	rad	rad/sec	rad/sec	rad/sec ²	rad	rad	rad/sec	rad/sec	rad/sec2	rad	rad	rad/sec	rad/sec	-3-d /sec2	rad	rad	rad/sec
VALUE									6250.		0.0			0.0		106.7			0.0		106.7			0.0	
TYPE	v(I)		(o)^	>	>	v(I)	v(I)	>	υ	>	U	>	>	U	>	U	>	>	v	>	U	>	>	U	>
SYMBOL	با لبا الم	r E	II.	Ľ.	Ļ	$\Theta_{\mathcal{G}}$, O	θs	$\Theta_{\mathbf{s}\phi}$.م	950	Φ,	θτ	970	φ	Ó To	9,	φ~	Owo.	Φ	Q wo	\$ •	φ	Ovo	Θ_{γ}

Table 11 (Contd)

KKO ROT SX TT TR TR TR	TYPE c c v v(I) v(I) v v v v v v v v v v v v v v v v v v v	0.0 23.32	UNITS b sec²/rad² in ib in ib	Unbalance Coefficient Undeflected Tire Radius Tire Rolling Radius Tire Deflection Brake Torque Torque Producing Rolling Resistance Torque Between Tire (Tread) and Wheel
) 0 > 0 0	1.0 2.2 4.5	! !	Rolling Radius Parameter Tire Friction Coefficient Tire Friction Parameters
< < < < × × × × × × × × × × × × × × × ×	U > >	2400	in/sec in/sec in/sec	Tire Hydroplanning Speed Velocity of Tire Footprint Relative to Flywheel Same as Vrx except rotational effects
× × × × ×	v (0)v		in/sec Rad/sec	Tire Footprint Relative Velocity in X Direction Relative Rotational Speed between Stators and Rotors
Wew Wis Wit	0000	1.6 16.8 115 66.0	lb sec²/in in lb sec²/rad in lb sec²/rad in lb sec²/rad	Effective Tire, Wheel, and Brake Mass Axle Moment of Inertia (+ Stators) Tread Moment of Inertia Wheel and Rotors Moment of Inertia

Table 11 (Contd)

JESCRIPTION	Ws = øs	Wr = Or	Equivalent Tire Tread Mass		_	Location of Tire Tread C. G. at Time = 0	ა	Tread C. G. Velocity at Time = 0	Tread C. G. Acceleration	Horizontal Axie Location	Horizontal Axle Location at Time = 0	Horizontal Axle Velocity	Horizontal Axle Velocity at Time = 0	Horizontal Axle Acceleration	(Dummy Variables used to	<pre> Simulate Visco-Elastic Tire</pre>	(Characteristic	Undeflected Axle Location (1 Direction)	ر د	, х С	Undeflected Axle Velocity (~ Direction)	Footprint Location (& Direction)	Ym at Time = $0 (\gamma_{MR0} = +60) \gamma_{ML0} = -60)$	Footprint Velocity	Ym at Time = 0
UNITS	rad/sec	rad/sec	16 sect/in	rad/sec	2.	2.	in/sec	in/sec	in/sec2	٤.	· 7	in/sec	in/sec	in /sec²	, C	2.	in/52c	2.	in /sec	2,	in /sec	. 5	÷.	in/see	in/sec
VALUE			0.0725			0.0		2400			0.0		2400			0,0							160.0		0.0
TYPE	>	>	υ	>	>	υ	>	Q	>	>	υ	>	U	>	>	Ü	>	(I)^	v(I)	v(I)	v(I)	(0) ^	บ	>	Ü
SYMBOL	W _s	ν.	WTE	N.W.	X	X +TO	×	XTTO	X	≯	Xwo	××	×××	`X	×	×	×	×a×	YAX	×××	×¢×	Σ,	×	٠,>	ÝMO

Table 11 (Contd)

■などのかがある。■などできたとのでは、■をは対域のはは、■国際の人のなどを表現のなってのの。■などのできないできない。 | 「「「「「」」」というできないできない。 「「「」」とは対域のはは、■国際の人のなどを表現のなっている。「「」」というできない。 「「」」というできない。 「「」」というできない。

Γ	_	
	DESCRIPTION	Footprint Acceleration Footprint Position (\approx Direction) Footprint Velocity
	UNITS	in/sect in/sec
	VALUE	
	TYPE	v (0)v v(0)
	SYMBOL	∵×× Σ × 3 Σ × 2

WHEEL SPEED SENSOR

The primary input parameter to an electronic antiskid control circuit is an airplane wheel speed signal. conventional control circuitry the input must be a direct current voltage. The wheel speed sensor may have any one of several forms such as a D.C. tachometer or an A.C. tachometer with variable voltage or frequency converted to a direct current voltage by suitable electronic cir-The control circuit input signal, Es, function of the wheel's angular velocity relative to the axle (tachometer mount) and the characteristics of any associated electronic circuitry used for radio interference suppression and/or for conversion of A.C. frequency or voltage signals to D.J. voltage. To provide the means for mathematically describing the control circuit input signal for a variety of wheel speed sensors, two approaches are The first, identified as Option 1, is applicable whenever there is a perceptible phase lag between actual wheel speed and the antiskid circuit inpu as is generally the case where A.C. voltage signals are converted to D.C. or where a D.C. tachometer is driven through an elastic coupling. A second simpler mathematical description, called Option 2, is provided to minimize computation difficulty and expense where no significant phase lag exists.

A. Mathematical Description

Option 1

Assume that a D.C. tachometer generator is mounted on the axle and is driven by the wheel. The output of the hypothetical generator is assumed to be applied to a linear force motor which acts upon a single degree of freedom damped spring mass system as shown on Figure 47. The control circuit input signal, $E_{\rm G}$, is proportional to the mass displacement. By adjusting the relative characteristics of the linear force motor, hypothetical generator, spring, mass and damper a mathematical description of a wide variety of wheel speed sensors can be accommodated.

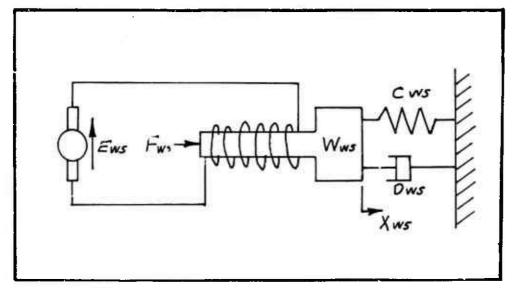


Figure 47 Wheel Speed Signal System

The output of the hypothetical generator, Ews, is proportional to the wheel's angular velocity relative to the axle, Ws, as defined by equation (5.1). Angular velocity, Ws, is obtained as an output of the tire and wheel system.

The force produced by the linear force motor, Fws, is proportional to the generator output, Ews, as defined by equation (5.2).

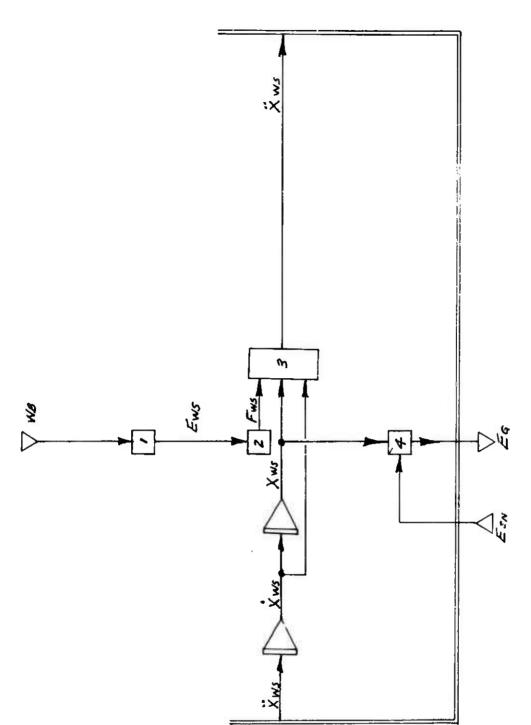
The hypothetical mass displacement, Xws, is obtained from equation (5.3) which results from summing forces on the hypothetical mass, Wws.

(5.3)
$$\ddot{X}_{WS} = \frac{F_{WS}}{W_{WS}} - \frac{C_{WS}}{W_{WS}} (X_{WS}) - \frac{D_{WS}}{W_{WS}} (\dot{X}_{WS})$$

The antiskid circuit wheel speed input voltage signal, E_6 , is proportional to the hypothetical mass displacement, X_{WS} , as defined by equation (5.4).

In equation (5.4), Es# is any extraneous "noise" which might be present due to the operation of other aircraft systems, etc.

The equation flow diagram is shown on Figure 48.



Wheel Speed Sensor Equation Flow Diagram (Option 1) Figure 48

Option 2

For cases where the wheel speed transducer is a D.C. tachometer, or equivalent, driven through a rigid coupling (such as the F-104 and F-111) there is usually very small difference between the actual wheel speed and antiskid control circuit input (i.e., very low phase lag or attenuation) and the extra mathematical complication incurred by using a very high gain second order equation is not justified. For these cases the antiskid control circuit input voltage may be considered proportional to the wheel's angular velocity as defined by equation (5.5).

No equation flow diagram is shown for Option 2.

B. Parameter Evaluation

Option 1

The objective of using a single degree of freedom damped spring mass system to describe the antiskid control circuit input is to provide a mathematical "tool" whereby phase lag within the wheel speed sensor device can be accounted for. Consequently, the values for mass, spring rate and damping coefficient are chosen to produce the desired effect rather than to describe physical devices. The other coefficients are chosen to achieve compatibility with the control circuit. For the F-111 modulated antiskid circuit let the hypothetical tachometer coefficient be the same as for the actual F-111 tachometer, 12 volts per thousand RPM. Therefore:

Let the force motor coefficient, the elastic system spring rate and output voltage coefficient all be equal to unity so that for steady state conditions the control circuit input, $\mathcal{E}_{\mathcal{G}}$, is the tachometer output. Therefore:

(5.7)
$$CWG = 1.0 \ 16F/VOLT$$

$$CWS = 1.0 \ 16F/INCH$$

$$CCGV = 1.0 \ VOLT/INCH$$

Based on information furnished by the Goodyear Aerospace Corp. the component characteristics and arrangement which is usually utilized for converting A.C. frequency to D.C. voltage produces about 30 degrees (or greater) phase lag at 5 cps. The following equations from reference 12 describe the single degree of freedom system's behavior when an oscillatory force XoKSWWt is applied.

(5.8)
$$\frac{\chi}{\chi_0} = \sqrt{\left[1 - \left(\omega/\omega_n\right)^2\right]^2 + \left(2s\omega/\omega_n\right)^2}$$

$$\sqrt{\frac{2}{1 - \left(\omega/\omega_n\right)^2} + \left(2s\omega/\omega_n\right)^2}$$

In these equations ϕ is the phase angle, S = Dws/ZWwsWn is the damping factor, wn = VCws/Wns is the undamped natural frequency, w is the frequency of applied oscillatory loading, and x/x_0 is the magnification factor. If the degree of attenuation and phase angle are known at a particular frequency, the undamped natural frequency and damping factor are established. Assuming two percent attenuation and 30 degree phase lag at 5 cps, the equations above give an undamped natural frequency of 14.6 cps (91.8 Rao/sec) and a damping factor of 0.746.

For an undamped natural frequency of 91.8 RAO /SEC and a spring rate, Cws, of 1.0 lbf//N the mass, Wws, is established as $O(105 \times 10^{-9})bf SEC^2/N$. The damping coefficient, O_{WS} , is established from the mass and damping factor as

Option 2

For use with the F-111 modulated antiskid control circuit, use the actual F-111 tachometer output of 12 volts D.C. per 1000 RPM. Therefore:

For use with the on-off antiskid circuit as installed on the F-104 (and B-58) the tachometer output is 20 volts per 1000 RPM. To make the on-off circuit compatible with the F-111 requires that the difference in tire size (46.5 inch dia. for F-111 versus 22 inch dia. for B-58) also be accounted for. Therefore, for the on-off antiskid circuit use:

Table 12 Wheel Speed Sensor Parameters

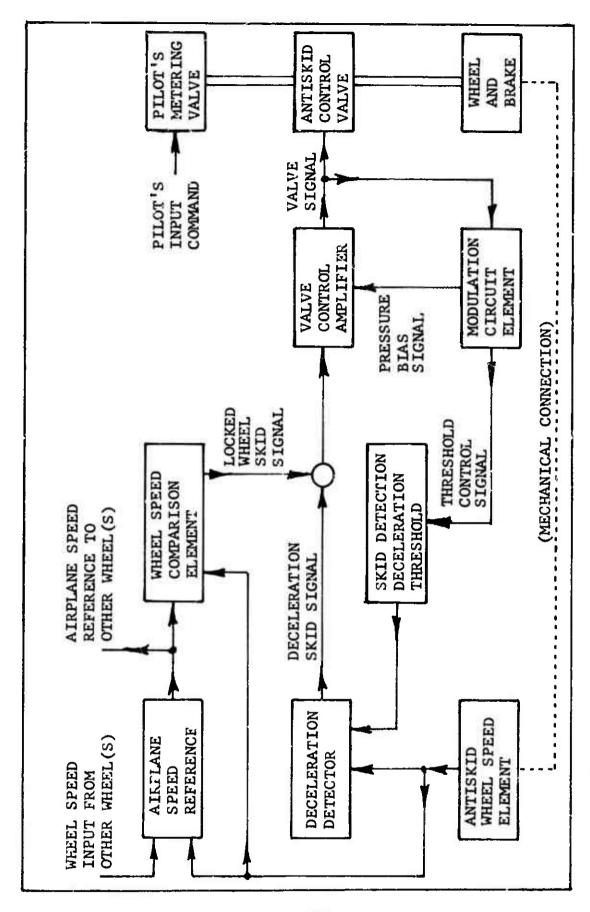
DESCRIPTION	FOR USE WITH F-111 MODULATED CIRCUIT	Output Voltage Coefficient	Hypothetical Liner Force Motor Coefficient	Spring Rate (Hypothetical Spring)	Damping Coefficient (Hypothetical Damper)	Antiskid Control Circuit Input Signal	Hypothetical Tachometer Voltage	Hypothetical Linear Force Motor Output	Force	Hypothetical Tachometer Voltage-Speed	Coefficient	Input Signal "Noise"	Mass (Hypothetical Mass)	Wheel Angular Velocity Relative to Angle	Hypothetical Mass Displacement	Hypothetical Mass Displacement at Time	Zero	Dimothotical Mass Velocity	Macc	CCBL	FOR USE WITH F-111 MODULATED CIRCUIT	
UNITS	FOR USE WITH	VOLT /IM	16F / VOLT	N1/391	165 Sec/14	VOLTS	VOLTS	16 6		VOLT SEC/RAD		VOLTS	1bf sec2/11	RAO/Sec	/NCT	INCH	, ,	וא / שבר	1N/ SEC	12/260	FOR USE WITH	VOLT SEC/RAD
VALUE	OPTION 1	1.0	1.0	1.0	0.1623×10-2					0.1147		0.0	O.1185×10			0.0		Į.	0.0		OPTION 2	0.1147
TYPE		ပ	ပ	ပ	ບ	(o) _A	>	>		υ	,	v(I)	υ	(I)^	>	U	i P	> (\$ د	•		c v(I)
SYMBOL		Ccgv	ر د د د	Cws	D WS	EG	Fws	Fws		Gws		ESN	Wws	WB	Xws	Xwso	•>	χ.,	× × × × × × × × × × × × × × × × × × ×	XWX		GWOC ESN

FOR USE WITH F104 ON-OFF CIRCUIT DESCRIPTION Table 12 (Contd) VOLT SEC / RAD VOLTS UNITS OPTION 2 VALUE 0.0 c v(I) TYPE SYMBOL Gwoc Esn

6a. MODULATED ANTISKID CONTROL CIRCUIT

After introduction of on-off type antiskid systems, it became apparent from various analyses and studies of test results and operational performance that braking effectiveness could be increased if the number of antlskid cycles and their intensity could be minimized. To minimize antiskid cycling occurrences and intensity, it is necessary to control the amount of brake torque being applied such that the available friction torque is not exceeded for as much of the time as is possible. A number of devices utilizing various principles of operation have been used for this These devices predominately utilize the principle of regulating or "modulating" brake pressure to keep its value as near as possible to that which will produce a skid. One of the first of these type devices is a hydraulic pressure modulator comprised of an orifice and accumulator installed upstream from the pilot's metering valve and configured such that repetitive antiskid cycling causes a temporary reduction in pilot's metered pressure. Convair Model 880 airplane's Hytrol MKI antiskid system with hydraulic modulation is a typical example of this type installation.

A subsequent development was the Bendix system which is used on Grumman A6A and Lockheed C141 aircraft. system combines hydraulic modulation accomplished within the off-on type control valve with two levels of skid detection, (i.e., brake pressure reduction in two steps controlled by skid intensity). Further improvements have been achieved by utilizing a servo type pressure regulating valve with electronic control to achieve a wide range of control characteristics and better accommodate widely varying runway friction conditions encountered during aircraft operation. The Goodyear Adaptive system used on General Dynamics F-111 aircraft and the Hytrol MK II system used on McDonnell-Douglas F4C and LTV A7A aircraft are examples of the servo valve type systems. Within each of the types or classes of systems there are a number of variations in circuitry and component arrangement depending upon the aircraft type, landing gear arrangement and configuration, and the airplane's mission requirements. For this program a mathematical model of the F-111 airplane's Goodyear Adaptive Antiskid Control Circuit is developed. Models for other type circuits can be developed using similar procedures.



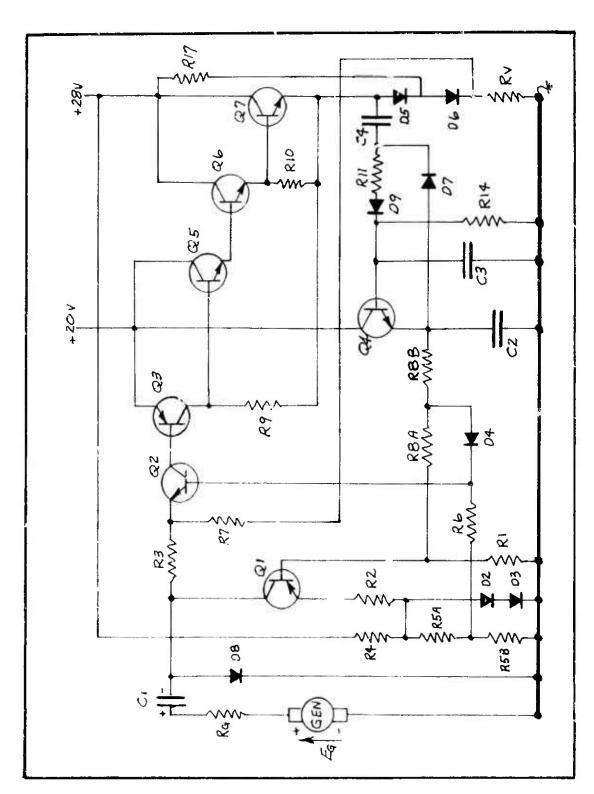
そのでは、1919年のでは、1919年のでは、1919年のできない。1919年のできないでは、1919年のできないできない。1919年のできないできないできない。 1919年の1919年の1919年のできない。1919年のできないできないできない。1919年のできないできないできない。1919年のできないできないできないできない。1919年の1919年の1919年の1919年の19

Modulated Antiskid Control Functional Block Diagram Figure 49

Figure 49 is a block diagram showing the basic functional elements of the Goodyear adaptive antiskid control circuit as used on the F-111 airplane and showing the relationship of the control circuit to the other brake system components. During antiskid circuit operation, a wheel speed signal is provided as an input to a deceleration detector. deceleration detector the wheel's deceleration rate is computed and compared to a threshold value provided by a skid detection threshold circuit element. The deceleration detector produces a skid signal proportional to the amount by which the wheel's deceleration rate exceeds the threshold The skid signal is applied to a valve control amplifier which in turn produces a valve control signal proportional to the input skid signal plus any pressure bias signal which might exist. The valve control signal is supplied to the antiskid control valve (a servo type pressure regulator) for brake pressure control and to a modulation circuit element. The modulation circuit element interprets the valve control signal and provides a pressure bias signal to the valve control amplifier and a threshold control signal to the skid detection threshold circuit The wheel speed signal is also supplied to the locked wheel prevention circuit elements consisting of an airplane speed reference and a wheel speed comparison When the airplane speed reference indicates that the airplane's speed exceeds "locked wheel arming speed" (usually 20 mph) and simultaneously the wheel speed is less than that which should exist for a slightly lower airplane speed (usually 10 mph), the wheel speed comparison circuit element produces a skid signal sufficient to fully release the brake. Locked wheel arming speed is chosen as some reasonably low speed below which a locked wheel is not particularly detrimental. The locked wheel feature is deactivated below locked wheel arming speed so that the airplane can be brought to a complete stop. The aircraft circuit also incorporates circuit elements for failure detection, automatic cutoff and prevention of brake application prior to touchdown. These logic type functions do nct affect aircraft stopping performance and are not included in this analysis.

A. Modulated Antiskid Circuit Mathematical Description

A simplified schematic diagram of the Goodyear adaptive antiskid circuit for one wheel as used on F-111 type aircraft is shown on Figure 50 . This circuit accom-



50 Modulated Antiskid Control Circuit Schematic Figure

plishes deceleration skid control as previously described in the control circuit functional description as follows. An input voltage, Eq., is provided by a wheel driven D. C. tachometer generator (GEN). Eg charges the deceleration detector, capacitor, Ci, through resistance RG and diode DB during wheel spin-up. For normal wheel deceleration rates, with no incipient skidding, the generator voltage will decrease relatively slowly and a small current will flow from the positive side of C_{ℓ} through R_{ξ} , the generator, R4, R2, and transistor Q_1 to the negative side of C_1 . This current discharges capacitor Co and causes its voltage to closely follow E_6 . Transistor Q_1 is the skid detection threshold circuit element. Qi is a currentlimiting device that offers very low impedance to current below its chreshold value and extremely high impedance to The threshold is conany current above that threshold. trolled by Ri. Diodes Di and Di provided bias voltage for the operation of Q_{I} . When an incipient skid occurs, the generator voltage decreases rapidly and since Q1 limits the discharge current into Ci, the voltage at the negative side of Co decreases and causes current to flow through R5A, R_6 , Q_2 , and R_3 . The current into the base of Q_2 is amplified by Q_1, Q_2, Q_3, Q_6 and Q_7 , (the valve control amplifier) to produce a voltage across Rv, the antiskid valve coil. Voltage applied to the antiskid valve causes brake pressure to be reduced proportionally and thereby alleviate the incipient skid. Antiskid valve voltage is feedback to the amplifier input through R7 to stabilize amplifier gain against changes due to temperature and component characteristic variations.

Antiskid valve voltage pulses are transmitted to the modulation circuit elements through capacitor C4. Within the modulation circuit element, consisting of C4, Rn, R14, D_7 , C_3 , C_2 , D_9 and Q_4 , each increase in voltage to the valve produces an increase in the charge on C_3 . Voltage on C_3 causes Q4 to charge C2. Since C2 discharges through R88, R84, and R_1 , the voltage on C_2 provides a threshold control The charge on C_3 , and in turn on C_2 , is signal to Q_i . a function of the amplitude and frequency of valve voltage pulses. Voltage on C2 is also applied to Q2 through Rag and \mathcal{D}_{ℓ} to provide a pressure bias signal to the valve control amplifier. The operation of the modulation circuit element results in an automatic threshold change to the skid sensing circuit and a bias to the valve control amplifier to match the braking conditions being encountered.

The equations listed in Tables 13, 14, 15, 16, and 17 describe the circuit's operation in accordance with the equation flow diagram shown on Figure 51. The assumptions and procedures used to develop these equations are described in Appendix I. The circuit has twelve possible modes of operation depending upon the instantaneous conditions which exist. The conditions which define the circuit's mode of operation at a particular instant are: (1) the current, Ac4, into capacitor C4 is either positive, negative or zero, (2) the valve control amplifier is operating either in the cutoff mode or in the amplification mode, and (3) the modulating circuit element is either providing a pressure bias signal or it is not. Table 18 lists the twelve circuit modes resulting from combinations of the above circumstances. The valve amplifier condition is indicated by current A_{EO2} being equal to or less than C607 in the cutoff mode and being greater than C607 in the amplification mode. The pressure bias signal is indicated as existing when voltage Vs is greater than zero and as not existing when Vs is equal to or less than zero.

The circuit condition which exists at a particular instant is established by assuming a condition and using the equations applicable to the assumed condition to test for the validity of the assumption. For instance, circuit condition number 1 assumes that current Ac4 is positive; therefore, equation 6a-N8-1 from Table 16 must indicate a positive value of Ac4 for the assumption to be correct. If so, then the equations for Ae4 and Ve are similarly tested. If the assumed condition is correct, the applicable equations are used to compute the various currents and voltages. If the assumed condition is found to be incorrect, other conditions are successively assumed and tested until the correct condition is found.

B. Parameter Evaluation

Table 19 lists the parameters defining the modulated circuit's operation. The values for the constants are computed from various circuit element characteristics (resistance, capacitance, etc.) as described in reference 13 and in the semiconductor component manufacturers catalogs.

Table 13 Modulated Antiskid Circuit Equation Summary

_	
Equation No.	Equation
(6a-1)	Vc1 = \int Vc1 dt
(6a-A1)	Vc1 = Ac1 C608
(6a-2)	Vc2= ∫ Vc2 dt
(6a-A2)	Vcz= Acz C609
(6a-3)	Vc3- S Vc3 dt
(6a-A3)	Vc3 = Ac3 C610
(6a-4)	Vc= / Vc4 dt
(6a-4A)	Vc4 = Ac4 C611
(6a-5)	$(E_6-V_{ci})=E_6-V_{ci}$
(6a-6)	ALWS = (C617 FOR VF > C615 AND EGCC616 = O FOR VF = C615 OR EG = C616
	= 0 FOR VF = CG15 OR EG = C616
(6a-LW-1)	AVAI = AEQ2 + ALWS
(6a-N3)	Ac3=(Ac4-Vc3 C614-ABA4 FOR Ac4>0
	Ac3={Ac4-Vc3 Co19-ABQ4 FOR Ac4>0 =(-Vc3 Co19-ABQ4 FOR Ac4=0
(6a-N4)	Ev = ADS C406+C407
(6a-N5-n)	See Table 15
(6a-N8-n)	See Table 16
(6a-N10)	AR3= AEQ2 C612+ [EV-(E6-Vei)] C613
(6a-N11)	Ac1 = AD8-AR1-ACQI
(6a-N14)	Ac2 = 1AEQ4 + Ac4-VC2 C618 FOR AC4 < 0 =VAEQ4 - VC2 C618 FOR Ac4 ≥ 0
	=1AEQ4 - VC2 C618 FOR AC4 ≥0

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Table 13 Modulated Antiskid Circuit Equation Summary (Contd)

Equation No. Equation

$$(6a-Q-1C) \qquad Acq_1 = |C_{604} - C_{605}|V_{C_2}| \quad For |E_4 - V_{C_1}| \leq 0$$

$$= 0 \qquad \qquad For |C_6 - V_{C_1}| \geq 0$$

$$= 0 \qquad \qquad For |V_{C_2}| \leq C_{604} / C_{605}|$$

$$(6a-Q4) \qquad AEQ4 = |C_{614}| \quad ARQ4$$

$$(6a-R10) \qquad AOS = |(E_6 - V_{C_1})|C_{620} - C_{621}| \quad For |E_6 - V_{C_1}| > C_{621} / C_{620}|$$

$$= 0 \qquad \qquad For |E_6 - V_{C_1}| \leq C_{621} / C_{620}|$$

$$= 0 \qquad \qquad For |E_6 - V_{C_1}| \leq C_{621} / C_{620}|$$

$$= 0 \qquad \qquad For |E_6 - V_{C_1}| \leq C_{621} / C_{620}|$$

$$= 0 \qquad \qquad For |E_6 - V_{C_1}| \leq C_{621} / C_{620}|$$

$$= 0 \qquad \qquad For |E_6 - V_{C_1}| \leq C_{621} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

$$= 0 \qquad \qquad For |V_{C_3} - V_{C_2}| \leq C_{623} / C_{622}|$$

Table 14 Pressure Bias Signal Condition Test Equations

Circuit Condition, n	Pressure Bias Signal Test Equation (Equation 6a-VB-n)
1 & 2	VB = VC2 Cm - C464 (EG-VC1) - C465 (VC3+VC4) + C463
3 & 4	VB = VC2 CM - C467 (EG-Ki) - C468 (VC3+VC4) + C466
5 & 6	VB = Vc2 Cm - C558 (E6 - Vc1) + C559
7 & 8	V8 = Vc2 Cm - C560 (EG-Vc1) + C561
9 & 10	VB = Vc2 Cm - C582 (EG-Vc1) - C583 (Vc2+Vc4) + C584
11 & 12	V8 = Vc2 Cm - C585 (E6-Vc1)-C586 (Vc2+Vc4) + C587

Table 15 Summary of Equations for Computing Current Aos

Circuit Condition, n	Applicable Equation 6a-N5-n (See Note)
1 & 2	A05 = AVAI C606 - AC4
3 & 4	A05 = AVAI C606 C404 - C405 - AC4
5 & 6	ADS = AVAI CGOG
7 & 8	A05 = AVAI C606 C404 - C405
9 & 10	A05 = AVAI C606 - AC4
11 & 12	ADS = AVAI C606 C404 - C405 - AC4

Note: For all circuit conditions if Aos < O, set Aos = O

Table 16 Capacitor C4 Current Mode Test Equations

Circuit Condition, n	Applicable Equation (6a-N8-n)
1	Ac4 = - (EG-VC,) C476 - (VC3+VC4) C477 - C478
2	AC4 = VC2 C480 - (E6-VC) C479 - (VC9+VC4) C481 - C482
3	AC4 = -(EG-VC)C469 - (VC3+VC4)C470 - C471
4	AC4 = VC2 C473 - (EG-VC,) C472 - (VC3+VC4) C474 - C475
5 - P	+Ac4 = - (E6-Vc,) C548 - (Vc = rVca) C537 r C549 mo
5 -N	-AC4 = (EG-K) C550 + (VC2+K4) C539 - C551
6-P	+ Ac4 = VC2 C552 - (EG-VG) C553 - (VC31 VC4) C537 - C554 AND
6-N	- Ac4 = - Vc2 C555 + (Eq-Ki) C556 + (Vc2 +Vcx) C539 - C557
7 - P	+ Ac4 = - (E4-Ve,)C516-(Vc3+Vc4)C517 + C518 AND
7-N	- Ac4 = (EG-VC,) C540 + (VC2+VC4) C539 - C541
8 - P	+ Ac4 = Vc2 C542 - (E6-Vc1) C543 - (Vc3+Vc4) C537 - C544 AND
8 - N	- AC4 = - VC2 C545 + (E6 +C1) C546 + (VC2+VC4) C639 - C547
9	AC4 = -(E6-16,) C589 - (VC2+VC4) C588 + C590
10	Ac4 = VC2 C592 - (E6-VG) C593 - (K2+VCa) C591+C594
11	Ac4 = - (EG-VC1) C596 - (VC2+VC4) C595 + C597
12	Ac4 = VC2 C599 - (EG-161) C600 - (162+164) C598+C601

Table 17 Valve Amplifier Operating Mode Test Equations

Circuit Condition,n	Applicable Equation (6a-Q2-n) (See Note)
1	AEQ2 = - (EG-Vc1) C456 - (VC3+VC4) C457 + C458
2	AERZ = VC2 C461 - (EG-VC1) C459 - (VC3+VC4) C460 + C462
3	AEQZ = -(EG-Vci) C446-(Vc3+Vc4) C447 + C448
4	AEQ2 = Yc2 C450 - (EG-Vc1) C449 - (Vc3 + Vc4) C451 + C452
5	AEQ2= - (EG-Vc1) C531 + C532
6	AEQ2 = VCZ C533 - (EG-VCI) C534 - C535
7	AEQ2 = - (EG-VCI) C526 + C527
8	AEQ2 = VC2 C528 - (EG - VC1) C529 - C530
9	AEQ2 = -(EG-VCI)C565-(VC2+VC4)C566 +C567
10	AEQ2 = VC2 C568 - (E6-VC1) C569 - (VC2+VC4) C570 - C571
11	AEQ2 = - (Eq-Vc) (575 - (Vc2 + Vc4) (576 + C577
12	AEQ2 = VC2 C578 - (EG - VC1) C579 - (VC2+VC4) C580 - C581

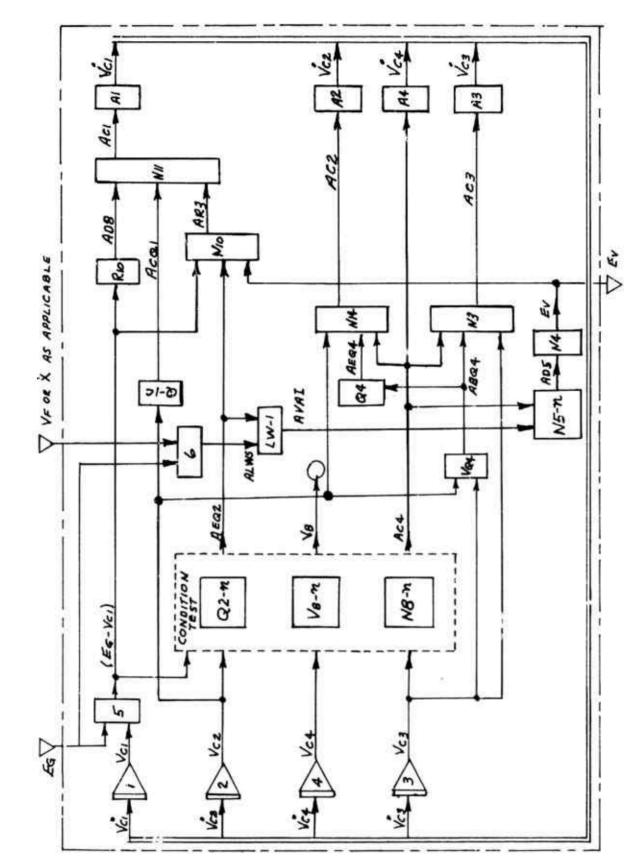
Note: For all Circuit Conditions if AEQ2 < 0, SET AEQ2 = 0

Table 18 Modulated Antiskid Circuit Conditions

Circuit Condition	Capacitor C4 Current Mode (See Note 1)	Valve Amplifier Operating Mode (See Note 2)	Pressure Bias Signal Condition (See Note 3)
1	Ac4 > 0	AEQ2 = (607	<i>YB</i> ≤ 0
2	Ac4>0	AEQ2 = C607	VB >0
3	Ac4>0	AEQ2 > C607	V8 ≤ 0
4	Ac4 > 0	AEQ2 > C607	VB>0
5	Ac4=0	AEQ2 = C607	V8 ≤0
6	Ac4 = 0	AEQ2 = C607	V8>0
7	Hc4 = 0	AEQ2 > (607	VB ≤0
8	Ac4 = 0	AEQ2 > (607	V8>0
9	Ac4 40	AEQ2 = C607	V8 ≤0
10	Ac4 LO	AEQ2 5 C607	V8>0
11	Ac4 < 0	AEQ2 > C607	V8 40
12	Ac4<0	AEQ2 > C607	V8 > 0

Notes:

- 1. Capacitor (4) is charging for Ac4>0, static for Ac4=0 and discharging for Ac4<0.
- The valve amplifier is amplifying for AEQ2 > C607 and is cutoff for $AEQ2 \le C607$.
- 3. A pressure bias signal exists for $\sqrt{s} > 0$ and does not exist for $\sqrt{s} \le 0$.



Modulated Antiskid Circuit Equation Flow Diagram 51 Figure

Table 19 Modulated Control System Parameters

Description (See Note)	Transistor Q4 Base Current	Current thru Capacitor Cl	Current thru Capacitor C2	Current thru Capacitor C3	Current thru Capacitor C4	Transistor Q1 Collector Current	Current thru Diode D5	Current thru Diode D8	Transistor Q2 Emitter Current	Transistor Q4 Emitter Current	Current thru Resistor R3	Input Signal from Wheel Speed Sensor	Circuit Condition Determination Voltage		across	across	Voltage across Capacitor C2 at Time Zero	Voltage across Capacitor C3	Voltage across Capacitor C3 at Time Zero	across	across	d Valve	Locked Wheel Skid Signal	Flywheel Velocity	VG2 Voltage Coefficient EQU VB -n	
Units	Amps	Amps	Amps	Amps	Amps	Amps	Amps	Amps	Amps	Amps	Amps	Volts	Volts	Volts	Volts	Volts	Volts	Volts	Volts	Volts	Volts	Volts	Amps	In/Sec	DIMLS	
Value									•						0.0		0.0		0.0		0.0				0.23	
Type	>	>	>	>	>	>	>	>	>	>	>	(I)^	>	>	ပ	>	ပ	>	ပ	>	U	(0)^	>	v(I)	ပ	
Symbol	ABQ4	Ac:	Acz	Acs	ACA	Acai	ADS	A 08	AEQ2	AEQ4	ARB	EG	1/8	VCI	VC10	1/62	VCZO	103	1/530	104	Vc40	EV	ALWS	Vr	ن	

For example, $\Lambda 11$ equation numbers in Description are preceded by 6a. EQU VB-n means equations number 6a-VB-n. Note:

Table 19 (Contd)

7 C 2476.0 Dimls 6 C 0.706 Amps 7 C 66.0 Ohms 7 C 1.57 Volts 7 C 1.825x10-6 Mhos 7 C 0.312x10-6 Mhos 8 C 0.474x10-6 Mhos 9 C 0.474x10-6 Mhos	w w
c 0.706 Amps c 66.0 Ohms l.5/ Volts c 7.825x10 ⁻⁴ Mhos c 0.312x10 ⁻⁶ Mhos c 0.474x10 ⁻⁶ Mhos c 0.474x10 ⁻⁶ Mhos c 0.474x10 ⁻⁶ Mhos	S
c 66.0 Ohms 1.5/ Volts c /.825x10^-6 Mhos c 0.312x10^-6 Mhos c 0.474x10^-6 Mhos c 0.474x10^-6 Mhos	Ø
c /.5/ Volts c /.825x10 ⁻⁶ Mhos c /.44x10 ⁻⁸ Mhos c /.86x10 ⁻⁶ Amps c /.86x10 ⁻⁶ Mhos c /.474x10 ⁻⁶ Mhos	v
c (.825x10° Mhos c (0.44x10° Mhos c (.86x10° Mhos c (.86x10° Mhos c (.474x10° Mhos	
c 0.1441.0-8 Mhos c 0.312×10-6 Amps c 1.86×10-6 Mhos c 0.4741.0-6 Mhos	
c 0.312×10 ⁻⁶ Amps c 7.86 × 10 ⁻⁶ Mhos c 0.474×10 ⁻⁶ Mhos	
c 0.47410-6 Mhos	
c 0.4741.0-6 Mhos	
0 17/77 P	
Soum	
-1.73 x10-6 Amps	
c 34.0 x 10 -6 Mhos	
Mhos	
Amps	
Mhos	_
Mhos	
c /3.25 x 10 6 Mhos	
Amps	Const EQU C
C463 c -1.151 Volts Cor	
C464 c 0.3/2 Dimls (E(Dimls (EG-VC1) Coefficient EQU VB1-2
c -0.911 Volts (_
Dimls	_
Dimls	(VC3 + VC4) Coefficient EQ
$C \neq 69$ c 975.0×10^{2} Mhos (Eq.	
C470 c 110,0110-6 Mhos (VC	Mhos (VC3 + VC4) Coefficient EQU N8-3

Table 19 (Contd)

	Units Description (See Note page 167)	Amps Const EQU N8-3	Mhos (EG-VC1) Coefficient EQU N8-4	N8-4	Mhos (VC3 + VC4) Coefficient EQU N8-4	Amps Const EQU N8-4	Mhos (EG-VC1) Coefficient EQU N8-1	Mhos (VC3 √ VC4) Coefficient EQU N8-1	Const EQU N8-1	Mhos (EG-VC1) Coefficient EQU N8-2	Mhos VC2 Coefficient EQU N8-2	Mhos (VC3 + VC4) Coefficient EQU N8-2		(EG-VC1) C		Mhos VC2 Coefficient EQU Q2-8	ш	Amps Const. EQU Q2-8	Mhos (EG-VC1) Coefficient EQU Q2-5	Amps Const. EQU Q2-5	Mhos VC2 Coefficient EQU Q2-6	ш	,	Mhos (EG-VC1) Coefficient EQU N8-7P	Mhos (VC3 + VC4) Coefficient EQU N8-5P, N8-6P,	N8-7P, N8-8P	Amps Const EQU N8-7P
-		و		_	-				?															_	_		
	Value	388.0 x 10	995.0x10-6	254.0110.4	110.0110.0	1480.0110.6	7.35 X10-6	109.0110-6	-227.5410	11.25	2.87x10-6	109.0 X10-6	-212.5 410-6	1.82x10-6	0.47/10-6	0.472110-6	1.85 x10	1.565×10-6	34.0 × 10-6	-17.5 x 10-6	1325410.6	57.6110-6	83.5×10-4	981.0110-6	110.0110-1	(-504.0x10
	Type	0	ပ	ပ	ပ	ပ	ပ	U	U	U	ပ	O	ပ	O	ပ	O	ပ	O	ပ	ပ	v	U	ပ	U	v		o
	Symbol	C471	C472	6473	C474	5475	C476	C477	(478	6479	C480	1842	C 402	C 526	C527	C528	C529	(530	C 531	(532	(533	C=34	C535	C536	(537	6	C 57.00

Table 19 (Contd)

Type Value Units Description (See Note page 167)	c 0.50 Mhos (VC2 + VC4) Ccefficient EQU N8-5N, N8-6N, N8-7N, N8-8N	c 4.46 Mhos (EG-VC1) Coefficient EQU N8-7N	c -0.78 Amps Const. EQU N8-7N	c 255.0x10' Mhos VC2 Coefficient EQU N8-8P	c 0.0010 Mhos (EG-VC1) Coefficient EQU N8-8P	t. EQU N8-8P	Mhos VC2 Coefficient EQU N8-8N	c 4.53 Mhos (EG-VC1) Coefficient EQU N8-8N	Amps	Mhos (EG-VC1	c 228.0x10-t Amps Const. EQU N8-5P	c 0.0317 Mhos (EG-VC1) Coefficient EQU N8-5N	Amps	c 2.19x/of Mhos VC2 Coefficient EQU N8-6P	c /2.55x/o ⁻⁴ Mhos (EG-VC1) Coefficient EQU N8-6P	c -2/4,0 x10 Amps Const. EQU N8-6P	c 0.0/3/5 Lanos VC2 Coefficient EQU N8-6N	c o.oszz Mhos (EG-VC1) Coefficient EQU N8-6N	c / 578 Amps Const. EQU N8-6N	c 0.3/2 Dimls (EG-VC1) Coefficient EQU VB5-6	c -/. 1545 Volts Const EQU VB 5-6	c 0.0/67 Dimls (EG-VC1) Coefficient EQU VB7-8	Volts C	Mhos (EG-VC1) Coefficient EQU	c 3.54×10^{-6} Mhos (VC2 + VC4) Coefficient EQU Q2-9
Туре	ပ	U	ပ	ပ	U	v	ပ	U	Ų	U	ပ	U	v	v	v	U	v	v	v	U	ပ	U	v	ပ	U
Symbol	C 539	C540	C541	C542	C543	C544	C5.75	C546	C547	C548	549	C550	(55)	C 552	5553	5554	C 555	5.556	C557	5550	C559	C560	C561	C565	C 566

Table 19 (Contd)

ומסיר די (סטורת)	Description (See Note page 167)	Const. EQU Q2-9	effici	(EG-VC1) Coefficient EQU 02-10	(VC2 + VC4) Coefficient EQU Q2-10	Const. EQU Q2-10	Ψ	(VC2 + VC4) Coefficient EQU Q2-11		VC2 Coefficient EQU Q2-12	(EG-VC1) Coefficient EQU Q2-12	(VC2 + VC4) Coefficient EQU Q2-12	Const. EQU Q2-12	Õ	(VC2 + VC4) Coefficient EQU VB9-10	Const EQU VB9-10	(EG-VC1) Coefficient EQU VB11-12	(VC2 + VC4) Coefficient EQU VB11-12	VB11-12	(VC2 + VC4) Coefficient EQU N8-9	×	Const. EQU N8-9	(VC2 + VC4) Coefficient EQU N8-10	VC2 Coefficient EQU N8-10	(EG-VC1) Coefficient EQU N8-10	Const. EQU N8-10	(VC + VC4) Coefficient EQU N8-11
181	Units	Amps	Mhos	Mhos	Mhos	Amps	Mhos	Mhos	Amps	Mhos	Mhos	Mhos	Amps	Dimls	Dimls	Volts	Dimls	Dimls	Volts	Mhos	Mhos	Amps	Mhos	Mus	Mhos	Amps	Mhos
	Value	-17.7 × 10 0	13.41 x 10-6	52.6410-6	5.42x10-6	66.5410-6	22.7×10-6	2.345410-6	-3.2 X 10-6	7.54110-6	29.55 4:0-6	3.05 110-6	36.8 x 10-6	0.314	0.0324	-1.156	0.208	0.0215	-1.0233	0.0/44	0.001	0.0468	0.0145	380.0810-6	0.00/49		0.179
	Type	ပ	υ	υ	υ	υ	ပ	υ	υ	υ	υ	ပ	υ	υ	ပ	υ	ပ	O	U	ပ	υ	υ	ပ	U	υ	υ	υ
	Symbol	Ŋ	C 568	C 569	C 570	(571	5255	C576	C527	0578	5579	6580	(581	C 592	6583	C 584	C505	€586	1850	285	C 589	0850	(56)	532	5650	C5.04	C595

Table 19 (Contd)

_				
Symbol	Type	Value	Units	Description (See Note page 167)
C596	U	1.59	Mhos	(EG-VC1) Coefficient EQU N8-11
8	υ	-0.28	Amps	Const. EQU N8-11
5.98	υ	0.228	Mhos	(VC2 + VC4) Coefficient EQU N8-12
6650	U	0.529	Mhos	
0000	υ	2.07	Mhos	(EG-VC1) Coefficient EQU N8-12
1090	υ	-2.64	Amps	
5000	U	16.1110.6	Amps	Const. EQU Q-1C
5000	U	7.25110-6	Mhos	VC2 Coefficient EQU Q-1C
0600	υ	29.2	Dimensionless	Q3 Collector - Q2 Emitter Current Ratio
1600	υ	1.46x10 6	Amps	AEQ2 Comparison Constant
()	U	0.037×10.0	Volts/Amp Sec	Reciprocal of Capacitance Cl
5090	υ	9.03 K10+4	Volt/Amp Sec	
0 10	U	2.637×10°	Volt/Amp Sec	of Capacitance
į ,	U	J. 222x 1 3 to	Volt/Amp Sec	ta
1.0.2	O	5.90%	Dimensionless	AEQ2 Coefficient EQU N10
7.,	υ	1.19 61.20	Mhos	
1 . 0	Ü	0.9	Dimensionless	
in G	U	352.0	In/Sec	Arming Speed
2	U	3.92	Volts	Signal
4	U	2.76 1.6	Amps	O
9	Ç	3 000000	Mhos	Coefficient EQU
· · · · · · · · · · · · · · · · · · ·	U		Mhos	VC3 Coefficient EQU N3
720 2	O		Mhos	(EG-VC1) Coefficient EQU R10
1.1	U	200.00x10-6	Amps	Const. EQU R10
76.2	·	E46 01.00	Mhos	(VC3-VC2) Coefficient EQU VQ4
6.623	0	593 1410 6	Amps	Const. EQU VQ4

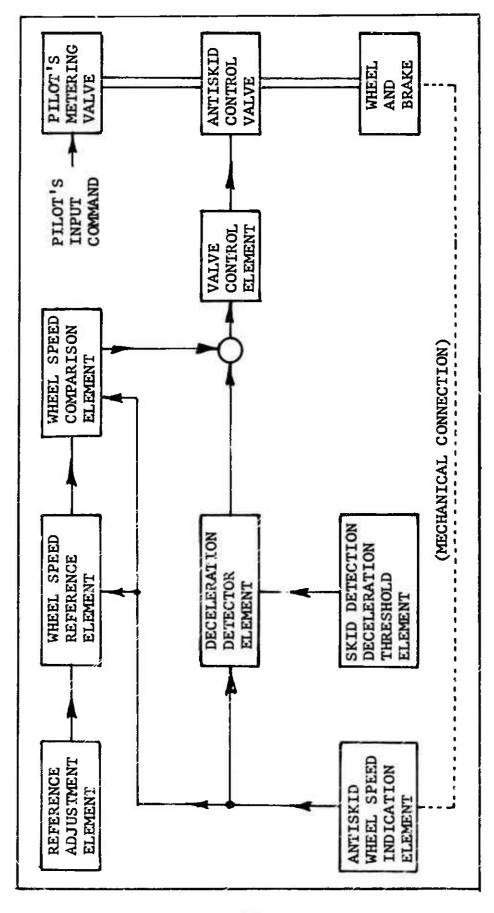
6b. ON-OFF ANTISKID CONTROL CIRCUIT

Most aircraft on-off type antiskid systems operate according to the functional block diagram shown on Figure 52 The various functional elements may be electrical, mechanical or a combination of electrical and mechanical devices. If during braking the brake torque applied to the wheel exceeds the amount which can be reacted by friction at the tire-ground interface, the antiskid system operates to prevent tire skids as follows. A wheel speed signal is provided to a deceleration detection element where the wheel's deceleration rate is computed and compared to a threshold value which is provided by a skid detection threshold ele-The deceleration detector produces a skid signal whenever the wheel's deceleration rate exceeds the threshold value. The wheel speed signal is also supplied to a wheel speed reference element and a wheel speed comparison element. The wheel speed reference element is a "memory" device which produces a "comparison index." The "comparison index" is the wheel's initial unbraked speed minus an adjustment to account for the aircraft's deceleration. wheel speed comparison element compares wheel speed to the "comparison index" and produces a skid signal whenever the wheel speed is less than the "comparison index." The deceleration detection element initiates a skid signal and the wheel speed comparison element maintains the skid signal until the wheel has regained most of its initial The skid signals from both the deceleration detection element and the wheel speed comparison element are transmitted to a valve control element which acts to control the antiskid valve such that the brake is released when a skid signal exists and the brake is applied when a skid signal does not exist.

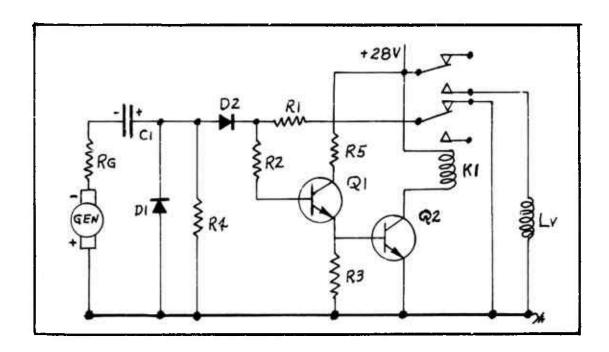
An electrical system of the form shown on Figure 53 or a mechanical device as shown on Figure 55 are the most common means used for implementing the on-off antiskid system function.

Electrical On-Off Antiskid System

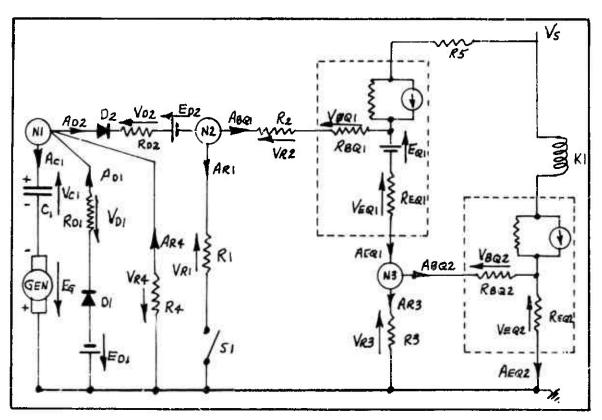
Figure 53 is a schematic diagram of the Goodyear electrical on-off antiskid control circuit as used on the Lockheed F104 and General Dynamics B-58 aircraft. This circuit accompaishes on-off an iskid control according to the preceding functional description as follows: The wheel speed



On-Off Antiskid Control Functional Block Diagram 52 Figure



(A) Schematic Diagram



(B) Mathematical Identification Showing Transistors and Diodes in Terms of their Equivalent Circuits

Figure 53 Electrical On-Off Antiskid Control Circuit

indication element, a wheel driven D. C. tachometer generator (GEN), supplies an input voltage EG which is proportional to wheel speed. EG charges capacitor Cl through R5. Diode D1 and Resistance RG during wheel spin-Capacitor Cl is both the deceleration detector and the wheel speed reference element. For normal wheel deceleration rates, with no incipient skidding, the generator voltage decreases relatively slowly and a small current will flow from the positive side of C1 through R5 and through D2 and R1, (GEN) and RG to the negative side of This current discharges Cl and causes its voltage to closely follow EG. The amplifier comprised of R2, Q1, R3, R4 and Q2 acts as the skid detection deceleration threshold element, the wheel speed comparison element, and, in conjunction with relay Kl. the valve control element. an incipient skid occurs, the generator voltage decreases rapidly. R5 and R1 limit the discharge current flow into Cl so that the voltage at the positive side of Cl increases. The value of the voltage at the positive side of Cl is proportional to wheel deceleration rate. The amplifier characteristics are set so that when the voltage at the positive side of Cl is a value V_{SOT} or greater, enough current flows into the base of Q1 to cause Q2 to conduct sufficiently for relay Kl to actuate. When relay Kl actuates the supply voltage is applied to the antiskid valve coil LV. voltage across the antiskid valve coil, EV, is equal to the supply voltage. Actuation of relay Kl also causes Rl to be disconnected from ground so that the resistance in the discharge path of Cl is increased to aid its action as a wheel speed reference. Voltage Vsor is the skid detection More modern versions of this circuit utilize threshold. transistors to perform the function of relay K1: however. their operation is the same. Resistor R5 is the speed reference adjustment element.

A-1 Electrical On-Off Mathematical Description

The mathematical description of the electrical circuit's operation is developed from Figure 53(b) which is the schematic from Figure 53(a) with the transistors and diodes shown in terms of their equivalent circuits and the appropriate currents and voltages identified.

The voltage across capacitor Cl is defined by:

(6b-1-1)
$$V_{C_1} = \int V_{C_1} dt$$

where (6b-1-A1) $V_{C_1} = A_{C_1} C_{705}$ (C205 = 1/C₁)

Current ACl is established by summing currents at node (N1) as:

(6b-1-N1)
$$A_{C1} = A_{O1} + A_{R4} - A_{O2}$$

Using Ohm's law and summing voltages around the loop of which RDl is a part, current ADl is established as:

(6b-1-R1)
$$A_{01} = E_{G} - V_{C1} - E_{01} / R_{01} \quad FOR (E_{G} - V_{C1} - E_{01}) > 0$$

$$= O \qquad FOR (E_{G} - V_{C1} - E_{01}) \leq 0$$

To combine constants, write equation (6b-1-R1) as:

$$A_{D1} = (E_G - V_{C1}) C_{706} - C_{707}$$
 FOR $(E_G - V_{C1}) > \frac{C_{707}}{C_{706}}$
= O FOR $(E_G - V_{C1}) \le \frac{C_{707}}{C_{706}}$

Noting that because of diode D1, Api is restricted to positive values only.

In a similar manner, using Ohm's law and summing voltages around the loop containing R4, current A_{R4} is established as:

Summing currents at node (N2) gives:

$$(6b-1-N2) \qquad \qquad A_{D2} = A_{BQ1} + A_{R1}$$

By Ohm's law the voltage across RD2 is

(6b-1-v3)
$$V_{02} = A_{02} R_{02}$$

For the case where no skid signal exists and relay Kl is not actuated, Rl is connected to ground and a current ARl may flow. Using Ohm's law and by summing voltages around the loop Rl, D2, Cl and (GEN), ARI is established as:

By substituting equation (N2) into equation (N1) current Aci is established as:

Since the variables EG and VCl are always used in the form of their difference, define the difference as:

(6b-1-3)
$$(E_{G}-V_{C_{1}})=E_{G}-V_{C_{1}}$$

By substituting (6b-1-V3) and (6b-1-N2) into (6b-1-V4),

$$(6v-1-V4)' \qquad A_{R1} = \frac{(V_{C_1}-E_G-E_{O2})}{R_{D2}+R_1} - \frac{A_{BQ_1}R_{O2}}{R_{D2}-R_1}$$

By summing currents at node (N3), current AEQ1 is

$$(6b-1-N3) \qquad \qquad \beta_{\tilde{e}Q} = \beta_{BQ2} + \beta_{R3}$$

By summing voltages around the loop containing R3 and the base and emitter of Q2,

Note: For Q2 the base-emitted junction potential has been omitted to reduce mathematical complexity. This is justified because whether or not Q2 is conducting has negligible effect on current Act.

By substituting (6b-1-N3) along with the Ohm's law expressions ABQ2 = VBQ2/RBQ2 AND AEQ2 = VEQ2/REQ2 and the transistor characteristic AEQ2 = (hFE2 + I)ABQ2 into (6b-1-V5) and solving for ABQ2,

By substituting $(6b-1-V5)^{\dagger}$ and (6b-1-N3) into the Ohm's law expression VR3 = RR3 R3

By summing voltages around the loop R3, REQ1, EQ1, RBQ1, R2, RD2, C1 and (GEN)

By substituting (6b-1-2) and (6b-1-V4) along with the Ohm's law expressions $V_{EQ_1} = A_{EQ_1} R_{EQ_1}$, $V_{BQ_1} = A_{BQ_1} R_{BQ_1}$ and the transistor characteristic $A_{EQ_1} = (h_{EQ_1} r_1) A_{BQ_1}$ into (6b-1-V6) and solving for A_{BQ_1} :

(6b-1-V6)'
$$ABQ_{1} = (Vc_{1} - E_{G})(701 - C_{702} FOR(Vc_{1} - E_{G}) > \frac{C_{702}}{C_{701}}$$

$$= O \qquad FOR(Vc_{1} - E_{G}) \leq \frac{C_{702}}{C_{701}}$$

For the case where relay K1 is actuated and R1 is disconnected from ground the same substitution is made except that $V_{\mathcal{D}\mathcal{L}} = \mathcal{As}_{\mathcal{R}^{\dagger}} \mathcal{R}_{\mathcal{D}\mathcal{L}}$ is used in place of equation (6b-1-V4). For the actual circuit components used on the aircraft, the resulting equation has coefficients that are negligibly different from (6b-1-V6); therefore, equation

(6b-1-V6) will be used for both cases.

The value of ABQ; which causes relay Kl to be actuated is defined as, C700, the skid detection threshold current. From this definition and equation (6b-1-V4)

(6b-1-V4-1)
$$ARI = (V_{C_1} - E_{G})C_{709} - C_{710} - ABQIC_{711}$$

$$FOR ABQI \leq C_{700}$$

$$= O \qquad FOR ABQI \geq C_{700}$$

When relay Kl is not actuated EV = 0, when relay Kl is actuated EV = VS; therefore,

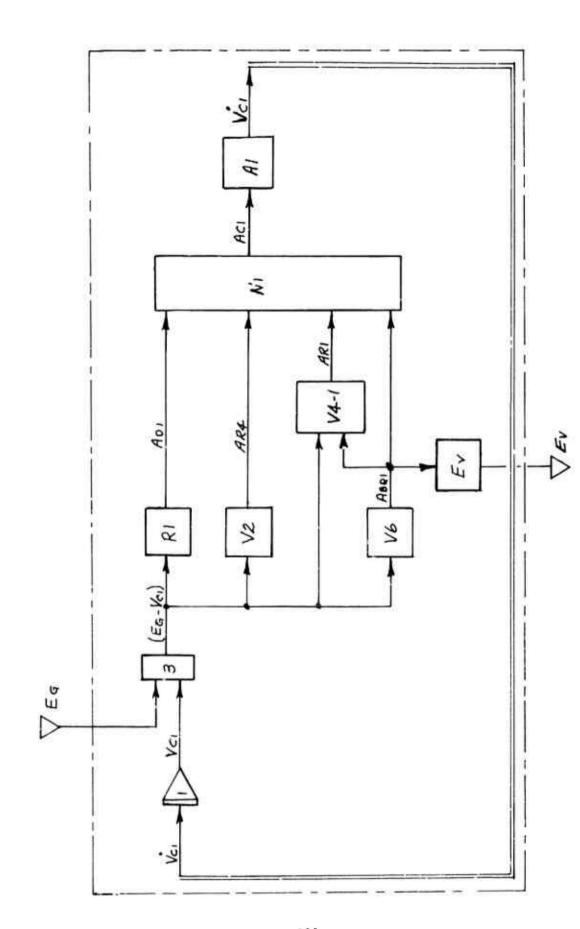
(6b-1-EV)
$$E_{V} = O \qquad For \quad ABQI \leq C700$$

$$= Vs \qquad FOR \quad ABQI \geq C700$$

The equation flow diagram for the electrical on-off control circuit is shown on Figure 54.

B-1 Electrical On-Off Parameter Evaluation

Table 20 lists the parameters and their values as applicable for the General Dynamics B-58 control circuit. (The same circuit is used on the Lockheed F-104.)



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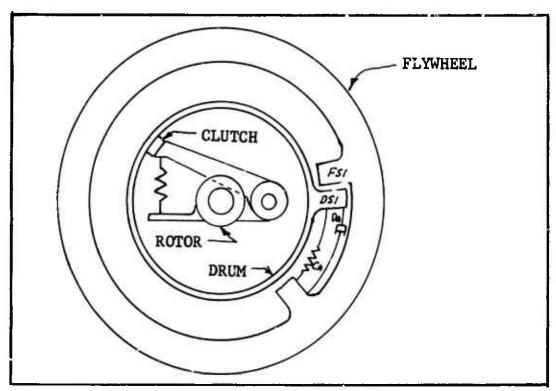
Electrical On-Off Circuit Equation Flow Diagram Figure 54

Table 20 On-Off Control System Parameters

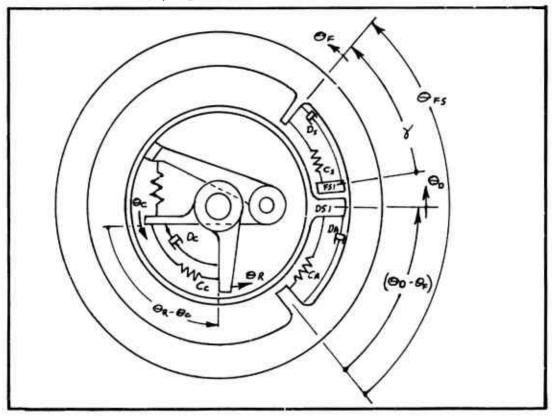
Description	Transistor Q1 Base Current	Current thru Capacitor Cl	Current thru Diode Dl	Current thru Resistor Rl	Current thru Resistor R4	Input Signal from Wheel Speed Sensor	Antiskid Valve Voltage	Voltage across Capacitor Cl	Voltage across Capacitor Cl at Time Zero	Capacitor Cl Voltage Change Rate	Supply Voltage	Skid Detection Threshold Current	(EG - VC1) Coefficient EQU V6	Constant EQU V6	Reciprocal of Capacitance Cl	(EG - VC1) Coefficient EQU Kl	Constant EQU R1	cient EQU	(EG-VC1) Coefficient EQU V4-1	Constant EQU V4-1	ABQ1 Coefficient EQU V4-1
Unite	Amps	Amps	Amps	Amps	Amps	Volts	Volts	Volts	Volts	Volts/Sec	Volts	Amps	Mhos	Amps	Volt/Amp Sec	Whos	Amps	Mhos	Mhos	Amps	Dimls
Value						. •			0		28.0	17.5×10-6	6.6×10-6	0.86x10-6	0.04 X 10+6	1667.0110-6	1000,0x10-6	19.35 × 10-6	7-01 x 191	96.8x10-6	0.000
Type	>	>	>	>	>	v(I)	(0)^	>	U	>	U	U	U	υ	U	υ	U	U	U	U	U
																			_		

Mechanical On-Off Antiskid Device

is a schematic drawing showing the operating Figure 55 principles of a commonly used mechanical on-off antiskid device of which the Hydroaire Hytrol Mk I and Dunlop Maxaret units are typical examples. The device operates as The rotor (the wheel speed indication element) is connected to the aircraft wheel by some positive means such as a direct connection or gear train, etc., so that the rotor's angular velocity is a constant ratio of aircraft wheel speed. During spinup the motion of the rotor is transmitted through the clutch to the drum. The clutch is configured such that it is self-energizing for rotation in the direction of wheel rotation associated with forward airplane motion, shown here as counterclockwise. Stop (DS1) on the drum engages stop (FS1) on the flywheel, thereby transmitting torque to cause the velocity of the flywheel to be the same as the drum. The flywheel and the drum are connected by spring (CA) and damper (DA). As the aircraft wheel and rotor decelerate, a clockwise torque is transmitted through the clutch to the drum and from the drum through spring (CA) and damper (DA) to the flywheel. amount of this torque is proportional to the product of the rotor's deceleration rate and the flywheel's inertia. torque compresses spring (CA) so that the flywheel moves counterclockwise with respect to the drum. For steady airplane wheel deceleration the amount of relative motion between the flywheel and drum is proportional to the deceleration rate. A suitable mechanism (usually a set of electrical contact points or a cam device) connected between the flywheel and drum causes a valve to be actuated so that brake pressure is relieved whenever a pre-established amount of relative motion occurs. The clutch is also configured so that when the torque from the rotor to the drum is clockwise, the torque capacity is limited to some slightly greater amount than that required to initiate brake release. If the rotor experiences greater deceleration than that required to initiate brake release, the clutch slips and allows the drum and flywheel to overrun the rotor. flywheel's inertia reacted by the drag of the clutch maintains a torque on spring (CA) so that the relative motion between the drum and flywheel (skid signal) is sustained until the flywheel's kinetic energy is dissipated or until the rotor has regained sufficient speed to eliminate clutch slippage. For this device the flywheel's inertia causing displacement of spring (CA) and damper (DA) is the



A. Functional Schematic



B. Mathematical Representation

Figure 55 Mechanical On-Off Antiskid Device

deceleration detector element, the clutch's overrunning drag torque on the drum is the reference adjustment element, the clutch is the wheel speed comparison element and the rotational kinetic energy of the flywheel is the wheel speed reference element.

A-2 Mechanical On-Off Mathematical Description

The mathematical description of the mechanical on-off antiskid device is developed by referring to figure 55(b) which defines the applicable parameters and shows flywheel stop (FS1) represented by a spring-damper system. Also, a spring-damper system is added between the rotor and clutch carrier to represent the small motion which actually occurs during clutch operation.

At flywheel stop (FS1) there is a torque, TS, which is exerted on the flywheel by the drum, if drum stop (DS1) is in contact with FS1. If the mass of FS1 is considered small in comparison to the stop spring (CS) and stop damper (DS) then, setting the sum of torques on FS1 at zero:

(6b-2-1)
$$Ts = Cs(x_0-x) - Ds\dot{x}$$

Where $Cs(Y_0-Y)$ is the stop spring torque, $(-Os\dot{Y})$ is the stop damper torque and Y_0 is the free length of spring CS.

Since TS results from a contact force, it cannot be less than zero; therefore, if $Y + (\Theta_0 - \Theta_F)$ is less than $\Theta_F S$ then TS = 0. Rewriting equation (1) solving for Y gives:

(6b-2-2)
$$\dot{y} = cs(x_0 - y) - Ts / Os$$

 γ is then established by:

 λ as computed from (6b-2-2) and (6b-2-3) is compared to $\Theta_{F5} - (\Theta_0 - \Theta_F)$ to establish TS. If TS is other than zero, it is computed from (6b-2-1) using $\chi = \Theta_{F5} - (\Theta_0 - \Theta_F)$ AND $\dot{\gamma}_z - (\dot{\Theta}_0 \cdot \dot{\Theta}_F)$.

Substituting the above expressions for \mathcal{X} and $\dot{\mathcal{X}}$ into (6b-2-1) gives:

(6b-2-1-1) TS = CS
$$\left[\frac{1}{3} - \Theta_{FS} + (\Theta_{D} - \Theta_{F}) \right] + 0.5 \left(\frac{1}{3} - \frac{1}{3} - \frac{1}{3} \right)$$

FOR $\left[\frac{1}{3} + (\Theta_{D} - \Theta_{F}) - \Theta_{FS} \right] \ge 0$

FOR $\left[\frac{1}{3} + (\Theta_{D} - \Theta_{F}) - \Theta_{FS} \right] \le 0$

Summing torques on the flywheel gives:

(6b-2-4)
$$\dot{\Theta}_F = \left[T_S + C_A(\Theta_0 - \Theta_E) + D_A(\dot{\Theta}_D - \dot{\Theta}_F) \right] / W_{FW}$$

Summing torques on the drum gives:

(6b-2-5)
$$\ddot{\Theta}_0 = [-T_S - C_A(\Theta_0 - \Theta_F) - D_A(\dot{\Theta}_0 - \dot{\Theta}_F) + 7c] / W_0$$

Where Tc is the clutch torque.

Subtracting (6b-2-4) from (6b-2-5) results in:

(6b-2-6)
$$(\ddot{\Theta}_0 - \ddot{\Theta}_F) = \left(\frac{1}{W_0} + \frac{1}{W_{FW}}\right) \left[-7s - C_A(\Theta_0 - \Theta_F) - D_A(\dot{\Theta}_n - \dot{\Theta}_F)\right] + 7c/W_0$$

By integrating (6b-2-6) twice, $(\circ \circ - \circ F)$ and $(\circ \circ - \circ F)$ are established as

(6b-2-7)
$$(\dot{\Theta}_0 - \dot{\Theta}_F) = \int (\ddot{\Theta}_0 - \ddot{\Theta}_F) dt$$

(6b-2-8)
$$(\Theta_0 - \Theta_F) = \int (\dot{\Theta}_0 - \dot{\Theta}_F) dt$$

Substituting values for $(\Theta_0 - \Theta_F)$ and $(\Theta_0 - \Theta_F)$ computed from (6b-2-7) and (6b-2-8) into equation (6b-2-4) and integrating once establishes Θ_F as follows:

$$(6b-2-9) \qquad \dot{\Theta}_F = \int \ddot{\Theta}_F dt$$

Combining the results from (6b-2-7) and (6b-2-9) establishes Θ_D as:

$$(6b-2-10) \qquad \dot{\Theta}_{D} = (\dot{\Theta}_{0} - \dot{\Theta}_{F}) + \dot{\Theta}_{F}$$

The clutch will now be examined.

The torque exerted on the clutch carrier by the rotor, T_c , is defined by:

(6b-2-11)
$$T_C = C_C (\Theta_R - \Theta_C) + D_C (\dot{\Theta}_R - \dot{\Theta}_C)$$

If, as for the flywheel stop, it is assumed that the clutch carrier inertia is negligibly small, the torque between the clutch and the drum equals the torque between the rotor and the clutch carrier. In this case equation (6b-2-11) may be solved for $(\Theta_R - \Theta_C)$ and by integrating once $(\Theta_R - \Theta_C)$ is obtained:

(6b-2-12)
$$(\Theta_R - \Theta_c) = \int (\dot{\Theta}_R - \dot{\Theta}_c) dt$$

Where $(\dot{\mathcal{G}}_R - \dot{\mathcal{G}}_c)$ is obtained from the following version of (6b-2-11)

$$(6b-2-11-1) \qquad (\cancel{O}_R - \cancel{O}_C) = \left[\mathsf{Tc} - \mathsf{Cc} \left(\cancel{O}_R - \cancel{O}_C \right) \right] / D_C$$

It follows that:

$$(6b-2-13) \qquad \dot{\Theta}_{c} = \dot{\Theta}_{R} - (\dot{\Theta}_{R} - \dot{\Theta}_{c})$$

If the clutch is configured so that there is no slipping for counterclockwise torque on the drum, Θ_c must equal Θ_0 and any difference between Θ_R and Θ_0 must be relative velocity between the clutch carrier and the rotor (i.e. $\Theta_c \cdot \Theta_c$). If Θ_0 is substituted for Θ_c in equation (6b-2-11) the the resulting equation can be used to compute the torque required to force Θ_c to be equal to Θ_0 . Therefore, making this substitution,

(6b-2-11-2)
$$T_{c} = C_{c} (\Theta_{R} - \Theta_{c}) + D_{c} (\Theta_{R} - \Theta_{n})$$

Equation (6b-2-11-2) adequately describes the component of clutch torque due to relative velocity; however, the component due to relative displacement is not satisfactorily described because the torque direction is independent of relative position. To compute the clutch torque for all conditions, equation (6b-2-11-2) will be modified and

a procedure for establishing the clutch condition will be defined. The clutch condition is established by the torque direction. The torque direction is determined by examining the direction the drum is attempting to move relative to the clutch. The direction of the drum's attempted movement relative to the clutch is established by comparing the drum velocity, Θ_{D} , to the velocity, Θ_{CH} , of a hypothetical or "index" clutch. The "index" clutch will be permitted to have slight slippage on the drum for counterclockwise torque so that there is a preceivable circumstance to indicate torque direction. To describe the "index" clutch motion relative to the rotor, equation (6b-2-11-1) is modified by substituting Θ_{CH} and Θ_{CH} for Θ_{C} and Θ_{C} as follows:

(6b-2-11-1M)
$$(\dot{\Theta}_R - \dot{\Theta}_{CH}) = \left[T_C - C_C (\Theta_R - \Theta_{CH}) \right] / D_C$$

The clutch torque, T_c , is defined by equation (6b-2-11-3). $(\Theta_R \cdot \Theta_{CH})$ is obtained from equation (6t-2-12) and Θ_{CH} is then established from equation (6b-2-13), noting that in each case Θ_{CH} and Θ_{CH} are used in place of Θ_C and Θ_C . The clutch condition is established by the difference between Θ_{CH} and Θ_C as follows:

For $(\dot{\Theta_{CH}} - \dot{\Theta_{D}}) > O$ Clutch torque is positive on the drum (clutch attempting to have positive velocity with respect to drum)

For $(\dot{\Theta_{CH}} - \dot{\Theta_{O}}) = O$ Clutch is not attempting to move relative to drum

For $(\Theta_{CH}^{\bullet} - \mathring{\Theta}_{D}) < \bigcirc$ Clutch torque is negative on the drum. (Drum is attempting to have positive velocity with respect to clutch).

Now that the clutch condition is defined, equation (6b-2-11-2) is modified so that the torque direction is established by the direction of relative velocity between the drum and the clutch as follows:

(6b-2-11-3)
$$T_{C} = G_{C} \langle \dot{g}_{ch} - \dot{g}_{o} \rangle | C_{C} \langle \dot{g}_{R} - \dot{g}_{ch} \rangle | + D_{C} \langle \dot{g}_{R} - \dot{g}_{o} \rangle | + D_{C} \langle \dot{g}_{R} -$$

The function $G_C \langle \dot{\Theta}_{CM} \cdot \dot{\Theta}_{o} \rangle$ is defined as follows:

(6b-2-14)
$$G_{c} \langle \dot{\Theta}_{CH} - \dot{\Theta}_{O} \rangle = +1.0$$
 FOR $(\dot{\Theta}_{CH} - \dot{\Theta}_{O}) > 0$

$$= 0 \quad \text{FOR} \quad (\dot{\Theta}_{CH} - \dot{\Theta}_{O}) = 0$$

$$= -1.0 \quad \text{FOR} \quad (\dot{\Theta}_{CH} - \dot{\Theta}_{O}) < 0$$

The constant C750 is the value of clutch drag torque when the drum is overrunning the clutch.

The amount of relative motion between the flywheel and drum $(\mathfrak{S}_{\mathfrak{g}} - \mathfrak{S}_{\mathcal{F}})$ is the skid signal. To be compatible with the electrical antiskid control circuits, assume the skid signal is produced by a set of electrical contact points; therefore,

(6b-2-15)
$$E_{V} = V_{S} \quad FOR \quad (\Theta_{O} - \Theta_{F}) \geq C751$$

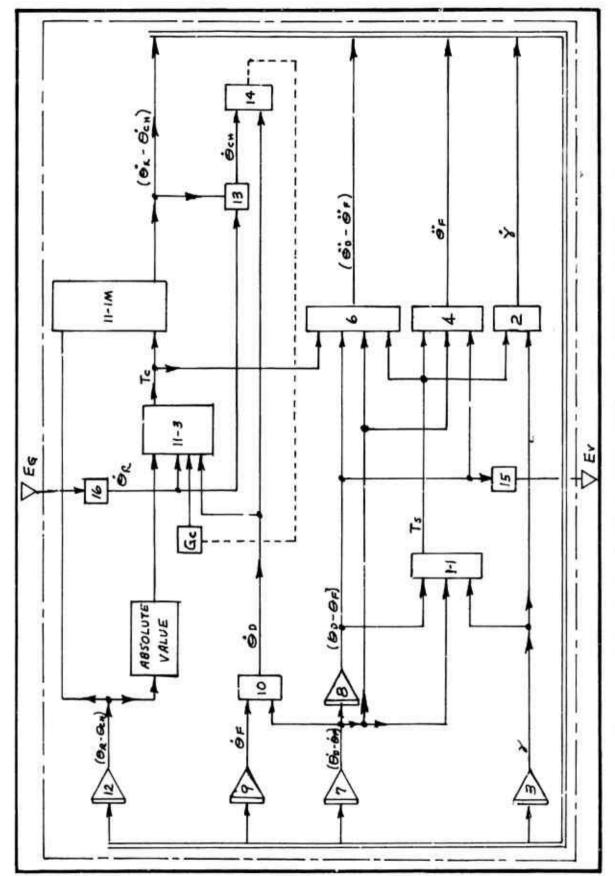
$$= O \quad FOR \quad (\Theta_{O} - \Theta_{F}) \leq C751$$

C751 is the skid detection threshold value of $(\Theta_0 - \Theta_F)$ Also, for compatibility with the other parts of the analysis, let the input be derived from the wheel speed sensor output, EG, as follows:

C752 is the conversion coefficient. The equation flow diagram for the mechanical on-off antiskid device is shown on Figure 56.

B-2 Mechanical On-Off Parameter Evaluation

No parameter evaluation has been accomplished for the mechanical on-off device because it is not applicable to the aircraft being considered.



Mechanical On-Off Device Equation Flow Diagram 98 Figure

7. ANTISKID CONTROL VALVE

Aircraft antiskid control systems typically utilize a twostage electrically operated pressure control valve. The first stage contains an electro-mechanical device such as a torque motor, solenoid or linear force motor which positions a hydraulic flow regulating element (flapper, nozzle or spool) such that a control pressure is produced. The control pressure is a function of the valve input pressure and the electrical input signal. The first stage control pressure is applied to the second stage hydraulic flow controlling power spool. The second stage spool is positioned by forces produced by the control pressure and valve output pressure in a manner such that output pressure is controlled in proportion to the first stage control pressure.

A. Mathematical Description

First Stage

The function of the first stage can be described mathematically by considering the control pressure producing element to be a single degree of freedom damped spring mass system as shown in Figure 57 acted upon by a force, F_{CV} , proportional to the electrical input signal.

$$(7.1) F_{cv} = C_{scv} E_{v}$$

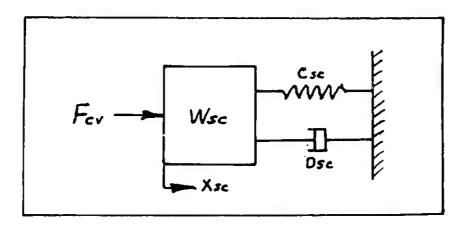


Figure 57 First Stage Spring Mass System

The first stage control pressure, Psc, is defined as a function of the mass position, Xsc, according to Figure 58. Xsc is established by equation (7.2) which results from summing forces on the first stage mass, Wsc.

(7.2)
$$Xsc = \frac{F_{cv}}{Wsc} - \frac{C_{sc}}{Wsc} Xsc - \frac{Osc}{Wsc} Xsc$$

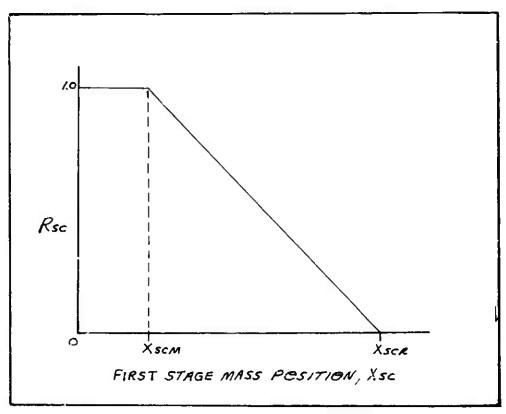


Figure 58 First Stage Control Pressure - Mass Position Relationship

(7.4)
$$Rsc = \begin{cases} 1.0 & \text{IF } Xsc \leq Xscm \\ \frac{XscR - Xsc}{XscR - Xscm} & \text{IF } Xscm \leq XscR \end{cases}$$

Second Stage

The physical arrangement of the F-111 antiskid valve second stage is shown schematically in Figure 59. Most other antiskid valves have the same operating principles.

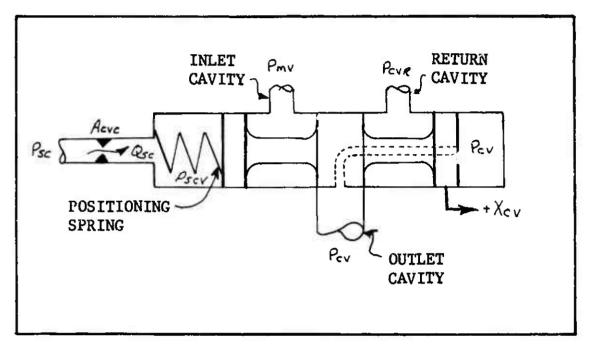


Figure 59 Antiskid Valve Second Stage

As described in the hydraulic system, the metering valve output pressure, P_{mv} , is supplied to the antiskid control valve second stage inlet. When the second stage spool is displaced in a positive direction a fluid passage opens permitting hydraulic flow from the metering valve to the antiskid valve outlet cavity. When the second stage spool is displaced in a negative direction a fluid passage opens permitting hydraulic flow from the outlet cavity to return. Therefore, the second stage spool position defines the hydraulic flow areas. The second stage spool position, Xcv , is escablished by equation (7.5) which results from summing forces on the spool mass, Wev. Figure 60 shows a schematic of a single degree of freedom damped spring mass system representing the antiskid valve second stage spool. Springs, Ccvs, and dampers, Ocvs, are stops representing the spool's longitudinal restraint caused by its contact with the valve body. The forces acting on the spool are the positioning spring force, damping force, stop spring and damper forces and forces due to outlet cavity pressure, ρ_{cv} , and control chamber pressure, P_{SCV} .

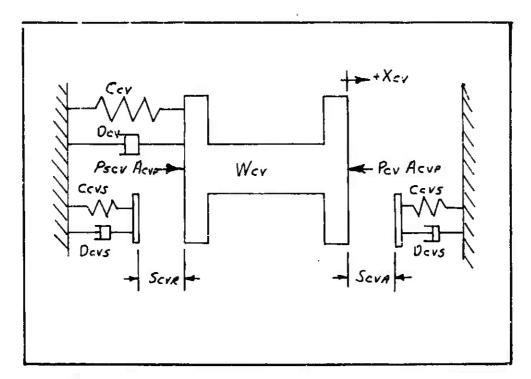


Figure 60 Second Stage Spool Forces

Summing forces on the second stage spool give:

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$$(7.5) \ \ddot{X}ev = (Psev - Pev) \frac{Aevp}{Wev} + (X.evp - Xev) \frac{Cev}{Wev} - \frac{Dev}{Wev} (Xev) + \frac{Fevsa}{Wev} + \frac{Fevsa}{Wev}$$

(7.6) FCVSR = O IF XCV ≥ -SEVR
=
$$\frac{Ccv}{Wcv} \left(-X_{CV} - S_{CVR}\right) - \frac{D_{CVS}}{W_{CV}} \left(\dot{X}_{CV}\right)$$
 IF $\dot{X}_{CV} \dot{X}_{CV} - S_{CVR}$

(7.7) Fousa = 0 IF Xev = Sova
=
$$\frac{Cevs}{Wev} \left(-Xev + Seva\right) - \frac{Qevs}{Wev} (Xev)$$
 IF Xev > Seva

The control chamber pressure, Psev, is established by the first stage control presure causing flow through the control orifice, Aeve, and the control chamber volume, Vsev, as follows:

The function $\phi < x, y$ is defined in the hydraulic system.

The hydraulic system contains provision for leakage flow associated with first stage pressure regulation and spool fit. Since these small flows have no effect on the valve's performance in the case under consideration, they have not been computed. Therefore, the following equations apply:

$$(7.12)$$
 Q cv2 = 0

$$(7.13) \qquad Q_{cV3} = 0$$

The Control Valve Equation Flow Diagram is shown on Figure 61

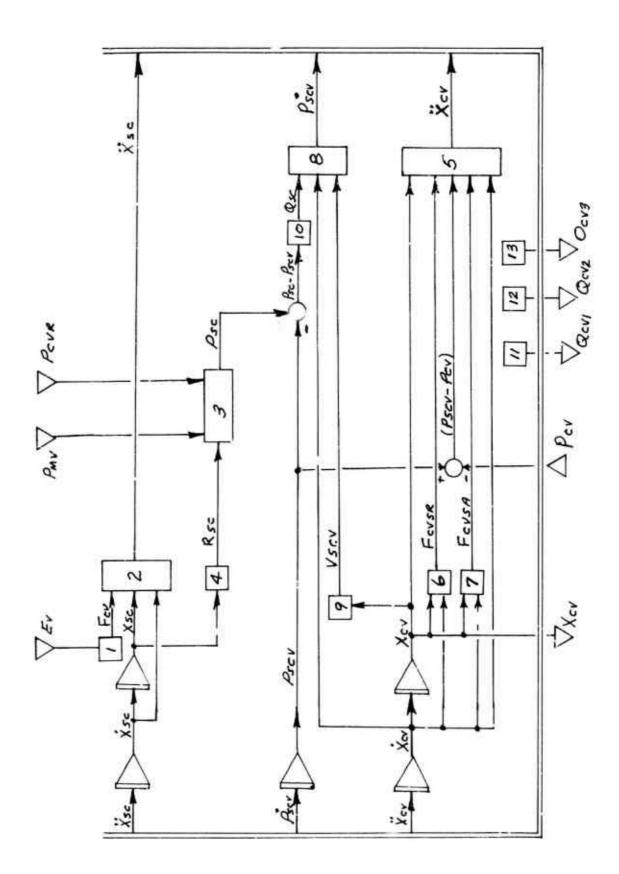


Figure 61 Antiskid Control Valve Equation Flow Diagram

B. Parameter Evaluation

The parameters used for describing the antiskid valve's first stage behavior are established from measured frequency response performance characteristics along with some features of its physical construction. Frequency response test results from the F-111 antiskid valve show 25 degrees phase lag at 5 cps. From various experiments it is known that the first stage accounts for most of the phase lag. The F-111 valve's approximate 700 cps undamped natural frequency is quite high compared to a more usual 100 cps value. Since antiskid operation is generally 10 cps or less and since the low frequency phase lag can be accurately described with a lower natural frequency system, an undamped natural frequency of 100 cps will be used to minimize computation difficulty.

Coefficients C_{SCV} and C_{SC} are set arbitrarily so that static values of X_{SCM} will be compatible with values of X_{SCM} and X_{SCM} (which are also arbitrarily chosen) and the proper valve voltage - output pressure relationship is achieved. In this example the following values are assigned:

For 100 cps (628 RAD/SEC) undamped natural frequency and $C_{SC} = 1.0 \, lbf/lW$, the mass W_{SC} is computed from $(W_{A})^{2} = C_{SC}/W_{SC}$

Using the equations relating natural frequency and phase angle listed in the wheel speed sensor parameter evaluation and assuming the first stage has 20 degrees phase lag at 5 cps, the damping factor is established as 3.63. For the values of W_{Sc} and C_{Sc} above this damping factor results in:

The area, A_{CVA} , the stop clearances, S_{CVA} and S_{CVA} , and the mass of the second stage spool, W_{CV} , are computed from the spool's physical dimensions as shown on the valve drawing.

Acrp =
$$0.05 \text{ in}^2$$

Wev = $41.5 \times 10^{-6} \text{ lbf sec}^2/\text{in}$
(7.17) Seva = 0.03 inch
Seva = 0.03 inch

The positioning spring rate, Cer, and spool damping coefficient were established based on the valve's transient response characteristic where it was observed that a 50 cps about .5 critically damped transient pressure oscillation appeared. From this observation

$$Cev = 4.0 \ lbf/lN$$
(7.18) $Dev = 13.0 \times 10^{-3} \ lbf see/lN$

The stop spring, Cevs, and damper, Devs, characteristics are arbitrarily chosen to be as high as possible within computation capability.

The control orifice area, Aevc, and control chamber length, Xevc, are established by the valves physical dimensions as shown on the valve drawing.

(7.20)
$$Acvc = 0.009 \text{ in}^2$$

 $Xcvc = 0.1 \text{ inch}$

The control chamber fluid bulk modulus is that of MIL-H-5606 hydraulic fluid as used in the hydraulic system.

The undeflected positioning spring length was computed assuming it produced approximately the same force on the valve spool as 25 PSI pressure differential.

$$(7.21) \qquad \chi_{CVP} = 0.2 \text{ INCH}$$

Table 21 lists the parameters and their values which are applicable to the F-111 and said control valve.

Table 21 Antiskid Control Valve Parameters

Table 21 (Contd)

DESCRIPTION	Second Stage Stop Clearance-Release Antiskid Valve Outlet Cavity Pressure Second Stage Control Chamber Volume First Stage Mass First Stage Mass Displacement First Stage Mass Velocity First Stage Mass Acceleration Second Stage Spool Displacement at Time = 0 Second Stage Spool Velocity Second Stage Spool Velocity Second Stage Spool Velocity Second Stage Spool Acceleration Second Stage Position for Undeflected Position Spring First Stage Mass Position for Zero Regulation First Stage Mass Position for Max Regulation	Flow Function
UNITS	1054 1054 1054 1054 1055 1054 1054 1054	
VALUE	0.03 41.5 x 10 -6 41.5 x 10 -6 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.	
TYPE	(H) A O O O O O O O O O O O O O O O O O O	+-
SYMBOL	Sover X X Sover X	Ø(x, x/>

8. HORIZONTAL TAIL CONTROL

In the 3 degree and 6 degree airplane models, the tail position can be controlled by two different means. The first is simply to require that the horizontal tail rotation be fixed at some value $S_{\rm HT}$. The second is to fix the input commands $S_{\rm EST}$ and $F_{\rm PX}$ and then let the stability augmentation system adjust the tail setting $S_{\rm HT}$.

A. Mathematical Description

Figure 62 shows a control system representation of the stability augmentation system.

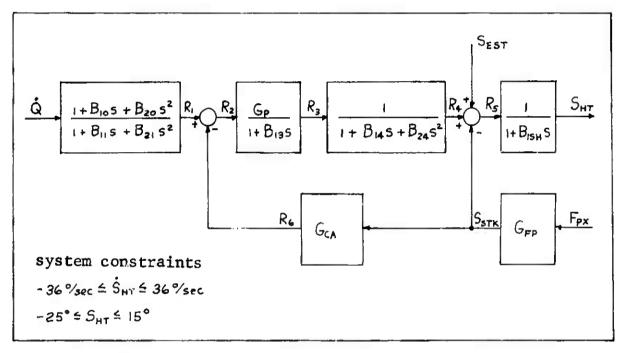


Figure 62 Stability Augmentation System

Using figure 62 as a guide, the following equations describe the stability augmentation system.

Where F_{PX} is the force exerted by the pilot on the stick.

Let Ua and Uaa be defined by

(8.3)
$$U_{\mathbf{Q}} = \left(\frac{180}{\pi}\right) \int \dot{\mathbf{Q}} dt$$

(8.4)
$$U_{QQ} = \int U_Q dt$$

Also, let U_{Ri} and U_{RRi} be defined by

$$(8.5) \ U_{Ri} = \int R_i \, dt$$

Then

$$(8.8) R_2 = R_1 - R_6$$

Let U_{R2} , U_{R3} , U_{RR3} , U_{R4} , and U_{RR4} be defined by

(8.9)
$$U_{R2} = \int R_2 dt$$

$$(8.10) \ U_{R3} = \int R_3 dt$$

$$(8.11) U_{RR3} = \int U_{R3} at$$

(8.12)
$$U_{R4} = \int R_4 dt$$

(8.13)
$$U_{RR4} = \int U_{R4} dt$$

Then

$$(8.14) R_3 = (G_P U_{RZ} - U_{RS}) / B_{13}$$

Because of rate and position limits, the equations that describe $S_{\rm HT}$ in terms of R_5 must be modified to reflect these limits. Let $S_{\rm HTP}$ be defined by

(8.17)
$$S_{HTP} = (R_S - S_{HT}) / B_{ISH}$$

Then

(8.18)
$$S_{HTI} = \begin{cases} S_{HTDMX} & \text{if } S_{HTP} > S_{HTDMX} \\ S_{HTP} & \text{if } -S_{HTDMX} \leq S_{HTP} \leq S_{HTDMX} \end{cases}$$
(8.19) $\dot{S}_{HT} = \begin{cases} \min\{0.0, S_{HTI}\} \text{ if } S_{HT} \geq S_{HTMAX} \\ S_{HTI} & \text{if } S_{HTMIN} \leq S_{HTMAX} \end{cases}$
(8.19) $\dot{S}_{HTI} = \begin{cases} \min\{0.0, S_{HTI}\} \text{ if } S_{HTMIN} \leq S_{HTMAX} \\ S_{HTI} & \text{if } S_{HTMIN} \leq S_{HTMIN} \end{cases}$

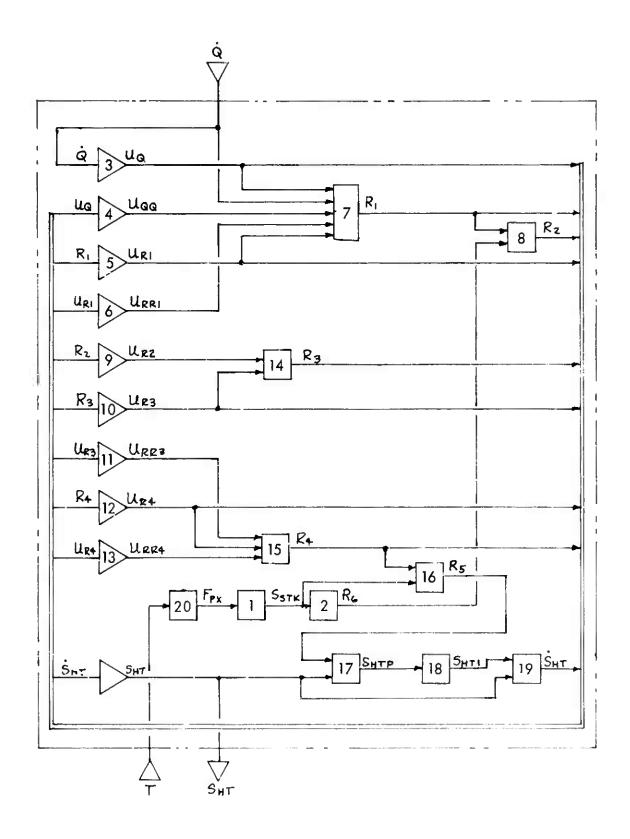
Finally the stick position F_{PX} may be positioned as a function of time by specifying two times and two loads.

(8.20)
$$F_{PX} = \begin{cases} 0 & \text{if } T_{PXZ} \leq T_{PX1} \\ F_{PX1} & \text{if } T \leq T_{PX1} < T_{PX2} \end{cases}$$

$$F_{PX2} & \text{if } T_{PX1} < T_{PX2} \leq T \\ F_{PX1} + (F_{PX2} - F_{PX1})(T - T_{PX1})/(T_{PX2} - T_{PX1}) \\ & \text{if } T_{PX1} < T < T_{PX2} \end{cases}$$

B. Parameter Evaluation

The values for the F-111A system parameters are listed in Tuble 22. In using this system for a braking problem the usual procedure is to first choose a steadystate value for $S_{HT}(S_{HTS})$. Set $S_{HTO} = S_{HSS} = S_{EST}$ and set $F_{PX} = 0$ ($T_{PX1} = T_{PX2} = 0$). Set all other initial conditions to zero.



在於**,我就被握了。我們**的說他,你可以完成一般的問題的。 我們們們

Figure 63 Horizontal Tail Control Equation Flow Diagram

Table 22 Horizonta! Tail Control Parameters

DESCRIPTION				SAS Constants					Stick Force	Determine Stick Force		Command Augmentation Gain	Stick Force Gain	Augmentation Gain	Airplane Pitch Rate			Intermediate SAS Variables				Series Trim Input
UNITS	sec	286	286	Sec	Sec	sec deg/ BAD	2,795	Sec 2	115	4	41	sec	de4/16	S & C: -1	RAD/sec	doy/sec	des / sec	dog/sec	der	290	de 3/50c	رددع
VALUE	4.	50.0	0.50	002e9	0.05	3,58	0.000555	0.00037		0.0	0.0	3.6	0.51	6.375							,	- 5.0
TYPE	υ	υ	O	υ	U	ο	υ	()	>	U	υ	υ	υ	()	v(1)	>	>	^	>	Þ	>	υ
SYMBOL	B,	 	<u>ج</u>	B.	BISH	Bzc	Bzi	B ₂₄	Y A	FPX;	FPX2	GCA	GFP	S.P.	···	אַ	R2	£3	R4	Rs	Pe	Sest

Table 22 (Contd)

THE SHARES CHARLES AND SHARES
SAS Variables and Initial Conditions DESCRIPTION Table 22 (Contd) deg sec deg sec deg sec deg sec deg sec deg sec UNITS VALUE 0,0 0.0 0,0 TYPE > 0 > 0 > 0 > 0 SYMBOL Kreto Kreto Kreto Kreto UR30 URR3 URR30

は、一般の記録があっている。

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This runway system is essentially the same as the runway system for the 6 degree. In fact, the relation between the two is given by $Z_{\rm GD}\langle\alpha\rangle=Z_{\rm GD}\langle\alpha\rangle$ and $Z_{\rm GDP}\langle\alpha\rangle=Z_{\rm GPP}\langle\alpha,o\rangle$. Even though this system is like the 6 degree system, the equations are listed below which take advantage of the fact that it takes less computer time to calculate $Z_{\rm GD}\langle\alpha\rangle$ than $Z_{\rm GP}\langle\alpha,o\rangle$. The data describing the runway is in tabular form and consists of runway elevation values as shown in table 24 as described in discussion of the 6 degree runway system. The data is from the center strip from station 4574 to station 6574.

A. Mathematical Description

Let $H_{RC}(i)$, $i=1,2,\cdots,1001$ denote the elevations at two foot intervals. As an example, $H_{RC}(s)=9.686$ If x is a distance measured down the runway where x is in inches, then $z=Z_{GD}(x)$ and $\omega=Z_{GDP}(x)$ correspond to the elevation in inches and the slope in inches per inch. The values for z and ω are determined as outlined below. The function Z_{GD} will have the property that $Z_{GD}(s)=0$.

Let X_{LRO} be a constant such that $o \le X_{LRO} < 2000$. The input X_{LRF} in feet is derived from x such that $o \le X_{LRF} < 2000$ and for some integer k

(9a.i)
$$X_{LRF} = X_{LRO} + \alpha/12 - 2000 k$$

Let n be an integer such that $2(n-1) \le X_{LRO} \le 2h$ and define Z_{GCO} by

If m is an integer such that $2(m-1) \le X_{LEF} \le 2m$ then \ge and ω are given by

Runway System Parameters (Flywheel and 3 Degree) Table 23

i i				
SYMBOL	TYPE	VALUE	UNITS	DESCRIPTION
H _{RC} (i)	C	六	Ft.	Center Runway Elevation Profile
3	(0) ^		uI/uI	Runway Slope at κ (ω = $\xi_{6DP}(\kappa)$)
×	(1) ^		In.	Distance Down Runway
XLRO	V	0.0	Ft.	Determines starting point (at time = 0)
				on Runway Profile
XLRF	>	****	Ft.	Determines position on runway profile
LN.	(0)		In.	Runway elevation at $lpha$
2,000	# V		평 t	Correction height

 \pm Determined from the constant X_{LRO}

See Table 24 of the 6 degree runway system (use center, sta. 4574 to 6574) <u>;</u><

9b. RUNWAY SYSTEM (6 DEGREE)

The runway system is not actually a "system" in the same sense as the brake system, for example. The runway system is simply a function called by the airplane system to supply values for ground slope and elevation. The data describing the runway is in tabular form and consists of runway elevation values as shown in Table 24. Except for a slight modification, the data in Table 24 is taken from station 4574 to station 6574 of runway 25 from reference 11. The left elevations and right elevations are 10 ft. to the left and 10 ft. to the right of center respectively. The elevations have been modified slightly so that the elevations at station 4574 match those as station 6574. This is done to provide an essentially "endless" runway by repeated use of a basic 2000 ft. strip.

A. Mathematical Description

Let $H_{RR}(i)$, $H_{RC}(i)$, $H_{RL}(i)$, $i=1,2,\cdots,1001$ denote the elevations at two foot increments of the right, center, and left runway strips respectively. As an example, $H_{RL}(ii)=9.550$ and $H_{RC}(5)=9.686$. If x is a distance measured down the runway, and y is a distance measured out from the center of the runway where x and y are in inches, then $z=Z_{GD}(x,y)$ and $\omega=Z_{GDP}(x,y)$ correspond to the elevation in inches and the slope in inches per inch. The values for z and ω are determined as outlined below. The function Z_{GD} will be chosen in such a way that $Z_{GD}(0,y)=0.0$ inches.

Let X_{LRF} and Y_{LRF} be the inputs in feet. Thus,

Let X_{LRO} be a constant such that $0 \le X_{LRO} < 2000$. X_{LRF} is a number such that $0 \le X_{LRF} < 2000$ and which also satisfies the following equation for some integer K.

(9c.2)
$$X_{LRF} = X_{LRO} + \chi/12 - 2000 K$$

Now let n be an integer such that $2(n-1) \le X_{LRO} \le 2n$. Define Z_{GRO} , Z_{GCO} , Z_{GLO} as follows:

Now let m be an integer such that $2(m-1) \le X_{LRF} \le 2m$ Define Z_{GEX} , Z_{GCX} , and Z_{GLX} as follows:

If $Y_{LEF} \ge 0$, then

$$(9c.11) = (Y_{LRF}/z0)(H_{RR}(m+1) - H_{RR}(m) - H_{RC}(m+1) + H_{RC}(m)) + \frac{1}{2}(H_{RC}(m+1) - H_{RC}(m))$$

If $Y_{LRF} < 0$, then

(9c.13)
$$\omega = (Y_{LRF}/20)(H_{RC}(m+1) - H_{RC}(m) - H_{RL}(m+1) + H_{RL}(m))$$

 $+ \frac{1}{2}(H_{RC}(m+1) - H_{RC}(m))$

Table 24 Three Track Elevation Profiles
(Stations and elevations are in feet)

STATION		ELEVATION	
	LEFT	CENTER	RIGHT
4574	9.597	9.703	9.593
4576	9.596	9.699	9.586
4578	9.593	9.696	9.581
4580	9.590	9.696	9.580
4582	9.590	9.686	9.580
4584	9.589	9.696	9.622
4586	9.580	9.688	9.629
4588	9.574	9.685	9.625
4590	9.570	9.686	9.616
4592	9.563	9.693	9.622
4594	9.564	9.704	9.634
4596	9.563	9.692	9.616
4598	9.556	9.676	9.611
4600	9.558	9.676	9.613
4602	9.592	9.694	9.612
4604	9.594	9.699	9.627
4606	9.595	9.711	9.641
4608	9.600	9.704	9.601
4610	9.604	9.703	9.605
4612	9.594	9.696	9.602
4614	9.585	9.697	9.606
4616	9.572	9.699	9.608
4618	9.569	9.702	9.607
	B 4 4 4 7 10 10 10 10 10 10 10 10 10 10 10 10 10		

Table 24 (Contd)

		Elevation			•	Elevation				Elevation	
Station	Left	Center	Right	Station	Left	Center	Right	Station	Left	Center	Right
4620	9.565	9.697	9.5)1	4760	9.557	9.667	9.567	4900	9.590	9. 716	9.603
4622 4624	9.572	9.658	9.631	4762	9.560	9.668	9.564 9.561	4902	9.593	9.714 9.717	9.582
4626	9.583	9.687	9.589	4766	9.565	9.676	9.568	4906	9 598	9.714	9.587
4628	9.583	9.693	9.57)	4769	9.557	. 9.676	9.567	4908	9. 591	9. 711	9.584
463F 4632	9.583 9.584	9.681	9.593	4773	9.563	9.564	9.564	4910	9.589	9.716 9.713	9.578
4634	9.591	9.699	9.514	4774	9.563	9.570	9,561	4914	9.592	9.712	9.581
4636	9.593	9.698	9.601	4776	- 9.565	9.675	9.561	4916	9.588	9.711	9.585
4638 4643	9.594	9,693	9.577	4778 4780	9.554	9.677	9.567	4919	9.587	9.710	9.592 9.585
4642	9.588	9.691	9.573	4782	9.557	9.678	9.575	4922	9.586	9.696	9.578
4644	9.586	5.687	9.589	4794	9. 552	9.683	9.574	4924	9.588	9.685	9.576
4646	9.593	9.668	9.533	4786 4788	9.554 9.57L	9.686	9.580 7.536	4926	9.585	9.695 9.731	9.572
4650	9.568	9.673	9.557	4797	9.572	9.763	9.587	4930	9.586	9. 702	9.573
4652 4554	9.573	9.659	9.569	4792	9.573	9.702	9.591	4932	9.590	9.711 9.707	9.571 9.568
4656	9.572	9.681	9.554	4796	9.582	9.703	9.597	4936	9.590	9.699	9.569
4553	9.555	3.665	9.557	4798	9.576	9.702	9.588	4938	9.590	9.692	9.567
4660	9.573	9.654	9.564	4877	9.557	9.697	9.590	4940		9.684	9.566
4662 4664	9.573	9.659	9.561	48C2	9.593	9.696	9.586	4942	9.583	7.687 9.688	9.573
4666	0.574	6.77.0	9,549	4806	9, 5,99	9.700	9.588	4946	9.582	7.682	9.562
4668	9.572	9.677	9.555	4858	9.593	9.698	9.585	+946	9.590	9.692	9.567
4670 4672	9.577	9.677	9.554	4812 4812	9.588	9.594	9.579 9.581	4953	9.576	9.679 9.678	9.569
4674	9.568	9.691	9.581	4314	9.531	9.698	9.583	4954	9.571	9.687	9.578
4675	9.571	9.685	9.597	4816	5.578	9.700	9.583	4956	9.575	9.682	9.579
4678 4680	9.577	9.697	9.595	4818 4820		9.693	9,579	4958 4950	9.581	9.689 7.686	9.585
4682	9.554	7.631	9.587	4322	9.534	9.679	9.574	4962		9.678	9.585
4674	9.564	9.630	9.587	4324	9. 589	9.676	9.574	4964	9.583	7.695	9.589
-689	9.535	9.632	9.535	4926	9.599	9.680	9.568 9.571	4966 4968	9.58n 9.576	9.699 9.709	9.588
459)	9.571	9-696	9-574	4832	9.593	9.609	9.574	4970	9.574	9.696	9. 585
4692	9.578	9.635	9,577	4932	9.575	9.584	9.581	4972	9.576	9.685	9.585
4694 4696	9.578	9.693	9.597	4834	9.596	9.593	9,585	4974	9.571	9.682	9.584
4678	9.555	9.713	9.676	4838	9, 590	9.698	9.599	4978	9.576	9.685	9.58)
4700	9,57)	9.694	9.571	4857	9.537	9.774	9.603	4989	9.573	9.679	9.583
4702 ·	9.567	9.696	9.670	4842	9.588	9.710	9.598	4982 4984	9.583	9.678	9.588
4706	9.571	9. 702	9.596	4846	9.590	9.591	9.577	4986	9.585	9.698	9.591
4708	9.57)	9.714	9.577	4849	9.591	9.689	9.596	4988	9.593	9.695	9.595
4710 4712	9.568	9.696	9.598	4850 4852	9.536	9.595	9.595	4990 4992	9.590	9.699	9.589
4714	9.562	9-695	9.575	4354	9.579	9.694	9.598	4994	9.593	9.69	9.592
4715	9.558	9.671	9.596	4956	5.585	9,693	9.595	4996	9.597	9.704	9.597
4718	9.567	9.638	9.591	4358	9.596	9.696	9.593	4998	9.598	9.709	9.590
4721 4722	9.562	9.691	9.573	4961 4952	9.598	9,694	9.587	5000		9.702	
4724	4.565	9.688	9.592	4864	5. 5 95	9.680	9.595	5004	9.608	7.703	9.610
4726	9.555	7.687	3.572	4966	9.535	9.583	9.632	5006		9. 724	9, 609
4728 4730	9.576	9.690	9.596	4968 497h	9.594	9,680	9.601 9.603	5008 5010		9.728	9,613
4732	9.582	5.690	9.604	4472	9, 590	9. 685		5012	9.509	9.721	9.614
4734	9.579	7.699	9.513	4974	.9.537	9.685	9.598	5014		9. 710	9.611
4736 4738	9.579	9.693	9.594	4876	9.571	9.677	9.596	5516 5018			9,604
4740	9.578	9.696	9.587	4331	9.593	9.573	9.594	5020	9.586	9.701	9.592
4742	9.575	9.674	9.587	4992	9.595	9.685	9.594	5022		9.691	9.583
4744	9.577	9.676	9.575	4884	9.599 5.610	9.698	9.595	5024 5026		9.682 9.666	9.580
4749	9.533	9.635	9.573	4389	9.632	9.599	9.596	5029		9.671	9.575
4750	9.587	9.670	9.571	489)	9.632	9.704	9.579	5030	9.581	9.572	9.576
4772	9.58? 9.581	9.630	9.573	4892	9.595	9.703	9.598 9.597	5032 5034		9.679	9.578
4756	9.583	7.673	9.574	4896	9,575	9.715	9.596	5036		9.692	9.585
475A	9.572	9.674	7.571	4393	9,596	9.715	9.593	5738		9.691	9.587
ليسيا				<u> </u>							

Table 24 (Contd)

		Elcvation				Elevation				Elevation	
Station	Left	Center	Rigit	Stati	Left	Center	Right	Station	Left	Center	Right
50-7	9.581	9.689	9.587	51.8		9,735	9.630	5320	9.65?	9.805	9.695
5042	7.587	9.686	9.582	.51.8		9.740	9.633	5322	9.658	9.810	9.692
5044	9.578	9.682	9.578	518		9.745	9.643	5324 5326	9.667	9.803	9.693
5048	9.572	9.680	9.573	518		9.756	9.640	5326	9.575	9.797	9.689
5050	9.571	9.683	9.567	519		9.750	9.637	5330	9.675	9. 803	9.690
5052 5054	9.575	9.684	9.568	519		9.757	9.641	5332	9.677	9.806	9.695
5056	9.583	9.655	9.588	519		9.75)	9.552	5336	9.686	9.811	9.702
5058	9.569	9.679	9.571	519		9.745	9.639	5338	9.689	9.823	9.702
5060 5052	9.588	9.702	9.593	520		9.741	9.633	5340 5342	9.683	9.812 9.811	9.704
5064	9. 577	9.686	9.553	520		9.758	9.648	5344	9.675	9.807	9.705
5066	9.558	9.679	9.579	-520	5 9. 619	9.759	9 . 655	5346	9.572	9.813	9.599
5068	9.569	9.663	9.555	523		9.767	9.5591	5348 5350	9.680	9.816	9.701 9.704
5970 5072	9.575	9.662	9.557	521		9,779	9.662	5352	9, 699	9. 810	9.704
5074	9.568	9.666	9.562	521		9.755	9.559	5354	9.705	9.813	9.766
5076	9.571	9.670	9.557	521		9.768	9.660	5356	9.710	9.011	9.708
5078 5382	9.569	9.675	9.555	521		9.773	9.557	5350 5360	9.714	9.817	9.707
5082	9.565	9.690	9.553	522		9.765	9.659	5362	9.699	9.813	9.700
5084	9.559	9.697	9.570	522		9.761	9.648	5364	9.697	9.804	9.70)
5088	9.566	9.685	9.565	522		9.766	9.652	5366 5358	9.697	9.808 9.802	9.701
5090	9.553	9.664	9.556	523		9.756	9.657	5370	9.708	9.797	9.706
5092	9.565	9.663	9.557	1 523	2 . 9-634	9.176	9.001	5572	9.713	9.799	9.706
5094 5096	9.565	9.674	9.557	523		9.777	9.661	5374 5376	9.719 9.731	9.811	9.705
5095	9.552	9.678	9.557	523		9,777	9.659	5378	9.737	9.835	9.715
5100	9.565	9.694	9. 574	524		9.778	9.550	5380	9.744	9.832	9.721
5172	9.555	7.702	9.576	524		9.775	9.668	5382	9.746	9.833	9.722
5104	9.565	9.736	9.577	524		9.779 9.780	9.675	5384 5386	9.751	9.835	9.732
5108	9.569	9.712	9.575	524		9.779	9.689	5388	9.764	9.852	9.729
5110	9.564	5.699	9.582	525		9.780	9.695	53 90	9.768	9.850	9.733
5112 5114	9.571	9.697	9.577	525		9.771 9.783	9.697	5392 5394	9.769	9.854	9.735
5116	9.554	9.658	9.577	525		9.783	9, 703	5396	9. 780	9. 862	9.731
5118	9.561	9.639	9. 575	525	9.657	9.797	9,725	5398	9.781	9.865	9.738
5127	9.552	9.676	9.557	526 526		9.793	9.714	5400 5402	9.777	9.871 9.860	9.737
5124	9.544	9.676	9.570	526		9.782	9.708	5404	9.777	9.670	9.743
512e j	7. 734	9.077	9.571	525		9.784	9,705	5406	9.783	9.962	9.742
5128	9.537	9.672 9.657	9.567	526 527		9.786	9.692	5498 5410	9.787	9.858	9.745
5130 5132	9.547	9. 667	9.567	527		9.785	9.683	5412	9.705	9.865	9.760
5134	9.549	9.657	9.558	527	9,655	9.782	9.681	5414	9.786	9. 864	9. 763
5136 5138	9.539	9.661 9.652	9.561	527		9.709 9.700	9.575	5416 5418	9.783	9.871 9.873	9.763
514C	9.542	9.653	5.569	527 528		9.778	9.562	5420	9.775	9.877	9.760
5142	9.545	9.651	7.557	528			9.662	5422	9.780	9.883	9.766
5144	9.548	9.664	9.555	529		9.757	9.557	5424 5426	9.787	9.880 9.872	9.773
5146 5148	9.552	9.678	9.573	528		9.775	9.557	5428	9.785	9.869	9.777
5157	9.552	9.675	9.573	529	9. 539	9,773	9.667	5430	9.787	9.862	9.784
5152	9.565	9.664	9.579	529		9.775	9.666	5432	9.790	9.857	9. 786
5154 5156	9.565	9.674	9.573	529		9.780 9.793	9,666	5434 5436	9.797	9.875 9.887	9.793
5158	9.590	9.705	9.590	529	9.652	9.601	9.557	5438	9.795	9.883	9.792
5160	9.579	9.715	9.5)1	533		9.801	9.674	5440	9.787	9.882	9. 787
5162 5164	9.589	9.718 9.723	9.674	530 530		9.805 9.808	9.587	5442	9.786	9.887	9.785 9.783
5166	9.598	9.719	9.513	530		9.836	9.685	5446	9.777	9.876	9.774
5155	9.632	9.723	9.617	539	9.657	9,803	9.691	5448	9.785	9.866	9.773
5170 5172	9.671	9.735	9.623	531		9.501	9.664	5450 5452	9.791	9.865	9.767
51.74	9.592	9.738	9.527	531		9.808	9.701	5454	9.770	9. 855	9.763
5176	9.592	9.732	9.633	531	9, 655	. 9.907	9.730	5455	9.771	7.856	9.767
5179	9.597	9.734	9.534	531	9.667	9.805	9. 702	5453	9.772	4, 020	9.767
				لنتلل		4.51	أستنست	L1		i	

Table 24 (Contd)

2000		Elevation		-			Klevation		-	Station		Elevation	
Station	Left	Center	Right		Station	Left	Center	Right		26461011	Left	Center	Right
5463 5462	9.777	9.861	9.753 9.789		5633 5632	9.838	9.917	9.862 9.351		5740 5742	9.964	17.058	9.944
9454	4.768	9.859	9.787		5604	9.831	9,921	9.862		5744	9.964	10.056	9.945
5466	9. 767	9.858	9.791	1	55.76	9.831	9.931	9.966		5746	9.962	10.049	9.946
5468	9.769	9.832	9.788		560,8	_9. 836	9.937	9. 376		5749	9.970	10.056	9.959
5470	9.785	9.886	9.792		551)	9.828.	9.936	9.875		5750	9.972	10.064	9, 966
5472 5474	9.871	9.893	9.9))	1	5612 5514	9.827	9.926 9.939	9.874		5752 5754	9.972	10.089	9.974
5476	9.873	9,910	9.797		5616	9.828	9.945	9.979	'	5756	9.966	13.092	9.981
5478	9.814	9.896	9.735		5618	9.829	9.953	9.876		5758	9.974	10.091	9.983
5480	9.813	9.915	9.799	- 1	.5627	9.837	9.95?	9.997		5760	9.982	17.098	9.985
5492	9.811	9,929	9.803		5622	9.841	9.956	9. 884		5762	9.980	10.101	9.982
5484 5486	9,812	9.927	9.866		5624	9.846	9,953	9.991 9.879		5764 5766	9.976	10.097	9.985
5488	9.818	9.922	9. 8:37		5628	9.846	9.973	9.384		5768	9.979	10.100	9.976
5491	9.815	9.977	9.807		56 30	9.843	9, 972	9.887		5770	9.978	10.087	9.975
5492	9.807	9.931	9,801		5532	9.849	9.978	9.893		5772	9.967	10.094	9.976
5494	9.817	9.920	9.793		5634	5.850	9. 977	9.896		5774	9.970	10.087	9.975
5496	9. 793	9,919	9.78?	-	5535	9.859	9.979	9.906		5776	9. 970	10.092	9.974
5498 5500	9.792	9,978	9.776		5638 5640	9.860	9.985	9.909		5778 5780	9.967	10.097	9.975
5502	9.797	9.903	9.771		5642	9.864	9.999	9,916		5782	9.963	13.089	9.976
5504	9.800	9.935	9.775		5644	9.862	10.006	9.927		5784	9.957	10.084	9.976
556	9.797	9.904	5.779		5646	9. 85 7	10.008	9.929		5786	9.943	10.077	9.977
95C8	9.799	9.905	9.794		55 48	9.862	10.011	9.936		5788	9.934	10.067	9.979
5510	9.799	9,906	9.788		5650	9.873	10.317	9.945		5790 5792	9.930	10.067	9.983
5512 5514	9.802	9.902	9.735		5652 5654	9.883	10.021	9.752		5794	9.927	10.064	9.982
5516	9.831	9,903	9.795		\$655	9,897	10.041	9, 955		5796	9.915	10.066	9.978
5518	9. 803	9.932	9. 790		5558	9.913	13,343	9,756	ľ	5798	9.912	10.074	9, 975
5527	9.873	9.974	9.795		5667	9,907	10.039	9.956		5800	9.910	10.071	9.975
5522	9.802	9.892	9.870		5562	2,912	13.239	9,954		5802	9.913	10.073	9.984
5524 5526	9.801	9.970 9.974	9.803		.5664 5655	9.916	10.046	9.949		5804 5806	9.925	10.091	9.987
5528	9.877	9.839	9.807		5668	9. 911	10.033	9.942		5909	9.933	17.105	10.001
5530	9.797	9.897	9.915		5570	9.913	19.333	9,939		5810	9.942	10.131	10.002
5532	9.797	9.974	9.824		5672	9.916	10.020	9.932		5812	9.947	10.125	9.994
5534	9.799	9.913	9.327		55.74	_9,914_	10.028	9.926		5914	9. 763	10.123	9.991
5536 5538	9.878	9.909	9.826 9.827		.5676 5578	9.926	30.037 13.044	9,929	·	5916 5818	9.965	10.108	9.984
5542	9.817	9.933	9.827		5080	3. 926	10.047	9.944		5820	9.970	17.134	9.985
5542	9.025	9. :37	9.929		55 92	9.923	10.357	9,950		5822	9.975	10.101	9.985
2244	9.023	7.733	2.035		5584	2.774	10,042	9.949		5824	9.970	13.395	9.986
5546	9.823	9.927	9.935		5585	9,933	13.752	9.949		5876	9.967	10.091	9.987
5548 5550	9.828	9.938	9.839		5688 5691	9, 930 9,923	10.052	9.951 9.954		5828 5830	9.961	10.095	9.999
5552	9.820	9.930	9.843	٠	5692	9.936	10 .055	9. 952		5832	9.963	13.137	10.004
5554	9.82?	9.933	9.547	. !	5694	9.947	10.053	9,949	- 1	5834	9.960	10.118	10.015
5556	9.821	9. 922	9. 850		5696	_,9,944	10.743	7.742		5836	9.959	10.121	10.014
5558	9.82?	9.930	9.954		5698	9,939	10.028	9.937		5838	9.963	10.115	10.013
5567 5562	9.829	9.947	9.860 9.855		5700	9.939	10,032	9.929		5840 5842	9.960	10.111	10.017
5564	9. 847	9.956	9.858		5704	9.917	10.024	9.925		5844	9.963		10.009
5556	9.85)	9.947	9.862	_]	5706	9, 913	10.030	. 9. 932		5846	9.957	10.115	10.004
5568	9.849	9.947	9.861		5708	_ 9 ,921.		. 9.936	-	5848	9.964		10.000
5573	9.845	9.961	9.860		5710	9, 929		9.943	ı	5850	9 977		9.995
5572 5574	9.836 9.841	9.948	9.855	٠.	5712 5714	9.731 9.929	12.3 <u>44.</u> .10.044	9.947	•]	5852 5854	9.990		9.995
5576	9. 841	9.962	9. 178	1	5715	9.735	10.052	9,952	ı	5855	9.991	19.105	9.993
5578	9.843	9.963	9.877	. 1	5718	9, 933	10.955	9.954	. 1	5858	9.988	10.105	9.994
5585	9.945	9.963	9.979		5723	9.934	10.756	9.953	Ì	5860	9.987	10.100	10.003
5582	9.840	5.970	9.875		5722	9.939	10.048	7.742	ļ	5862	9.939	1).095	10.203
5584 5586	9.839 9.841	9.953	9.374		5724 5726	9.938	10.750	9.949	- {	5864 5866	9.983	10.091	9.999
55R8	9.843	9.954	9.861		5729	9.945	10.049	9.956	-	5868	9.962	10.088	9.992
5590	9. 835	9.943	9.961	-	573)	9.943	13.754	9.955	- 1	5870	9.957	13.081	9.985
5592	9.836	9.934	9.862		5732	9. 950	10.053	9.956	1	5872	9.952	10.088	9.979
5594	9. 534	9. 937	9.862		5734	9.95)	12.743	9.949	-	5874	9.950	10.073	9.976
5575	9.833	9.911	9.565		5736	9,959	10.041	9.943	į	5976	9.343	10.064	3,373
5598	9.833	9.916	9.857		5739	9.956	10.347	9.939	ì	5573	9.947	10.051	9.955
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Table 24 (Contd)

		Elevation				Elevation				Elevation	
Station	Left	Center	Right	Etation	Left	Center	Right	Station	Left	Center	Right
5882	9.945	10.055	9.957	60 20	9.967	10.082	9.979	6160	9.937	10.079	10.011
5882	9.943	10.041	9.954	60.22	9.954	10.083	9,975	6152	9.937	10.086	10.012
5884	9.947	13.025	9.947	6026	9.953	10.386	9.975	6166	9.940	10.096	10.015
5988	9.915	12.028	9.952	6728	9.957	10.076	9.971	6168	9.940	10.093	10.014
5890	9.952	10.021	9.957	5337	9.960	10.385	9.973	6170	9.938	10.096	10.019
5892 5894	9.957	10.038	9.957	5732 5734	9.953	10.396	9, 972	6172	9.943	10.076	9.993 10.006
5396	9.953	17.065	9.994	6036	9.973	10.296	9.964	6176	9.942	10.080	10.705
5898	9.971	12.071	10.000	6733	9.973	13.293	9.960	6178	9.939	10.079	10.002
5900	9.978	10.075	10.776	6040	9.973	10.089	9.959	6180	9.942	13.070 19.062	9.999
5902	9.993	10.072	10.009	5742 6044	9.976	10.287	9.955	6184	3.942	17.059	9.995
590 6	12.029	17.089	13.337	67.46	9.973	10.088	9.955	6186	9.955	10.063	9.995
5908	10.017	10.102	10-003	6048	9.973	10.084	9.951	6188	9.946	13.057	9.986
5913 5912	10.032	13.112	9.997	6757	9.972	10.094 10.773	9.946 9.346	6190	9.943	13.065 13.062	9.985 9.973
5914	17 939	10.117	10.774	6054	9.931	10.082	9.946	6194	9.936	19.049	9.962
5916	10.038	17.116	10.718	6355	9.792	10.089	9.951	6196	9.930	10.048	9.955
5918	10.040	10.119	10.010	60.58	9.938	10.093	9.949	6198	9.929	10.059	9.954
5920	10.041 10.038	17.119	10.775	6763 6062	9.950	10.797	9.952	62.02	9.929	10.081	9.955
5924	10.030	13.123	13.132	5364	9.979	10.091	9.942	6204	9.922	10.075	9.949
5926	10.013	10.113	9. 998	6066	9.970	10.093	9.343	6206	9.914	10.071	9.946
5929 593r	9.934	13.105	10.000	6069	9.970	10.062	9.942	6209	9.912	10.061	9.945
5932	9 970	13.110	13.034	6072	9.976	10.083	9.963	6212	9.897	10.060	9.953
5934	9.997	10.098	10.330	5774	9.977	10.786	9.968	6214	9.894	10.058	9.949
5936	9.987	10.134	9.937	6076	9. 993	10.088	9.973	6216	9.887	13.362	9.949
5938 5940	9.983	13.098	9.93)	6080	9.993	10.123	9.981	6218	9.889	10.061	9.941
5942	2.983	13.091	9.935	6782	9.933	10.108	9.986	6222	9.885	10.068	9.935
5944	9.983	10.099	9. 930	6P84	9.937	10.795	9.795	6224	9.880	10.061	9.929
5945	9.976	13.098	9.975	6186	9.970	10.089	9.996	6226	9.877	10.055	9.925
5948	9.982	10.092	9.984	6097	9. 993	10.083	9.996	6230	9.867	10.061	9.914
5952	10.023	17.995	9.987	5792	9.977	10.796	9.996	6232	9.869	10.055	9.912
5954	13.338	13.171	9.992	61.94	9.976	10.089	9.991	6234	9.853	13.243	9.915
5956 5958	10.019	12.125	9.937	6395 6098	9.955	13.192	9.982	6236	9.850 9.846	10.044 13.041	9.922
5961	in 023	10.135	12.227	61 27	9.353	13.385	9.986	6240	9.841	12.031	9.719
5962	10.000	10.138	10.062	61/12	9.956	10.076	9.988	6242	9.844	10.021	9.915
5964	9.995	13.128	9.937	6104	9.941	10.081	9.998	6244	9.854	10.015	9.909
5966	9.994	10.115	9.988	6106	9.957	10.779	9.987	6248	9.843	9.997	9.397
5970	9.987	16.100	9.977	6119	9.952	10.074	9.938	6250	9.844	16.009	9.898
5972	9.997	10.094	9.374	6112	9.946	10.072	9.985	6252	9.840	10.018	9.395
5974 5976	9.984	13.097	9.958	6116	9.944	10.077	9.732	6254	9.836	10.013	9.899
5978	9. 991	17.095	9.954	6119	9.941	12.271	9.977	6258	9.827	10.013	9.899
5980	9.993	10.098	9.95%	4120	9. 941	10.079	9.975	6257	9.827	13.301	9.891
5982	9.972	13.095	9.35)	6122	9.938	10.063	9,963	6262	9.821	10.004	9.886
5984	9.997	10.090	9.947	6124	9.938	10.074	9.968	6266	9.821 9.82 6	9.983	9.833
5988		10.094	9.957	6128	9, 947	10.273	9.772	6269	9.828	9.958	9.881
5993	9.994	10.003	9.963	6130	9.936	10.072	9,977	6270	9.830	9.963	9.982
5992	9. 983	10.783	9.957	6132	9.933	17.376	9.974	6272	9.830	9.964	9.881 9.879
5994 5996	9.975	10.038	9.966	6134	9.937	13.777	9.769	62 .,	9.832	9.978	9.884
5998	9.975	10.086	9.965	6139	9. 940	10.076	9.767	6278	9.933	7.994	9.495
6000	9.977	13.075	9.754	6147	9.934	10.061	9.970	6281	9.827	9. 994	9.585
6004	9,960	17.071	9.959	6142	9.935	10.066	9.971	6282	9.823	9.974	9,993
6004	9.945	10.073	9.965	6146	9.933	10.057	9.777	6286	9.824	9.967	9.990
6008	9.95)	10.071	9.958	6149	9.936	10.066	9. 981	6288	9.823	9.958	9.882
6010	9.956	10.068	9.977	6157	9.932	13.374	9.987	6290	9.820	9.949	9.379
6012 6014	9.955	13.077	9.931	6152	9.930	10.069	9.996	6294	9.815 9.806	9.957	9,871
6°16	9.967	10.083	9. 937	6156	9.93?	10.382	13.335	6296	9.937	3.9,5	9.155
6018	9.955	10.070	0.795	6155	9.936	17.071	10.114	6298	9.919	9, 941	9, 453
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Table 24 (Contd)

Station		Elevation	-	Station		Elevation		Station		Elevation	
SCRCTON	Left	Center	Right	Station	- Left -	Center	Right -	Station	Left	Center	Right
6300	9.818	9.937	9.852	6392	9.754	9.864	9,779	6484	9.651	9. 752	9.657
6302	9.817	9.935	9.853	6394	9.743	9.856	9.775	6486	9.651	9.755	9.657
6374	9.822	9.937	9.849	6396	9.727	9.853	9. 772	6488	9.648	1 9.751	9.549
6306	9. 815	9.934	9.355	6398	9.723	9 . 8 46	9.755	6490	9.643	9.737	9. 645
6308	9.811	9.928	9.852	6490	9.719	9 . 8 54	9,701	_6497.	9,641	9.734	9.539
6310	9.839	9.931	9.851	6472	9.716	9.849	9.730	5494	_9.636	9.730	9.637
6312	9.807	9.936	9.847	6404	9.721	9.855	9,779	. 5196.	9.636	9 - 7.32	.9.540
6314	9.836	9,937	9.845	6406	9.727	9 . 8 54	9.730	6498	.9.635	9.730	9.643
6316	9.803	9.939	9-843	6408	9.734	9.846	9.734	65 77	9.637	9.734	9.637
6318	9.795	9.943	9.841	6410	9.744	9.849	9-,787	6502	9.641	9,736	9.635
6320	9.794	9.944	9.835	6412	9.753	9.850	9.735	6534	9.642	9.738	9.641
6322	9.739	9.949	9.822	6414	9.753	9.855	9. 776	65.06	. 9.640	.9.736	9.542
6324	9.784	5-947	9.829	6415	9.757	9 . 8 56	9.774	6508	9.641	9.739	9.641
6326	9.781	9.948	9.830	6418	9.759	9.858	9. 73	6510	9.640	9.737	9.539
6328	9.783	9.949	9.932	6420	9.758	9.862	9.773	6512	9.638	9.739	9.637
6330	9.782	9.941	_ 9. 833.	6422	9.755	9.859	9.773	6514	9.639	9.735	9.539
6332	9.783	9.944	9.832	6424	9.752	9.861	9.765	6516	9.637	9.735	9,637
6334	9.786	9.938	9.834	6426	9.754	9.862	. 9.753	6518	9.634	9.733	9.535
6336	9.787	9.956	9-842	6428	9.751	S. 6 26	9. 760	5572	9.633	9.736	9,638
6338	9.794	9.956	9-841	6431	9.744	9.859	9.755	6522	9.527	9,740	9.537
634)	9.796	9.950	9.839	6432	9.739	9.852	9.751	65.24	9,626	9,733	9.634
6342	9.793	9-954	9.835	6434	9.732	9.847	9.743	5525	9.62)	9.731	9.630
6344	9.792	9.934	9.834	6436	9-729	9-834	9.733	85 25	9, 620	9.727	9.625
6346	9.734	9.938	9.827	6438	9.724	9 • 9 33	9.724	6532	9.612	9.721	9.620
6348	9.793	9.923	9.826	6440	9.721	9-831	9.720	6532	9.608	9.713	9.616
635)	9.784	9.931	9.825	54.42	9.71.7	9.827	9-720	6534	9.610	9.704	9.609
6352	9.783	9.921	9.825	6444	_5,716	9.826	.9.714	65.36	9.607	9,702	9.574
6354	9.787	9.929	0.820	6845	9.716.	9.822	9.713	_6538	9,632	9.713	9.597
6356	9. 779	9.924	9.812	6443	94.717	9.822	9.707	.6543	_9.597	9.595	9.594
6359	9.782	9.914	9-874	6457	9.720	9.821	9.711	6542	9,599	9,701	9.595
6360	9.786	9-927	9-804	6452	9-721	9.827	9-713	6544	9.537	9.698	9.572
6362	9.790	9.910	9.798	6454	9.718	9,834	9.714	6546	S- 674	9,696	9.591
6364	9.794	9-909	9.737	6456	_ 9• <u>7</u> 21	9.831	9.719	6543	9.672	9.699	9.593
6366	9.797	9.917	9.786	6458	9,721	9,830	9- 720	5550	9.593	9,702	9,530
6368	9.795	9.9.2	9.786	6457	9720	_9.824	9.720	.65 52	9,588	9.706	9.604
6370	9.794	9.914	9. 765	6462	9.724	9.829	9.711	4554	9.538	9,592	9.575
6372	9.794	9 -0 76	9.754	5454	9.718	9.827	9.711	6556	9.590	9.704	9. 005
3374	9.793	9.195	9. 786	6466	9.727	9,817	9.710	6553	9.531	9.707	9.533
6376	9-787	9.904	9.733	6463	9 - 6.28	.9.812	9.704	6560	9.588	9,708	9.501
6378	9.782	9.898	9.791	6473	9.693	_9.808	9.596	5552	9.539	9.704	9.594
6383	9.79)	9.908	9.788	64.72	9.693	9.811	9.683	6564	9. 591	9.693	9.587
6382	9-778	9.99)	.9-734	6474	9.682	9.799	9.532	6566	_9.59 <u>n</u>	9.695	9.585
6354	9.776	9.901	9.785	6476	5.680	.9.786	9-681	6568	9.590	9-596	9.599
6386	9.774	9.888	9.784	6473	9,677	9.777	9.680	657)	9-591	9-702	9. 594
											9.593
6388	9.773	9.884	9.779	6487 5492	9,653	9.766 9.758	9.673	6572	9.597	9.701 9.703	

Table 25 Runway System Parameters (6 Degree)

文章,张文文文文文章,文文文文文章,中文文文文章,《文文文文文》,《文文文文文》,《文文文文文》,《文文文文文》,《文文文文文》,《文文文文文》,《文文文文文》

DESCRIPTION	Center runway elevation profile Left runway elevation profile Right runway elevation profile Runway slope at coordinate (χ, γ) Distance down the runway Determines starting point (at time = 0) on runway profile Determines position on runway profile Distance from runway ξ ., Inches Distance from runway ξ ., Feet Runway elevation at coordinate (χ, γ) Center profile height at time = 0 Left profile height Left profile height Right profile height
UNITS	Ft Ft In/In In/In Ft In Ft Ft Ft
VALUE	*** 0 + + +
TYPE	
SYMBOL	HRC (i) HRL (i) HRC (i) K K K K K K K K K K K K K

Use station 4574 to 6574. and Hgg. * See Table 24 for values of HRC, HRL

 \pm Determined from the constant \times

* This input allows starting the airplane on a different part of the runway profile even though its distance down the runway is the same.

SECTION IV

TOTAL SYSTEM ANALYSIS

Three different total system mathematical models have been formulated to perform antiskid analysis. The first model which is referred to as the flywheel system represents an antiskid system installed on a wheel and brake which are mounted on a dynamometer. The second system. referred to as the three degree system, represents an antiskid system installed on a wheel and brake mounted on a rigid airplane which is allowed three degrees of freedom (longitudinal translation down the runway, translation vertically, and pitch rotation). The third system, referred to as the six degree system, represents a rigid airplane having all six degrees of freedom and equipped with a conventional single wheeled main landing gear incorporating independent antiskid control of each brake. All of these systems are created utilizing the models described in Section III. The basic reason for utilizing three models is economics. The six degree system takes at least twice as long to run as the flywheel system and not all antiskid system parameters require the sophistication of the six degree system. However, it might be necessary to check certain effects under the most comprehensive circumstances.

The "Basic Control System" is made of the following models as described in Section III:

- 1. Brake System
- 2. Hydraulic System
- 3. Wheel Speed Sensor
- 4. Control System
- Antiskid Control Valve

To form the flywheel system, the "Basic Control System" is combined with the 3a. Airplane System (Flywheel), 4a. Wheel and Tire System (Flywheel), and the 9a. Runway System. To form the three degree system, the "Basic Control System" is combined with the 3b. Airplane System (3 Degree), 4b. Wheel and Tire System (3 Degree), 8. Horizontal Tail Control System, and 9a. Runway System. The six degree system incorporates two separate "Basic Control Systems" and two separate 4c. Wheel and Tire Systems. These are combined with a 3c. Airplane System (6 Degree) which utilizes the

8. Horizontal Tail Control and 9c. Runway System (6 Degree). The model flow diagrams are shown in Figures 64 , 65 , and 66 . When utilizing the "Basic Control Systems" with the six degree system, the variables communicating with the airplane model are reidentified to correspond to the right or left side of the airplane. Thus, X_{AXR} is X_{AX} in the right side and X_{AXL} is X_{AX} in the left side.

The high degree of modularity used in this analysis is desirable for three reasons. The first reason is that it is easy to combine the component models together to form different types of overall systems. This is true not only from modeling considerations but especially from programming aspects. As an example, the only basic change required to accommodate a twin or tandem gear would be to remodel the strut in the airplane system. The second reason for modularity is the difficulty in being completely general. Should a component arise which is not described by the existing models, it is easy to create a new program for the new model without having to modify the operation of other systems. Thus, from the programming point of view, to incorporate a new wheel speed sensor for example, the new model program can fall back on the existing read, write, and logic statements of the existing wheel speed model. input and output variables of the new component model are automatically incorporated properly into the overall computational procedure, unless some new variables are defined. The third reason for using a modular approach is to take advantage of the different response characteristics of the different component models. In the digital procedures utilized for computation, essentially a "fixed step" integration technique is employed. The step size used in a "slow" responding model does not have to be as small as one used in a "fast" model. Thus, different component models utilize different size integration steps which minimizes the overall time of computation.

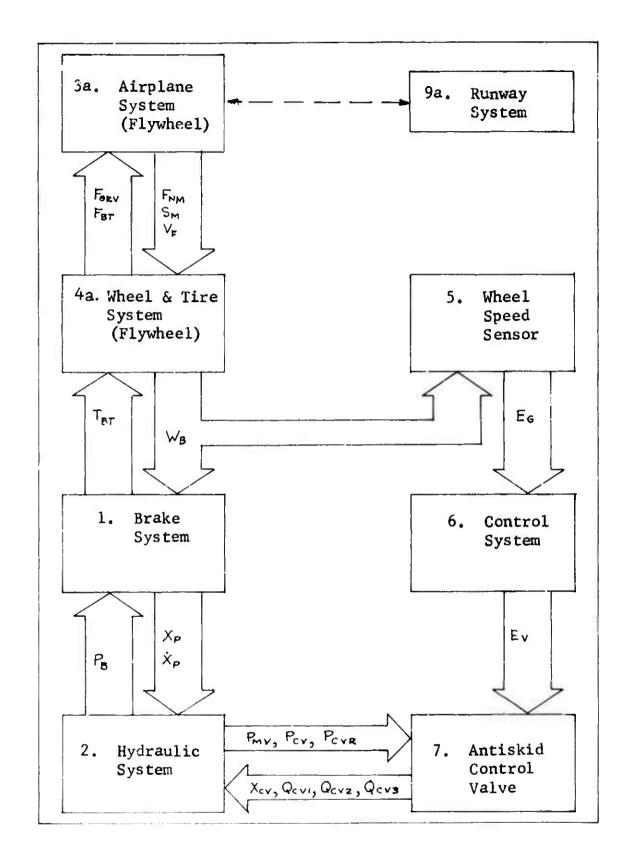
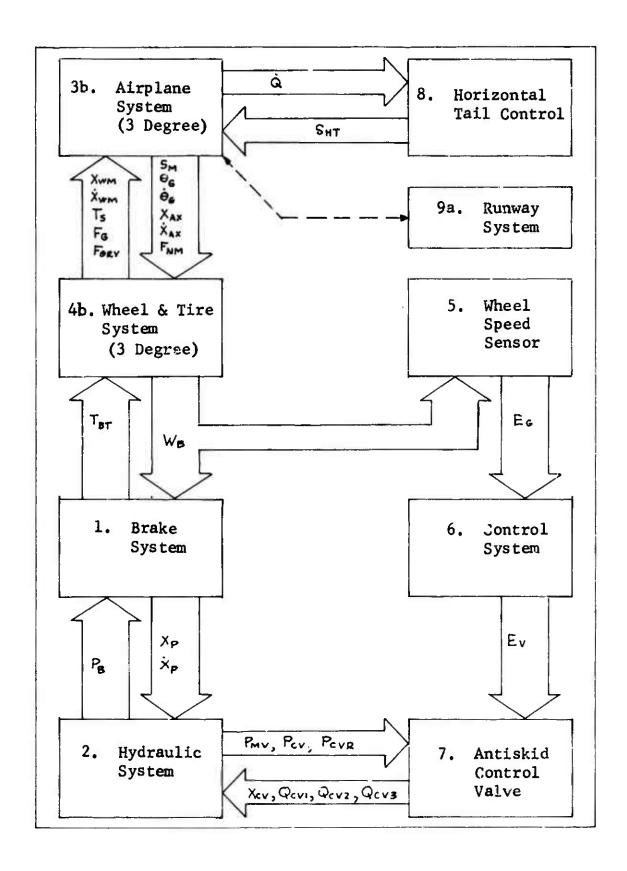
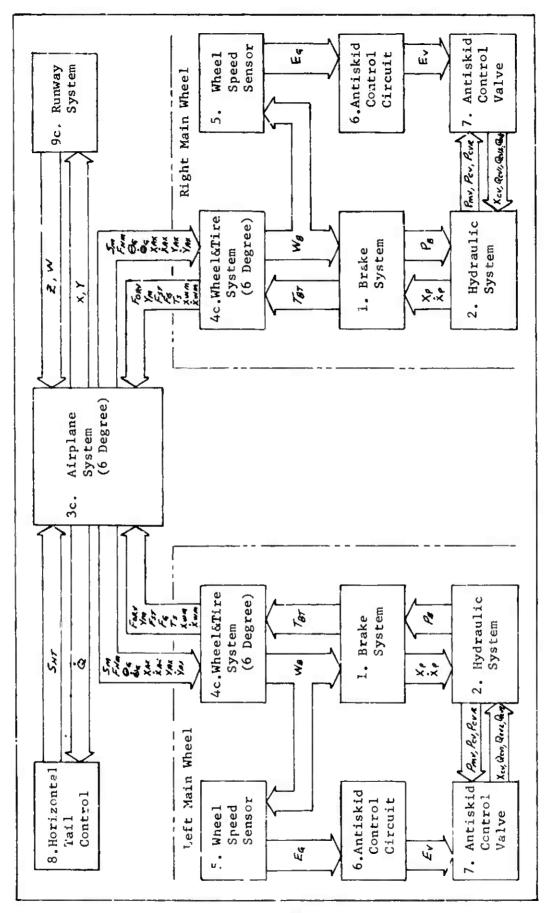


Figure 64 Flywheel System



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Figure 65 Three Degree System



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Figure 66 Six Degree System

SECTION V

SAMPLE CASE ANALYSIS

A digital computer solution of the composite total system mathematical models for the flywheel and three degree systems have been programed and checked out. In addition, during the development of the individual component mathematical models an analog computer program was used to conduct various explorations and prove the equations. Figure 67 presents an example of on-off antiskid operation as recorded from the analog computer program of the flywheel system. The analog computer results are shown because they are more easily related to aircraft operational data. The digital computer program is a solution of the same equations.

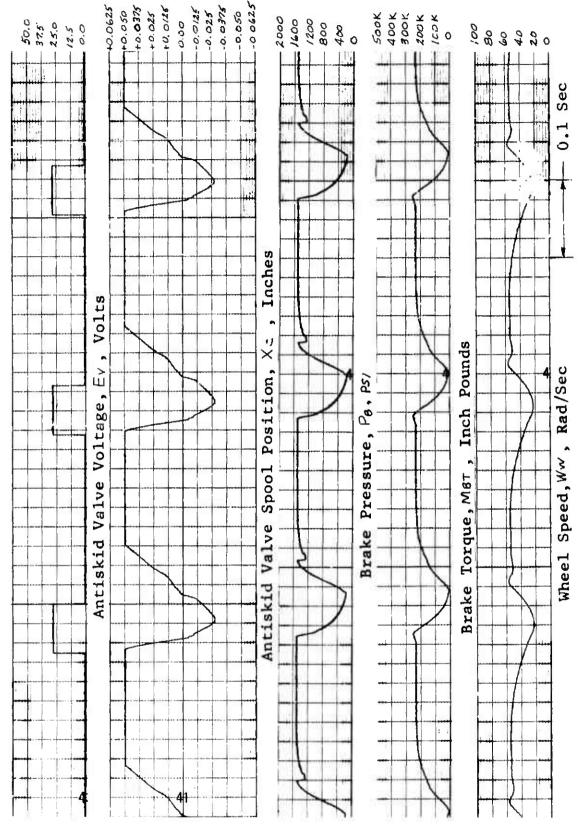
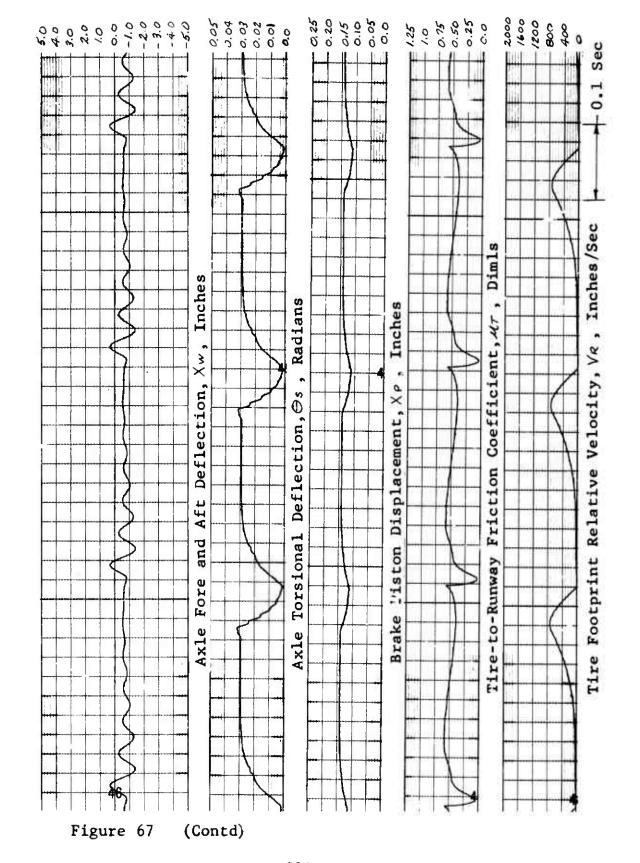


Figure 67 Analog Computer On-Off Antiskid Operation



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APPENDIX I

DERIVATION OF EQUATIONS DESCRIBING
THE OPERATION OF THE GOODYEAR ADAPTIVE
ELECTRONIC ANTISKID CONTROL CIRCUIT

The mathematical description of the operation of the Goodyear adaptive electronic antiskid control circuit as shown on Figure 50 is developed with conventional circuit analysis techniques using Kirchhoff's Laws. 68 is the schematic diagram from Figure 50 with the transistors and diodes shown in terms of their equivalent circuits and the various currents and voltages identified. The transistor and diode equivalent circuits are adaptations of equivalent circuits developed and described in references 13, 14 and 15. Some of the diode forward resistances are combined with other resistance in series with the diodes and are not shown separately. Also, since the current through RG (the output resistance of the wheel speed signal source) has three non-mutually influencing components, Rg is included in R3, Rog and R15 to simplify equations. Other simplifications will be described and discussed during the development of equations.

Referring to Figure 68, the circuit equations are developed as follows:

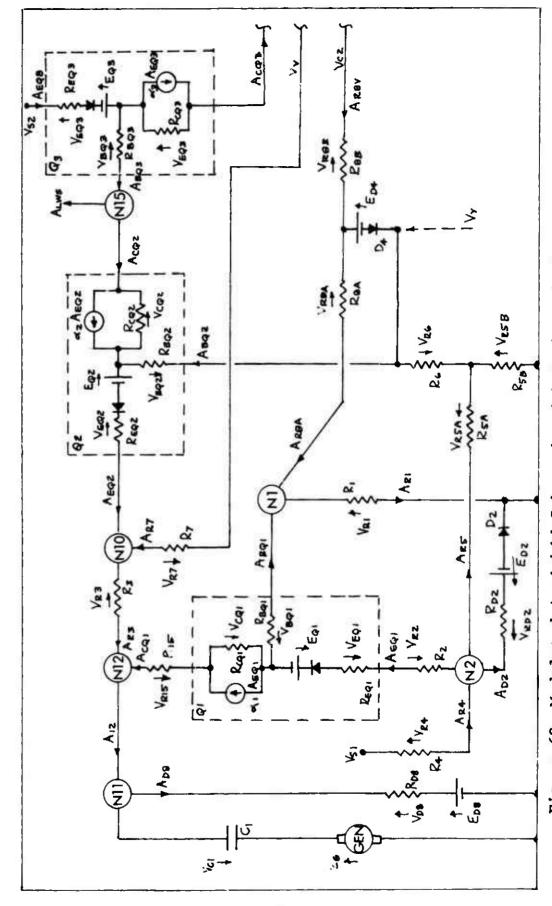
The voltage across capacitor C_1 is defined as:

(1)
$$V_{C_1} = \int V_{C_1} dt$$

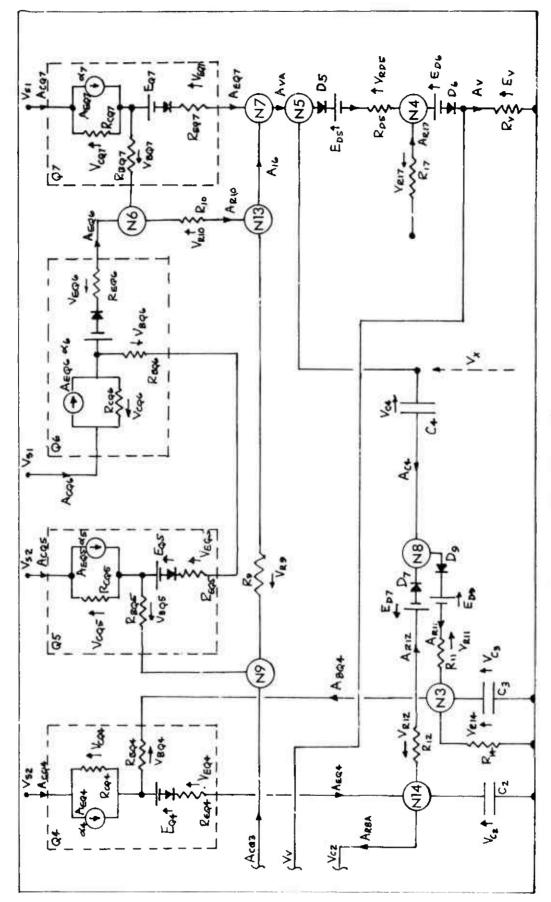
 A_{C_1} is the current through C_1 and C_1 is the capacitance. A_{C_1} is established by summing currents at node (W_1) as:

Using Ohm's law and summing voltages around the loop of which Rog is a part, Aog is established as:

(R10)
$$A08 = (E_G - Ve_1 - E_{08})/R_{08}$$
 FOR $(E_G - Ve_1 - E_{08}) > 0$
= 0 FUR $(E_G - Ve_1 - E_{08}) \leq 0$



Modulated Antiskid Schematic with Mathematical Identification and Incorporating Equivalent Circuits for Transistors and Diodes Figure 68



CONTROL SCORES NESSERVE CANDIDA ACCIDENT

Figure 68 (Contd)

Noting that because of diode \mathcal{O}_{∂} , $\mathcal{A}_{\mathcal{O}\partial}$ is restricted to positive values only.

To combine constants, write equation (R10) as:

(R10)
$$A08 = (E_G - V_{C_1})C_{620} - C_{621}$$
 FOR $(E_G - V_{C_1}) > C_{620}/C_{621}$
= 0 FOR $(E_G - V_{C_1}) = C_{620}/C_{621}$

By summing currents at Node (N12), current A_{i2} is established as:

Substituting equation (N12) into equation (N11) gives:

To compute $\mathcal{A}_{\mathcal{CQ}_l}$ it is desirable to first obtain equations for the voltages at the base and emitter of \mathcal{Q}_l in terms of the base and emitter currents and the appropriate voltage sources. The voltage at the base of \mathcal{Q}_l is $V_{\mathcal{R}_l}$. Summing currents at Node (N1) establishes current $\mathcal{A}_{\mathcal{R}_l}$ as:

Summing voltages around the loop R_I , R_{BR} , R_{BB} to V_{C2} gives: $V_{RBA} + V_{RBB} = V_{C2} - V_{RI}$. If the current through diode U_4 is assumed negligible, then $A_{RBA} = A_{RBB}$. (Because of the relative resistances, the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current through U_4 is a very small fraction of the current U_4 is a v

(N1)'
$$V_{R1} = R_1 \left(A_{BQ1} + \frac{V_{C2}}{R_{BA} r R_{BB}} \right) \left(1 + \frac{R_1}{R_{BA} r R_{BB}} \right)$$

The voltage at Node N2 is Eo2+1/Ro2. (Here two diodes 02 and 03 as shown on Figure 50 are combined in an equivalent single diode). Summing currents at Node N2 establishes current Ao2 as:

By Ohm's law, VRO? = AO2 RO2, VR4 = AR4 R4, and (VR5A + VR5A) = AR5 (R5A + R5B) (Note: Because of the relative resistances, AR6 is a very small component of the current in R5A and is assumed to be zero when computing VRO2.) Summing voltages around the appropriate loops establishes that VR4 = VSI - VRO2 - EO2 and VR5A + VR5B = VRO2 + EO2. By substitution into equation (N2) and solving for VRO2 gives:

$$V_{R02} = \frac{\left[\frac{V_{Si}}{R_4} - E_{02}\left(\frac{1}{R_4} + \frac{1}{R_{5A} + R_{5B}}\right) - A_{EQI}\right]}{\left(\frac{1}{R_{02}} + \frac{1}{R_4} + \frac{1}{R_{5A} + R_{5B}}\right)}$$

Summing voltages around the loop through which ABQ_1 (the base of current Q_1) flows results in:

By substituting VR2 = AEQ|R2, VEQ| = AEQ|REQ| and VBQ| = ABQ|RBQ| (From Ohm's Law) along with equations (N1)', (N2)', and the basic transistor relationship $AEQ| = (h_{EE}|r|)ABQ|$ into equation (Q-1) and solving for AEQ|

$$(Q-1)^{1} AEQI = C602 - C603 VC2, WHERE$$

$$C602 = \frac{\left\{ E_{02} \left[1 - \left(\frac{1}{R_{4}} + \frac{1}{R_{5}} \right) / \left(\frac{1}{R_{02}} + \frac{1}{R_{4}} + \frac{1}{R_{5}} \right) \right] + VS_{1} \left(\frac{1}{R_{01}} / \left(\frac{1}{R_{02}} + \frac{1}{R_{4}} + \frac{1}{R_{5}} \right) - EQ_{1} \right\}}{\left\{ R_{2} + REQ_{1} + \frac{R_{8}Q_{1}}{(h_{FE_{1}}+1)} + \frac{R_{1}}{(h_{FE_{1}}+1)} / \left(1 + \frac{R_{1}}{R_{8}} \right) + 1 / \left(\frac{1}{R_{02}} + \frac{1}{R_{4}} + \frac{1}{R_{5}} \right) \right\}}$$

$$\frac{R_{1}}{R_{1}+R_{8}}$$

$$\left\{R_{2}+R_{EQ_{1}}+\frac{R_{BQ_{1}}}{(h_{FE_{1}+1})}+\frac{R_{1}}{(h_{FE_{1}+1})}/(1+\frac{R_{1}}{R_{8}})+1/(\frac{1}{R_{0}z}+\frac{1}{R_{4}}+\frac{1}{R_{5}})\right\}$$

And where in the above $R_5 = R_{5/4} + R_{5/3}$ and $R_8 = R_{8/4} + R_{8/8}$.

For Q_1 to operate as a transistor, V_{CQ_1} must be positive. Using equation $(Q_{-1})^1$, the basic transistor characteristic (Q_2) $A_{CQ_1} = h_{FC_1} A_{CQ_1} / h_{FC_1} H)$ and by writing the voltage loop equation through 02, Q_1 , R_1S , C_1 and $G_{C}N$ it can be shown that V_{CQ_1} is positive for $(E_{C}-V_{C_1})$ negative; therefore, equation $(Q_{-1})^1$ is applicable only for $(E_{G}-V_{C_1}) < O$. Substituting (Q_{-1}) into (Q_{-2}) gives the following equation:

(Q-1C)
$$ACQI = CGO4 - CGO5 VC2$$
 FOR $(EG - Ve_1) = 0$
 $= 0$ FOR $(EG - Ve_1) \ge 0$
 $= 0$ FUR $Ve_2 \ge CGO4/CGO5$
 $CGO4 = CGO2 \left(\frac{hFE_1}{hFE_1 r_1}\right)$
 $CGO5 = CGO3 \left(\frac{hFE_1}{hFE_1 r_1}\right)$

By summing currents at node (110), current A_{R2} is established as:

To compute the components of AR3 (i.e., AEQ2 and AR7) it is desirable to have equation (N10) in a form where AR7 is expressed in terms of the appropriate voltages and resistances. By summing voltages around the loop RV, R7, R3, C1 and GEN, VR7 is established as:

(V7)
$$V_{R7} = E_V - V_{R3} - (E_6 - V_{C_1})$$

Substituting equation (V7) along with VR3 = AR3 R3 and VR7 = AR7 R7 into (N10) gives:

(N10)'
$$AR3 = \frac{AEQ2}{1 + R^3/R_7} + \frac{EV}{(R_1 + R_3)} - \frac{(E_6 - Vc_1)}{(R_1 + R_2)}$$

To combine constants write as:

To compute current $A \in \mathbb{Q}^2$, sum voltages around the loop through which $A \in \mathbb{Q}_2$ flows:

Here voltage $\forall y$ is the base voltage on Q2 and is either $(V_{C5}B - V_{R6})$ or $(V_{C2} - V_{R6}B - E_{04})$ whichever is the largest; therefore, there will be a version of equation (Q-2) for each of these conditions. To establish which condition exists, it is necessary to compute $(V_{R5}B - V_{R6})$ and $(V_{C2} - V_{R7}B - E_{04})$

During derivation of Equation (N2)' it was observed that VRSA + VRSB = VRO2 + EO2 and it was assumed that AR6 was small when compared to ARS. Using the same assumption VRSB is established as follows by Ohm's Law:

By substituting AR5 (R5A + R5B) = VR5A + VR5B into equation (R-5) above gives:

By substituting equation (N2)' for $V_{R}\rho_{2}$ and investigating the influence of $A_{EQ_{1}}$ within its allowable range, it can be seen that for practical purposes $V_{R}\rho_{S}$ is a constant.

To compute VRL, it can be seen that ARL equals ARL when V_{R} is VRSB-VRL; therefore, VRL-ARUZ RL by Ohm's law.

By Ohm's Law VRSS = ARBB RBB. Since the current through D4 is very small and may be assumed zero, and since ABQI is such a small component of the current through R1 that it can be assumed zero, by Ohm's Law:

Therefore:

To establish whether $V_Y = (V_{RSB} - V_{RG})$ UR

$$V_{y} = \left[V_{C2} \left(\frac{R_{1} + R_{8}A}{R_{1} + R_{8}A + R_{8}B} \right) - E_{D4} \right]$$

A voltage VB will be defined as follows:

where Cn above is defined as:

$$C_{m} = \left(\frac{R_{1} + R_{8A}}{R_{1} + R_{8A} + R_{8B}}\right)$$

Before proceeding with the computation of Ak3, the valve control amplifier and modulation circuit elements will be examined to develop equations for Ev and Vc2.

By summing currents at Node (N5) current Av_5 is established as:

The voltage at Node (N5) is defined as V_X . Summing voltages around the loop ℓv , ℓv , and ℓv gives:

$$(VX) \qquad V_X = E_V + E_{06} + V_{R05} + E_{05}$$

(EV)
$$E_V = A_{05} C_{406} + C_{407}$$

By summing currents at Node (N4), current $A_{R/7}$ is established as:

By substituting equations (N4), (N5), and (EV) into equation (VX) and by using Ohm^ts Law to establish that Ev = AvRv, VRII = ARII RII and VROS = AOS ROS, VX is established as:

By substituting equation (EV) into (N4) and using the relationships $E_V = A_V R_V$ and $V_{R17} = A_{R17} R_{17}$ EV is established as:

The operation of transistors Q2, Q3, Q5, Q6, and Q7 will now be considered to develop an equation for current AVA (Valve Control Amplifier Output Current).

By summing currents at Node (N7) current Av_A is established as:

By summing currents at Node (N13), current A_{IG} is established as:

By summing currents at Node (N6), current ARIO is established as:

By summing currents at Node (N9), current $\mathcal{H}_{\mathcal{A}}$ is established as:

(N9)
$$A_{R9} = A_{CQ3} - A_{BQ5}$$

Summing voltages around the loop, Req 7, Req 7 and Rio gives:

By using the relationships VRIO = ARIO RIO, VEQT = AEQT REQT and VBQT = ABQT RBQT as established by Ohm's law along ith the transistor characteristic AeQT = (heatt) ABQT and substitution equation (N6) into (V10) and solving for ABQT;

By substituting (V10) and (N6) into the relationship $VR_{I3} = RR_{I0} R_{I0}$

Summing voltages around the loop R10, Reae, Reae, Reae, Reae, Reae, Reae, and Re gives:

By substituting equations (A10) and (N9) into (V9) along with transistor characteristics Aeab = lhFeb+l Aeab and the Ohm's Law relationships VR4 = AR4 R4, VEQb = Aeab Reab and the Ohm's Law relationships VR4 = AR4 R4, VEQb = Aeab Reab and solving for Aeab:

Substituting equations (N13), (N6), (N9), and (V9)' into equation (N7) along with transistor characteristics AEQS = (hFESFI) ABQS and AEQO = (hFEOFI) ABQO and solving for AVA gives:

It should be noted that these operations involving Q5, Q6, and Q7 assume that Aca3 is large enough such that AvA is not negative and that the applicable supply voltages, VS1 and VS2, are large enough to keep Vca1, Vca6 and Vca5 positive at all times. The latter assumption can be proven to be true for the range of currents experienced during circuit operation. If Aca3 is not greater than C405/C404, insufficient voltage is developed across R9 to cause Q5, Q6 and Q7 to operate. For Aca3 less than C405/C404 all of Aca3 goes through R9 and AvA = Aca3; therefore, equation (N7) has two forms depending on the value of Aca3. Write these two forms as follows:

Supply voltage VS2 is large enough so that voltages VcQ3 and VeQ3 are always positive and a small leakage current Acq30 flows. All the equations developed here are for the increment of Acq3 above the leakage value.

By using the transistor characteristics Aca3 = hFe3 ABa3 Aca2 = Aea2 hFe2 / (hFe2+1)

And if at Node N15 $ALW_5=0$, $ABQ_3=Acq_2$ then:

(Q3)
$$A CQ3 = A EQ2 C606$$

WHERE $C606 = \frac{(hFe2)(hFe2)}{(hFe2 + 1)}$

The operation of the modulating circuit element will now be examined. To compute valve voltage EV from equation (N4) the value of current A_{05} which is established by Equation (N5) is required. Equation (N5) shows that a

component of A_{DS} is A_{C4} . Before developing equations for computing A_{C4} some observations relative to the operation of C4 and Q4 are helpful.

By summing currents at Node (N8) current Acq is established as:

(N8)
$$Ac4 = ARH - AR12$$

However, because of diodes D7 and D9 currents ARI and ARI have limitations depending upon the direction of voltage across the diodes. Summing voltages around the loop C3, R11, D9, C4 to VX gives:

(V11)
$$V_{C3} + V_{R11} + E_{09} + V_{C4} - V_{X} = 0$$

Substituting equation (V11) into the expression $V_{RH} = A_{RH} R_H$ as established by Chm's law gives:

Because of D9, $A_{RII} = 0$

Summing voltages around the loop C3, R12, D7, C4, to VX gives:

Substituting equation (V12) into the expression $V_{R/L} = A_{R/L} R_{LL}$ as established by Ohm's law gives:

Because of D7 ARIL = 0

Summing voltages around the loop C3 through Q4 to C2 gives:

Since the currents ABQ4 and AEQ4 in transistor Q4 are restricted to positive values only, voltages VBQ4 and VEQ4 are are always positive; therefore, equation (V-Q4) shows that VC2 is always less than VC3 by an amount at least equal to EQ4. Also, because of diodes D7 and D9, no current can flow from C3 through R11, D9, D7 and R12 to C2. For these circumstances, it is observed (1) that for Ac4 positive, all of Ac4 passes through R11 and all of Ac4 passes through R12 and all of Ac4 passes through

Since there cannot be positive ARII and positive ARI2 simultaneously, equation (N8) evolves to:

(N8)'
$$AC4 = ARII$$
 For $ARII > 0$
 $AC4 = 0$ FOR $ARII = 0$ AND $ARI2 = 0$
 $AC4 = -ARI2$ FOR $ARI2 > 0$

By substituting equations (N5), (VX)' and (N7)" into equations (V11)' and (V12)', equations for Ac4 are developed for each case.

The remaining equations for the modulation circuit element will now be developed. Substituting the expressions VBQ4 = ABQ4 RBQ4 and VEQ4 = AEQ4 REQ4 as established by Ohm's law along with the transistor characteristic $AEQ4 = (h_{EE4+1}) ABQ4$ into equation (V-Q4) and solving for ABQ4 gives:

$$(V-Q4)' \quad ABQ4 = \frac{V_{C3} - EQ4 - V_{C2}}{[R8Q4 + (hFE4 + 1) REQ4]}$$

$$= 0 \quad FOR (V_{C3} - EQ4 - V_{C2}) \ge 0$$

To combine constants, write equation (V-Q4) as:

$$(V-Q4) \quad A8Q4 = (V_{C3}-V_{C2}) C_{622} - C_{623}$$

$$FUR \ (V_{C3}-V_{C2}) > C_{623}/C_{622}$$

$$= 0 \quad FUR \ (V_{C3}-V_{C2}) \leq C_{623}/C_{622}$$

Also, since current AEQ4 is needed, define the transistor characteristic as equation Q4:

(Q-4)
$$AEQ4 = A8Q4 C614$$

where $C614 = (hFE4+1)$

By summing currents at Node (N14) current Ac_2 is established as:

Using the same assumption relative to ARIA as was made for equations (N1)' and (V8) and by Ohm's Law ARIA is established by equation (V8) as:

(V8)
$$AR8A = \frac{Vc2}{R_1 + R8A + R83}$$
 (Repeated)

By summing currents at Node (N3) current \mathcal{A}_{C3} is established as:

Current AR/4 is computed from $Vc_3 = PR/4 R/4$ established by Ohm's law and ABQ4 is computed from equation (V-Q4)' and Equation (Q-4).

Equation (N8) establishes that:

$$AR12 = -Ac4$$
 FUR $Ac4 \ge 0$
= 0 FUR $Ac4 \ge 0$

Substituting the above and equation (V8) into equation (N14) gives:

$$(N14)$$
' $Ac2 = AEQ4 + AC4 - Vc2 C618$ FOR $Ac4 = 0$
= $AEQ4 - Vc2 C618$ FOR $Ac4 \ge 0$

Similarly, by substituting the above ARII to ACA relationship and VC3 = ARIA RIA into equation (N3) AC3 is established as:

(N3)'
$$Ac3 = Ac4 - Vc3 C619 - A804$$
 FOR $Ac4 > 0$
= $-Vc3 C619 - A804$ FOR $Ac4 \leq 0$

The voltages across capacitors C2, C3 and C4 are established by:

$$(2) Vc_2 = \int Vc_2 dt$$

$$(3) Vc_3 = \int Vc_3 dt$$

$$(4) \qquad V_{C4} = \int V_{C4}^{\prime} dt$$

All of the equations describing the antiskid circuit's operation have now been developed; however, to obtain a computer solution of these equations, they have to be converted to a suitable form so that there are no "closed loops." Also, since the equations for AEQ2, AVA and Ac4 have different forms depending upon which circumstances exist, a procedure must be established to define which form of equations (Q2), (N7)" and (N8)' applies for each instance. There are twelve (12) possible combinations of circumstances as shown on Table 18 . The procedure for defining which condition exists will be to assume a condition and develop a set of equations based on the assumption. Using these equations, the assumption will be If the test is affirmative, the assumed condition If the test is negative, the assumption is incorrect and other assumed conditions are tested until an affirmative test result is obtained. To illustrate this procedure, the equations for circuit condition 4 will be developed:

For circuit condition 4 Ac4 is positive, Ac3 greater than C405/C404 and VB greater than zero. Substitute equation (N5) and the applicable version of equation (N7)" into equation (VX).

From equations (N8)' and (V11)' Ac4 is established as:

(N8) - P
$$Ac4 = \frac{V_X - V_{C4} - E_{04} - V_{C3}}{R_{II}}$$

Substitute (VX)'-4 into (N8)'-P and solve for Ac4

$$(N8)^{1}-P4$$

Now substitute equations (N5), (N7)" and (N8)'-P4 into equation (N4)' and solve for EV

Substituting equations (N4)'-4, (N10)', (Vy-1), and (Q3) into equation (Q-2) and solving for A_{EQ2} gives:

Substituting equations (Q-2)-4 and (Q3) into equation $(N8)^{1}-P4$ gives:

Substituting equations (Q-2), $(N10)^{1}$, $(N4)^{1}-4$, and (Vy-2) into equation (VB) results in:

Now using equations (VB)-4, (Q-2)-4, (Q3) and (N8)'-P4 the assumption that $A_{C4}>O$, $A_{C43}>C$ 405/C404 and $V_B>O$ can be tested. If the test is affirmative, then values for A_{C4} , A_{R3} and EV can be computed. If the test is negative another condition must be tested for.

Tables 14, 16 and 17 are a summary of test equations developed in the same manner as above. Since equation (Q3) establishes a linear relationship between Aea2 and Aca3 and since Aea2 needs to be computed as a step in the computation of Aea3, the test equations for Aca3 will be performed implicitly by computing Aea2 and comparing its computed value to C607 where C607 is defined as:

$$C607 = \frac{C405}{(C404)(C606)}$$

Currents Ac4 and Aeq2 are computed using the applicable test condition equations.

As shown on Figure 49 the locked wheel prevention circuit elements also have an input to the valve control amplifier. In the equations thus far it has been assumed that the locked wheel skid signal, Alws at node (N15), is zero. When computing the valve voltage, it is necessary that the non-zero value of Alws be accounted for. If Alws is not zero then equation (Q3) is:

Since A_{LWS} is a two valued variable (i.e. either zero or the value required to drive the amplifier as necessary to achieve full brake release) insofar as valve voltage computation is concerned, it can be considered as a current which can be added to A_{EQL} in Equation (Q3). If we define a current A_{VAL} , valve amplifier input current, as:

and treat this current like Aeax in equation (Q3) and if we substitute equations (Q3) and (N7)" into equation (N5) an equation for computing Aos is formulated for each circuit condition. Current Aos is then used in equation (N4) to compute EV. Table 15 lists the version of equation (N5) which is to be used for computing current Aos for each circuit condition.

Since the variables EG and VCl are always used in the form of their difference, we will define the difference as equation (5)

(5)
$$E_{G}-V_{C_{i}}=(E_{G}-V_{C_{i}})$$

For the cases where the antiskid control circuit mathematical model is used with the flywheel system or three dimensional airplane system, the flywheel velocity, VF, or the airplane velocity, X, as applicable, will be used as the airplane speed reference circuit element. The wheel speed comparison element will be described as follows:

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